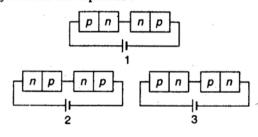
### **Physics**

- 1. Ionization power and penetration range of radioactive radiation increases in the order:
  - (a)  $\gamma$ ,  $\beta$ ,  $\alpha$  and  $\gamma$ ,  $\beta$ ,  $\alpha$  respectively
  - (b)  $\gamma$ ,  $\beta$ ,  $\alpha$  and  $\alpha$ ,  $\beta$ ,  $\gamma$  respectively
  - (c)  $\alpha$ ,  $\beta$ ,  $\gamma$  and  $\alpha$ ,  $\beta$ ,  $\gamma$  respectively
  - (d)  $\alpha$ ,  $\beta$ ,  $\gamma$  and  $\gamma$ ,  $\beta$ ,  $\alpha$  respectively
- 2. The half-life of a radioactive element is 3.8 days. The fraction left after 19 days will be:
  - (a) 0.124
- (b) 0.062
- (c) 0.093
- (d) 0.031
- 3. Two identical p-n junctions are connected in series in three different ways as shown below to a battery. The potential drop across the p-n junctions are equal in:

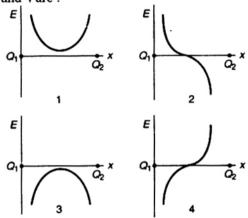


- (a) circuits 2 and 3 (b) circuits 1 and 2
- (c) circuits 1 and 3 (d) none of the circuit
- **4.** The temperature coefficient of a zener mechanism is:
  - (a) negative
- (b) positive
- (c) infinity
- (d) zero
- **5.** Identify the logic gate from the following truth table :

|   | Input      | Output |  |  |
|---|------------|--------|--|--|
| A | . <b>B</b> | Y      |  |  |
| 0 | 0          | 1      |  |  |
| 0 | 1          | 0      |  |  |
| 1 | 0          | 0      |  |  |
| 1 | 1          | 0      |  |  |

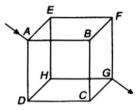
- (a) NOR gate
- (b) NOT gate
- (c) AND gate
- (d) NAND gate
- **6.** In Boolean algebra,  $\overline{A} \cdot \overline{B}$  is equal to :
  - (a)  $\overline{A} \cdot \overline{B}$
- (b)  $\overline{A} + \overline{B}$
- (c)  $A \cdot B$
- (d) A + B
- 7. Radar waves are sent towards a moving aeroplane and the reflected waves are received. When the aeroplane is moving towards the radar, the wavelength of the wave:
  - (a) decreases
  - (b) increases
  - (c) remains the same
  - (d) sometimes increases or decreases
- **8.** The transmission of high frequencies in a coaxial cable is determined by:
  - (a)  $\frac{1}{(LC)^{1/2}}$ , where L and C are inductance and capacitance
  - (b)  $(LC)^2$
  - (c) the impedance L alone
  - (d) the dielectric and skin effect
- **9.** The output stage of a television transmitter is most likely to be a :
  - (a) plate-modulated class C amplifier
  - (b) grid-modulated class C amplifier
  - (c) screen-modulated class C amplifier
  - (d) grid-modulated class A amplifier
- 10. The antenna current of an AM transmitter is 8 A when only the carrier is sent, but it increases to 8.93 A when the carrier is modulated by a single sine wave. Find the percentage modulation.
  - (a) 60.1%
- (b) 70.1%
- (c) 80.1%
- (d) 50.1%
- 11. Two point like charges  $Q_1$  and  $Q_2$  of whose strengths are equal in absolute value are placed at a certain distance from each other.

Assuming the field strength to be positive in the positive direction of x-axis, the signs of the charges  $Q_1$  and  $Q_2$  for the graphs (field strength versus distance) shown in Fig. 1, 2, 3 and 4 are:

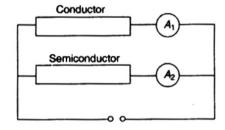


- (a)  $Q_1$  positive,  $Q_2$  negative; both positive;  $Q_1$ negative,  $Q_2$  positive; both negative
- (b)  $Q_1$  negative  $Q_2$  positive;  $Q_1$  positive,  $Q_2$ negative; both positive; both negative
- (c) Q<sub>1</sub> positive, Q<sub>2</sub> negative; both negative;  $Q_1$  negative,  $Q_2$  positive; both positive
- (d) both positive;  $Q_1$  positive,  $Q_2$  negative;  $Q_1$ negative,  $Q_2$  positive; both negative
- **12.** ABCD is a rectangle. At corners B, C and D of the rectangle are placed charges  $+10 \times 10^{-10}$  C,  $-20 \times 10^{-12}$  C and  $10 \times 10^{-12}$  C, respectively. Calculate the potential at the fourth corner. (The side AB = 4 cm and BC = 3 cm
  - (a) 1.65 V
- (b) 0.165 V
- (c) 16.5 V
- (d) 2.65 V
- 13. A parallel plate capacitor of capacitance 100 pF is to be constructed by using paper sheets of 1 mm thickness as dielectric. If the dielectric constant of paper is 4, the number of circular metal foils of diameter 2 cm each required for the purpose is:
  - (a) 40
- (b) 20
- (c) 30
- (d) 10
- 14. The electric field intensity E, due to an electric dipole of moment  $\vec{p}$ , at a point on the equatorial line is:
  - (a) parallel to the axis of the dipole and opposite to the direction of the dipole moment  $\vec{p}$

- (b) perpendicular to the axis of the dipole and is directed away from it
- (c) parallel to the dipole moment
- (d) perpendicular to the axis of the dipole and is directed towards it
- 15. Twelve wires of each of resistance  $6\Omega$  are connected to form a cube as shown in the figure. The current enters at a corner A and leaves at the diagonally opposite corner 6. The joint resistance across the corners A and G are:

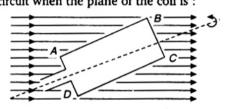


- (a) 12 Ω
- (b) 6Ω
- (c) 3Ω
- (d) 5Ω
- 16. A conductor and a semiconductor are connected in parallel as shown in the figure. At a certain voltage both ammeters register the same current. If the voltage of the DC source is increased then the :



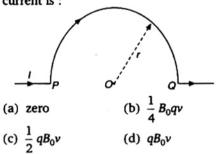
- (a) ammeter connected the will semiconductor register higher current than the ammeter connected to the conductor
- (b) ammeter connected to the conductor will register higher current than the ammeter connected to the semiconductor
- connected both (c) ammeters to semiconductor and conductor will register the same current
- (d) ammeters connected both to and will semiconductor conductor register no change in the current

- 17. A uniform copper wire of length 1 m and cross-sectional area 5 × 10<sup>-7</sup> m<sup>2</sup> carries a current of 1 A. Assuming that there are 8 × 10<sup>28</sup> free electron/m<sup>3</sup> in copper, how long will an electron take to drift from one end of the wire to the other?
  - (a)  $0.8 \times 10^3$  s
- (b)  $1.6 \times 10^3$  s
- (c)  $3.2 \times 10^3$  s
- (d)  $6.4 \times 10^3$  s
- 18. The temperature coefficient of resistance of a wire is 0.00125/K. At 300 K, its resistance is  $1 \Omega$ . The resistance of the wire will be  $2 \Omega$  at :
  - (a) 1154 K
- (b) 1100 K
- (c) 1400 K
- (d) 1127 K
- 19. A rectangular coil ABCD which is rotated at a constant angular velocity about an horizontal as shown in the figure. The axis of rotation of the coil as well as the magnetic field B are horizontal. Maximum current will flow in the circuit when the plane of the coil is:

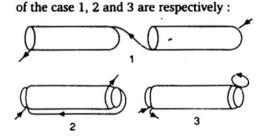


- (a) inclined at 30° to the magnetic field(b) perpendicular to the magnetic field
- (c) inclined at 45° to the magnetic field
- (d) parallel to the magnetic field
- 20. If the total emf in a thermocouple is a parabolic function expressed as  $E = at + \frac{1}{2}bt^2$ , which of the following relation does not hold good?
  - (a) neutral temperature  $t_n = -\frac{a}{b}$
  - (b) temperature of inversion,  $t_i = \frac{-2a}{b}$
  - (c) thermoelectric power P = a + bt
  - (d)  $t_n = \frac{a}{b}$
- 21. The proton of energy 1 MeV describes a circular path in plane at right angles to a uniform magnetic field of 6.28 × 10<sup>-4</sup> T. The mass of the proton is 1.7 × 10<sup>-27</sup> kg. The cyclotron frequency of the proton is very nearly equal to:
  - (a)  $10^7$  Hz
- (b)  $10^5 \text{ Hz}$
- (c) 10<sup>6</sup> Hz
- (d) 10<sup>4</sup> Hz

22. The magnetic field at the centre of a loop of a circular wire of radius r carrying current I may be taken as B<sub>0</sub>. If a particle of charge q moving with speed v passes the centre of a semicircular wire, as shown in figure, along the axis of the wire, the force on it due to the current is:

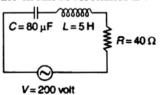


23. There are two solenoids of same length and inductance L but their diameters differ to the extent that one can just fit into the other. They are connected in three different ways in series. (1) They are connected in series but separated by large distance, (2) they are connected in series with one inside the other and senses of the turns coinciding, (3) both are connected in series with one inside the other with senses of the turns opposite as depicted in figures 1, 2 and 3, respectively. The total inductance of the solenoids in each



- (a)  $0, 4L_0, 2L_0$
- (b)  $4L_0$ ,  $2L_0$ , 0 (d)  $2L_0$ ,  $4L_0$ , 0
- (c) 2L<sub>0</sub>, 0, 4L<sub>0</sub>
- 24. From figure shown below a series L-C-R

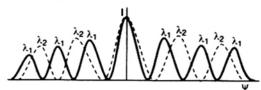
circuit connected to a variable frequency 200 V source. L = 5 H,  $C = 80 \mu\text{F}$  and  $R = 40 \Omega$ . Then the source frequency which drive the circuit at resonance is:



- (a) 25 Hz
- (c) 50 Hz
- (b)  $\frac{25}{\pi}$  Hz (d)  $\frac{50}{\pi}$  Hz
- 25. If the coefficient of mutual induction of the primary and secondary coils of an induction coil is 5 H and a current of 10 A is cut-off in  $5 \times 10^{-4}$  s, the emf inducted (in volt) in the secondary coil is:
  - (a)  $5 \times 10^4$
- (b)  $1 \times 10^5$
- (c)  $25 \times 10^5$
- (d)  $5 \times 10^6$
- 26. A voltage of peak value 283 V and varying frequency is applied to a series L-C-R combination in which  $R = 3\Omega$ , L = 25 mHand  $C = 400 \,\mu\text{F}$ . The frequency (in Hz) of the source at which maximum power is dissipated in the above, is:
  - (a) 51.5
- (b) 50.7
- (c) 51.1
- (d) 50.3
- 27. Four independent waves are represented by equations:
  - (1)  $X_1 = a_1 \sin \omega t$
  - (2)  $X_2 = a_1 \sin 2\omega t$
  - (3)  $X_3 = a_1 \sin \omega_1 t$
  - $(4) X_4 = a_1 \sin(\omega t + \delta)$

Interference is possible between waves represented by equations:

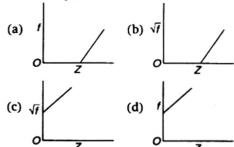
- (a) 3 and 4
- (b) 1 and 2
- (c) 2 and 3
- (d) 1 and 4
- 28. Following diffraction pattern was obtained using a diffraction grating using two different wavelengths  $\lambda_1$  and  $\lambda_2$ . With the help of the figure identify which is the longer wavelength and their ratios.



- (a)  $\lambda_2$  is longer than  $\lambda_1$  and the ratio of the longer to the shorter wavelength is 1.5
- (b)  $\lambda_1$  is longer than  $\lambda_2$  and the ratio of the longer to the shorter wavelength is 1.5
- (c)  $\lambda_1$  and  $\lambda_2$  are equal and their ratio is 1.0
- (d)  $\lambda_2$  is longer than  $\lambda_1$  and the ratio of the longer to the shorter wavelength is 2.5
- 29. In Young's double slit experiment, the interference pattern is found to have an

intensity ratio between bright and dark fringes is 9. This implies that :

- (a) the intensities at the screen due to two slits are 5 units and 4 units respectively
- (b) the intensities at the screen due to the two slits are 4 units and 1 units, respectively
- (c) the amplitude ratio is 7
- (d) the amplitude ratio is 6
- **30.** Rising and setting sun appears to be reddish
  - (a) diffraction sends red rays to earth at these times
  - (b) scattering due to dust particles and air molecules are responsible
  - (c) refraction is responsible
  - (d) polarization is responsible
- 31. The magnetic moment of the ground state of an atom whose open sub-shell is half-filled with five electrons is:
  - (a)  $\sqrt{35}\sqrt{\mu_B}$
- (b)  $35\mu_{R}$
- (c)  $35\sqrt{\mu_R}$
- (d)  $\mu_{B}\sqrt{35}$
- 32. Indicate which one of the following statements is not correct?
  - (a) Intensities of reflections from different crystallographic planes are equal
  - (b) According to Bragg's law higher order of reflections have high  $\theta$  values for a given wavelength of radiation
  - (c) For a given wavelength of radiation, there is a smallest distance between the crystallographic planes which can be determined
  - (d) Bragg's law may predict a reflection from a crystallographic plane to be present but it may be absent due to the crystal symmetry
- 33. Identify the graph which correctly represents the Moseley's law?



- **34.** Assuming f to be frequency of first line in Balmer series, the frequency of the immediate next (i.e., second) line is:
  - (a) 0.50 f
- (b) 1.35 f
- (c) 2.05 f
- (d) 2.70 f
- 35. The velocity of a particle at which the kinetic energy is equal to its rest energy is:
- (b)  $3\frac{c}{\sqrt{2}}$
- (c)  $\frac{(3c)^{1/2}}{2}$
- **36.** One electron and one proton is accelerated
- by equal potential. Ratio in their de-Broglie wavelength is:
  - (a) 1
- (b)  $\frac{m_e}{m_p}$ (d)  $\sqrt{\frac{m_e}{m_p}}$
- 37. Two electrons are moving in opposite direction with speeds 0.8 c and 0.4 c, where c is the speed of light in vacuum. Then the
  - relative speed is about: (a) 0.4 c
    - (b) 0.8c
  - (c) 0.9c
- (d) 1.2 c

- 38. A photo-sensitive material would emit electrons, if excited by photons beyond a threshold. To overcome the threshold, one would increase the:
  - (a) voltage applied to the light source
  - (b) intensity of light
  - (c) wavelength of light (d) frequency of light
- 39. The radius of nucleus is:
  - (a) proportional to its mass number (b) inversely proportional to its
  - number (c) proportional to the cube root of its mass number
  - (d) not related to its mass number
- **40.** Radio carbon dating is done by estimating in specimen the :
  - (a) amount of ordinary carbon still present (b) amount of radio carbon still present
    - (c) ratio of amount of <sup>14</sup>C<sub>6</sub> to <sup>12</sup>C<sub>6</sub> still present
    - (d) ratio of amount of 12C6 to 14C6 still present

## Chemistry

- 41. An ion leaves its regular site occupy a position in the space between the lattice sites is called: (a) Frenkel defect (b) Schottky defect
  - (d) vacancy defect (c) impurity defect
- **42.** The 8:8 type of packing is present in:
  - (a)  $MgF_2$ (c) KCl
- (b) CsCl (d) NaCl
- **43.** When a solid melts reversibly:
  - (a) H decreases (b) G increases
- (c) E decreases (d) S increases
- **44.** Enthalpy is equal to:
  - (a)  $T^2 \left[ \frac{\delta(G/T)}{\delta T} \right]_p$  (b)  $-T^2 \left[ \frac{\delta(G/T)}{\delta T} \right]_p$ (c)  $T^2 \left[ \frac{\delta(G/T)}{\delta T} \right]_V$  (d)  $-T^2 \left[ \frac{\delta(G/T)}{\delta T} \right]_V$
- 45. Condition for spontaneity in an isothermal process is:
  - (a)  $\Delta A + W < 0$
- (b)  $\Delta G + U < 0$
- (d)  $\Delta G U < 0$ (c)  $\Delta A + U > 0$

46. Given :

$$2C + 2O_2(g) \longrightarrow 2CO_2(g);$$

$$\Delta H = -787 \text{ kJ}$$

$$H_2(g) + \frac{1}{2}O_2(g) \longrightarrow H_2O(l);$$

$$C_2H_2(g) + 2\frac{1}{2}O_2(g) \longrightarrow 2CO_2(g) + H_2O(l);$$

$$C_2H_2(g) + 2\frac{1}{2}O_2(g) \longrightarrow 2CO_2(g) + H_2O(l);$$
  

$$\Delta H = -1310 \text{ kJ}$$

The heat of formation of acetylene is: (a) -1802 kJ(b) +1802 kJ(c) +237 kJ

47. Given the equilibrium system:

$$NH_4Cl(s) \longrightarrow NH_4^+(aq) + Cl^-(aq)$$

 $(\Delta H = + 3.5 \text{ kcal/mol}).$ 

(d) -800 kJ

 $\Delta H = -286 \text{ kJ}$ 

What change will shift the equilibrium to the right?

- (a) Decreasing the temperature
- (b) Increasing the temperature

- (c) Dissolving NaCl crystals in the equilibrium mixture
- (d) Dissolving NH<sub>4</sub>NO<sub>3</sub> crystals in the equilibrium mixture
- **48.** According to Arrhenius equation, the rate constant (k) is related to temperature (T) as:

(a) 
$$\ln \frac{k_2}{k_1} = \frac{E_a}{R} \left[ \frac{1}{T_1} - \frac{1}{T_2} \right]$$

(b) 
$$\ln \frac{k_2}{k_1} = -\frac{E_a}{R} \left[ \frac{1}{T_1} - \frac{1}{T_2} \right]$$

(c) 
$$\ln \frac{k_2}{k_1} = \frac{E_a}{R} \left[ \frac{1}{T_1} + \frac{1}{T_2} \right]$$

(d) 
$$\ln \frac{k_2}{k_1} = -\frac{E_a}{R} \left[ \frac{1}{T_1} + \frac{1}{T_2} \right]$$

- 49. Equivalent amounts of H<sub>2</sub> and I<sub>2</sub> are heated in a closed vessel till equilibrium is obtained. If 80% of the hydrogen can be converted to
  - HI, the  $K_c$  at this temperature is: (a) 64 (b) 16
- (c) 0.25 (d) 4
- **50.** For the reaction  $H_2(g) + I_2(g) \longrightarrow 2HI(g)$ ,

the equilibrium constant  $K_{\rho}$  changes with:

- the equilibrium constant  $K_p$  changes with (a) total pressure
- (b) catalyst
- (c) the amount H2 and I2
- (d) temperature
- 51. How long (in hours) must a current of 5.0 A be maintained to electroplate 60 g of calcium from molten CaCl<sub>2</sub>?(a) 27 h(b) 8.3 h
- (c) 11 h
   (d) 16 h
   52. For strong electrolytes the plot of molar conductance vs √C is:
  - (a) parabolic (b) linear
- (c) sinusoidal (d) circular

  53. If the molar conductance values of Ca<sup>2+</sup> and Cl<sup>-</sup> at infinite dilution are respectively 118.88 × 10<sup>-4</sup> m<sup>2</sup> mho mol<sup>-1</sup> and

 $77.33 \times 10^{-4}$  m<sup>2</sup> mho mol<sup>-1</sup> then that of CaCl<sub>2</sub> is (in m<sup>2</sup> mho mol<sup>-1</sup>):

- (a)  $118.88 \times 10^{-4}$  (b)  $154.66 \times 10^{-4}$  (c)  $273.54 \times 10^{-4}$  (d)  $196.21 \times 10^{-4}$
- **54.** The standard reduction potentials at 298 K for the following half reactions are given against each:

$$Zn^{2+}(aq) + 2e^{-} \rightarrow Zn(s)$$
  $E^{\circ} = -0.762 \text{ V}$ 

$$Cr^{3+}(aq) + 3e^{-} \rightarrow Cr(s)$$
  $E^{\circ} = -0.740 \text{ V}$ 

$$2H^{+}(aq) + 2e^{-} \rightarrow H_{2}(g)$$
  $E^{\circ} = 0.00 \text{ V}$ 

 $Fe^{3+}(aq) + 3e^{-} \rightarrow Fe^{2+}(aq) E^{\circ} = + 0.762 V$ 

The strongest reducing agent is:

- (a) Zn(s)
- (b) Cr(s)
- (c)  $H_2(g)$
- (d)  $Fe^{2+}(aq)$
- 55. The epoxide ring consists of which of the following:
  - (a) three membered ring with two carbon and one oxygen
    - (b) four membered ring with three carbon and one oxygen(c) five membered ring with four carbon and
    - one oxygen
      (d) six membered ring with five carbon and
- one oxygen

  56. In the Grignard reaction, which metal forms
  - an organometallic bond?
    (a) Sodium (b) Titanium
  - (c) Magnesium (d) Palladium
- 57. Phenol is more acidic than:
  - (a) p-chlorophenol (b) p-nitrophenol (c) o-nitrophenol (d) ethanol
- 58. Aldol condensation is given by:
  - Aldoi condensation is given by
    - (a) trimethylacetaldehyde
    - (b) acetaldehyde
    - (c) benzaldehyde(d) formaldehyde
- 59. Give the IUPAC name for

- (a) ethyl-4-oxoheptanoate
- (b) methyl-4-oxoheptanoate
- (c) ethyl-4-oxohexanoate
- (d) methyl-4-oxohexanoate
- 60. In which of the below reaction do we find α, β-unsaturated carbonyl compounds undergoing a ring closure reaction with conjugated dienes?
  - (a) Perkin reaction
  - (b) Diels-Alder reaction
  - (c) Claisen rearrangement
  - (d) Hofmann reaction

| 61               | . The catalyst used in Rosenmund reaction is :  |      | (c)         |
|------------------|---|------|-------------|
|                  | (a) Zn/Hg (b) Pd/BaSO <sub>4</sub>  |      | (d)         |
|                  | (a) Zn/Hg (b) Pd/BaSO <sub>4</sub> (c) Raney Ni (d) Na in ethanol                     | 71.  | In T        |
| 62               | $(CH_2CO)_2O + RMgX \xrightarrow{H_2O}$ ?   |      | (a)         |
|                  | (a) ROOC(CH <sub>2</sub> )COOR  |      | (b)         |
|                  | (b) RCOCH, CH, COOH   |      | (c)         |
|                  | (c) RCOOR   |      | (d)         |
|                  | (d) RCOOH   | 72.  | Whi         |
| 63.              | Identify, which of the below does not possess   |      | vola        |
|                  | any element of symmetry?  |      | (a)         |
|                  | (a) (+)(-) tartaric acid  |      | (c)         |
|                  | (b) Carbon tetrachloride (c) Methane  | 73.  | Αn          |
|                  | (d) Meso-tartaric acid  |      | proc        |
| 64.              | The weakest acid amongst the following is:  |      | elen        |
|                  | (a) CICH <sub>2</sub> COOH (b) HCOOH  |      | (a)         |
|                  | (c) FCH <sub>2</sub> CH <sub>2</sub> COOH (d) CH <sub>2</sub> (I)COOH                 |      | (a)         |
| 65.              | Urea on slow heating gives:   |      | (c)         |
|                  | (a) NH <sub>2</sub> CONHNO <sub>2</sub>   | 74.  | •           |
|                  | (d) NH <sub>2</sub> CONHCONH <sub>2</sub>   |      | wat         |
|                  | (c) HCNO  |      | (a)         |
|                  | (d) NH <sub>2</sub> CONH <sub>2</sub> · HNO <sub>3</sub>                              |      | (p)         |
| 00.              | Trans esterification is the process of:  (a) conversion of an aliphatic acid to ester |      | (c)<br>(d)  |
|                  | (b) conversion of an aromatic acid to ester   |      | (4)         |
|                  | (c) conversion of one ester to another ester  | 75.  | Whi         |
|                  | (d) conversion of an ester into its   |      | liga        |
|                  | components namely acid and alcohol  |      | (a)         |
| 67.              | The correct sequence of base strengths in   |      | (b)         |
|                  | aqueous solution is :   |      | (c)         |
|                  | (a) $(CH_3)_2NH > CH_3NH_2 > (CH_3)_3N$   | 76   | (d)         |
|                  | (b) $(CH_3)_3N > (CH_3)_2NH > CH_3NH_2$   | 76.  | A co<br>Whi |
|                  | (c) $(CH_3)_3N > CH_3NH_2 = (CH_3)_2NH$   |      | (a)         |
|                  | (d) $(CH_3)_2NH > (CH_3)_3N > CH_3NH_2$   |      | <b>\-</b> / |
| 68.              |   |      | (b)         |
|                  | diazoniumchloride is boiled, the product formed is :                                  |      | 1           |
|                  | (a) $C_6H_5CH_2OH$ (b) $C_6H_6 + N_2$   |      | (c)         |
|                  |   |      |             |
| 60               |   |      | (d)         |
| U <del>9</del> . | Carbylamine reaction is given by aliphatic :  (a) primary amine                       | 77.  | Whi         |
|                  | (b) secondary amine   | //.  | mag         |
|                  | (c) tertiary amine  |      | (a)         |
|                  | (d) quaternary ammonium salt  |      | (c)         |
| 70               | C <sub>6</sub> H <sub>5</sub> CHO NH <sub>3</sub> ?                                   | 78.  | The         |
| , <b>J</b> .     |   | , 0. | (a)         |
|                  | (a) $(C_6H_5CHN)_2CH \cdot C_6H_5$  |      | (a)         |

(b) C<sub>6</sub>H<sub>5</sub>NHCH<sub>3</sub>

- (c) C<sub>6</sub>H<sub>5</sub>CH<sub>2</sub>NH<sub>2</sub>
- (d)  $C_6H_5NHC_6H_5$
- 71. In TeCl<sub>4</sub>, the central atom tellurium involves:
  - a) sp<sup>3</sup> hybridisation
  - (b) sp<sup>3</sup>d hybridisation
  - (c) sp<sup>3</sup>d<sup>2</sup> hybridisation
  - (d) dsp<sup>2</sup> hybridisation
- 72. Which of the following compounds volatilises on heating?
  - a) MgCl<sub>2</sub>
- (b) HgCl<sub>2</sub>
  (d) FeCl<sub>3</sub>
- (c) CaCl<sub>2</sub>
- 3. A nuclear reaction of  $^{235}_{92}$ U with a neutron
- produces <sup>90</sup><sub>36</sub>Kr and two neutrons. Other element produced in this reaction is:
  - (a) <sup>137</sup>Te
- (b) 144 Cs
- (c) 137 Ba
- (d) 144 Ba
- 74. AgCl dissolves in a solution of NH<sub>3</sub> but not in water because :
  - (a) NH<sub>3</sub> is a better solvent than H<sub>2</sub>O
  - (b) Ag+ forms a complex ion with NH<sub>3</sub>
  - (c) NH<sub>3</sub> is a stronger base than H<sub>2</sub>O
     (d) the dipole moment of water is higher
- than NH<sub>3</sub> **75.** Which of the following is hexadentate ligand?
  - (a) Ethylene diamine
  - (b) Ethylene diamine tetra acetic acid
  - (c) 1, 10-phenanthroline
  - (d) Acetyl acetonato
- 76. A coordiante bond is a dative covalent bond. Which of the below is true?
  - (a) Three atom form bond by sharing their electrons
  - (b) Two atom form bond by sharing their electrons
  - (c) Two atoms form bond and one of them provides both electrons
  - (d) Two atoms form bond by sharing electrons obtained from third atom
- 77. Which of the following complex has zero magnetic moment (spin only)?
  - (a)  $[Ni(NH_3)_6]Cl_2$  (b)  $Na_3[FeF_6]$
  - (c)  $[Cr(H_2O)_6]SO_4$  (d)  $K_4[Fe(CN)_6]$ The IUPAC name of  $[Ni(PPh_3)_2Cl_2]^{2+}$  is:
- (a) bis dichloro (triphenylphosphine) nickel (II)

- (b) dichloro bis (triphenylphosphine) nickel
- (c) dichloro triphenylphosphine nickel (II)
- nickel phosphine (II)(d) triphenyl dichloride
- 79. Among the following the compound that is both paramagnetic and coloured is:
  - (a)  $K_2Cr_2O_7$
- (b)  $(NH_4)_2[TiCl_6]$

- (d)  $K_3[Cu(CN)_4]$ (c) VOSO<sub>4</sub>
- 80. On an X-ray diffraction photograph the intensity of the spots depends on:
  - (a) neutron density of the atoms/ions
  - (b) electron density of the atoms/ions
  - (c) proton density of the atoms/ions
  - (d) photon density of the atoms/ions

#### Mathematics<sup>'</sup>

- **81.** If the normal to the curve y = f(x) at (3, 4)makes an angle  $\frac{3\pi}{4}$  with the positive x-axis, then f'(3) is equal to:
  - (a) 1

(c) 1

- **82.** The function  $f(x) = x^2 e^{-2x}$ , x > 0. Then the maximum value of f(x) is:

- **83.** If  $(x + y) \sin u = x^2 y^2$ , then  $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y}$  is
  - equal to:
- (b) cosec u
- (a) sin u (c) 2 tan u
- (d) 3 tan u
- 84. The angle between the tangents at those points on the curve  $x = t^2 + 1$  $y = t^2 - t - 6$  where it meets x-axis is:
  - (a)  $\pm \tan^{-1} \left( \frac{4}{29} \right)$  (b)  $\pm \tan^{-1} \left( \frac{5}{49} \right)$
  - (c)  $\pm \tan^{-1} \left( \frac{10}{49} \right)$  (d)  $\pm \tan^{-1} \left( \frac{8}{29} \right)$
- **85.** The value of  $\int_0^4 |x-3| dx$  is equal to :
  - (a) 2

- 86. The area of the region bounded by the straight lines x = 0 and x = 2, and the curves  $y = 2^x$  and  $y = 2x - x^2$  is equal to:

- $(a) \frac{2}{\log 2} \frac{4}{3}$
- (b)  $\frac{3}{\log 2} \frac{4}{3}$
- (c)  $\frac{1}{\log 2} \frac{4}{3}$  (d)  $\frac{4}{\log 2} \frac{3}{2}$
- **87.** The value of  $\int_0^\infty \frac{dx}{(a^2 + x^2)}$  is equal to :
  - (a)  $\frac{\pi}{2}$
- (b)  $\frac{\pi}{2\pi}$
- (d)  $\frac{1}{2a}$
- **88.** The value of the integral  $\int e^x \left(\frac{1-x}{1-x^2}\right)^2 dx$  is:
  - (a)  $e^x \left( \frac{1-x}{1+x^2} \right) + c$  (b)  $e^x \left( \frac{1+x}{1+x^2} \right) + c$
  - (c)  $\frac{e^x}{1-e^x} + c$  (d)  $e^x(1-x) + c$
- **89.** If  $x \sin\left(\frac{y}{x}\right) dy = \left[y \sin\left(\frac{y}{x}\right) x\right] dx$  $y(1) = \frac{\pi}{2}$ , then the value of  $\cos\left(\frac{y}{x}\right)$  is equal

to:

(a) x

- (b)  $\frac{1}{x}$
- (c)  $\log x$
- 90. The differential equation of the system of all circles of radius r in the xy plane is:

(a) 
$$\left[1 + \left(\frac{dy}{dx}\right)^3\right]^2 = r^2 \left(\frac{d^2y}{dx^2}\right)^2$$

(b) 
$$\left[1 + \left(\frac{dy}{dx}\right)^3\right]^2 = r^2 \left(\frac{d^2y}{dx^2}\right)^3$$

$$(c) \left[ 1 + \left( \frac{dy}{dx} \right)^2 \right]^3 = r^2 \left( \frac{d^2 y}{dx^2} \right)^2$$

$$(d) \left[ 1 + \left( \frac{dy}{dx} \right)^2 \right]^3 = r^2 \left( \frac{d^2 y}{dx^2} \right)^3$$

91. The general solution of the differential equation  $\frac{d^2y}{dx^2} + 2\frac{dy}{dx} + y = 2e^{3x}$  is given by:

(a) 
$$y = (c_1 + c_2 x) e^x + \frac{e^{3x}}{9}$$

(b) 
$$y = (c_1 + c_2 x) e^{-x} + \frac{e^{-3x}}{8}$$

(c) 
$$y = (c_1 + c_2 x) e^{-x} + \frac{e^{3x}}{8}$$

(d) 
$$y = (c_1 + c_2 x) e^x + \frac{e^{-3x}}{8}$$

92. The solution of the differential equation  $ydx + (x - y^3) dy = 0$  is:

(a) 
$$xy = \frac{1}{3}y^3 + c$$
 (b)  $xy = y^4 + c$ 

(b) 
$$xy = y^4 + c$$

(c) 
$$y^4 = 4xy + c$$
 (d)  $4y = y^3 + c$ 

(d) 
$$4y = y^3 + c$$

93. The number of integral solutions  $x_1 + x_2 + x_3 = 0$ , with  $x_i \ge -5$ , is: (a)  ${}^{15}C_2$  (b)  ${}^{16}C_2$ 

(c)  $^{17}C_2$ 

**94.** Let  $A = \{1, 2, 3, ..., n\}$  and  $B = \{a, b, c\}$ , then the number of functions from A to B that are onto is:

- (a)  $3^n 2^n$
- (b)  $3^n 2^n 1$
- (c)  $3(2^n-1)$
- (d)  $3^n 3(2^n 1)$

95. Everybody in a room shakes hands with everybody else. The total number of hand shakes is 66. The total number of persons in the room is:

(a) 9

(b) 12

- (c) 10
- (d) 14

 $G = \{1, 3, 7, 9\}$ a group multiplication modulo 10, the inverse of 7 is:

(a) 7

(b) 3

(c) 9

(d) 1

97. A box contains 9 tickets numbered 1 to 9 inclusive. If 3 tickets are drawn from the box one at a time, the probability that they are alternatively either {odd, even, odd} or {even, odd, even} is:

- (a)  $\frac{5}{17}$
- (c)  $\frac{5}{16}$  (d)  $\frac{5}{10}$

**98.** If  $P(A) = \frac{1}{12}$ ,  $P(B) = \frac{5}{12}$  and  $P\left(\frac{B}{A}\right) = \frac{1}{15}$ , then

 $P(A \cup B)$  is equal to :

- (a)  $\frac{89}{180}$
- (b)  $\frac{90}{180}$
- (c)  $\frac{91}{180}$
- (d)  $\frac{92}{180}$

99. If the probability density function of a random variable X is  $f(x) = \frac{x}{2}$  in  $0 \le x \le 2$ , then P(X > 1.5 | X > 1) is equal to :

- (a)  $\frac{7}{16}$
- (c)  $\frac{7}{12}$

100. If X follows a binomial distribution with parameters n = 100 and  $p = \frac{1}{2}$ , then P(X = r)is maximum when r is equal to:

- (a) 16
- (b) 32
- (c) 33
- (d) none of these

**101.** If  $A(\theta) = \begin{bmatrix} 1 & \tan \theta \\ -\tan \theta & 1 \end{bmatrix}$  and AB = I, then  $(\sec^2 \theta) B$  is equal to :

- (a)  $A(\theta)$
- (b)  $A\left(\frac{\theta}{2}\right)$
- (c)  $A(-\theta)$
- (d)  $A\left(\frac{-\theta}{2}\right)$

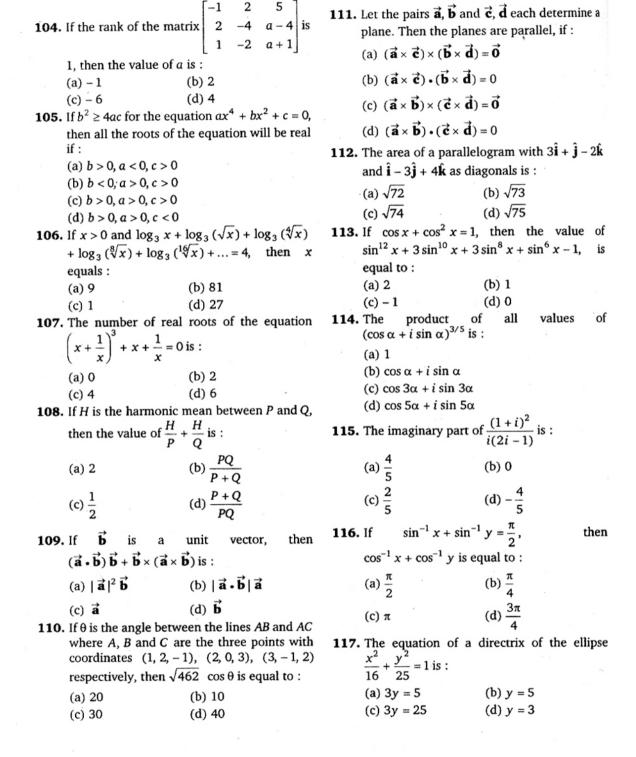
**102.** If x = -5 is a root of  $\begin{vmatrix} 2x + 1 & 4 & 8 \\ 2 & 2x & 2 \end{vmatrix} = 0$ ,

then the other roots are:

- (a) 3, 3.5
- (b) 1, 3.5
- (c) 1, 7
- (d) 2, 7

**103.** The simultaneous equations Kx + 2y - z = 1, (K - I)y - 2z = 2 and (K + 2)z = 3 have only one solution when:

- (a) K = -2
- (b) K = -1
- (c) K = 0
- (d) K = 1



# HINTS & SOLUTIONS

# **Physics**

Because of large mass and large velocity, α-particles have large ionising power. Each α-particle produces thousands of ions before being absorbed. The β-particles ionise the gas through which they pass, but their ionising power is only  $\frac{1}{100}$  th that of

α-particles. γ-rays have got small ionising power.

Because of large mass, the penetrating power of α-particles is very small, it being 1/100 times that to  $\beta$ -rays and 1/10000 times that of  $\gamma$ -rays.  $\alpha$ -particles can be easily stopped by an Aluminium sheet, only 0.02 mm thick. B-particles have very small mass, so their penetrating power is large. γ-rays have very large penetrating power.

In time t = T,  $N = \frac{N_0}{2}$ 

In another half-life, (i.e., after 2 half-lives)

$$N = \frac{1}{2} \frac{N_0}{2} = \frac{N_0}{4} = N_0 \left(\frac{1}{2}\right)^2$$

After yet another half-life (i.e., after 3 half-lives)  $N = \frac{1}{2} \left( \frac{N_0}{4} \right) = \frac{N_0}{8} = N_0 \left( \frac{1}{2} \right)^3$  and so on. Hence, after n half-lives

$$N = N_0 \left(\frac{1}{2}\right)^n$$
$$= N_0 \left(\frac{1}{2}\right)^{t/T}$$

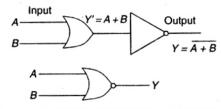
where  $t = n \times T = \text{total time of } n \text{ half-lives.}$ 

Here, 
$$n = \frac{t}{T} = \frac{19}{3.8}$$
  
= 5

.. The fraction left

$$\frac{N}{N_0} = \left(\frac{1}{2}\right)^n = \left(\frac{1}{2}\right)^5 = \frac{1}{32}$$
$$= 0.031$$

- In circuit 2, each p-n junction is reverse 3. biased, some current will flow giving equal potential difference across each p-n junction diode. In circuit 3, each p-n junction is forward biased, hence same current flows, giving same potential difference across p-n junctions.
- Zener breakdown occurs in heavily doped p-n junction. The temperature coefficient of the zener mechanism is negative or the breakdown voltage for a particular diode decreases with increasing temperature.
- NOR gate is a combination of OR gate and NOT gate. In other words, output of OR gate is connected to the input of a NOT gate as shown in figure. Note that output of OR gate is inverted to form NOR gate. This is illustrated in the truth table for NOR gate. It is clear that truth table for NOR gate is developed by inverting the output of the OR gate.



| Inj | out | Output |        |  |
|-----|-----|--------|--------|--|
| A   | В   | OR(Y') | NOR(Y) |  |
| 0   | 0   | 0      | 1      |  |
| 1   | 0   | 1      | 0      |  |
| 0   | 1   | 1      | , 0    |  |
| 1   | 1   | 1      | 0      |  |

The Boolean expression for NOR function is Y = A + B

According to De-Morgan's theorem

$$\overline{A} \cdot \overline{B} = (\overline{A + B})$$

$$(\overline{\overline{A} \cdot \overline{B}}) = (\overline{A + B})$$

$$= (A + B) \qquad (\because \overline{A} = A)$$
$$(\overline{\overline{A} \cdot \overline{B}}) = (A + B)$$

7. Here,  $v_s = 0$  and  $v_L$  is negative where  $v_s$  is velocity of source and  $v_L$  is velocity of listener (aeroplane)

$$v_s = 0$$
  $v_L (-)$ 

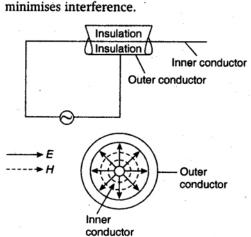
If apparent frequency is  $\nu'$  and  $\nu$  is actual frequency, then

$$v' = \frac{v - (-v_L)}{v} v$$
$$= \frac{v + v_L}{v} v$$

i.e.,

So, apparent frequency will increase, it means apparent wavelength will decrease.

Basically, a coaxial cable consists of a hollow (outer) cylindrical conductor surrounding a single (inner) conductor along its axis. The two conductors are well insulated from each other. The electric field (**E**) and magnetic field (**H**) at the cross-sections are shown by solid lines and dotted lines, respectively. The outer conductor acts as the shield and



Different kinds of dielectric materials, such as teflon and polythene are covered over copper wire, it acts as a spacer.

In the transmission of power through coaxial cable, the dielectric medium separating the inner conductor from outer one plays a vital

role. These dielectric materials are good insulators only at low frequencies. As the frequency increases, the energy loss becomes significant. That is why a coaxial cable can be used effectively for transmission upto a frequency of 20 MHz.

A steady signal flowing in a wire, uniformly distributes itself throughout the cross-section of the wire. A high frequency signal, on the other hand distributes itself uniformly, there being a concentration of current on the outer surface of the conductor. If the frequency of the current is very high, the current is almost wholly confined to the surface layers. This is called 'Skin effect'.

- 9. Because of their inherent distortion class C amplifiers are never used as audio amplifiers, but they are primarily employed in the final stage of TV transmitters. Also, owing to low efficiency of class A operations, these amplifiers are not employed where large RF (radio frequency) power is involved e.g., to excite transmitting antenna. In such cases class C amplifiers are used, since a class C amplifier has a very high efficiency, it can deliver more load power. In out put stage of a TV transmitter grid modulated class C amplifier is used.
- 10. The power dissipated in any circuit is a function of the square of voltage across the circuit and the effective resistance of the circuit. Equation of AM wave reveals that it has three components of amplitude  $E_c$ ,  $mE_c/2$  and  $mE_c/2$ . Clearly, power output must be distributed among these components.

Carrier Power, 
$$P_C = \frac{(E_c/\sqrt{2})^2}{R} = \frac{E_c^2}{2R}$$

Total power of side bands,

$$P_{S} = \frac{(mE_{c}/2\sqrt{2})^{2}}{R} + \frac{(mE_{c}/2\sqrt{2})^{2}}{R}$$

$$= \frac{m^{2}E_{c}^{2}}{4R}$$

$$\frac{P_{S}}{P_{C}} = \frac{1}{2}m^{2}$$

and 
$$P_T = P_C + P_S = P_C \left( 1 + \frac{m^2}{2} \right)$$

$$\frac{P_T}{P_C} = 1 + \frac{m^2}{2}$$

or 
$$\left(\frac{I_T}{I_A}\right)^2 = 1 + \frac{m^2}{2}$$

Given that,  $I_T = 8.93 \text{ A}$ ,  $I_C = 8 \text{ A}$ , m = ?

$$\therefore \qquad \left(\frac{8.93}{8}\right)^2 = 1 + \frac{m^2}{2}$$

or 
$$1.246 = 1 + \frac{m^2}{2}$$

or 
$$\frac{m^2}{2} = 0.246$$
  
or  $m = \sqrt{2 \times 0.246} = 0.701$ 

=70.1%

The situation is summarised in figure. AB = DC = 4 cm,BC = AD = 3 cm,AC = 5 cm.

Now, potential at A

Now, potential at A
$$V_A = \frac{1}{4\pi\epsilon_0} \frac{q_B}{AB} + \frac{1}{4\pi\epsilon_0} \cdot \frac{q_C}{AC} + \frac{1}{4\pi\epsilon_0} \cdot \frac{q_D}{AD}$$

$$= \frac{1}{4\pi\epsilon_0} \left[ \frac{10 \times 10^{-12}}{4 \times 10^{-2}} - \frac{20 \times 10^{-12}}{5 \times 10^{-2}} + \frac{10 \times 10^{-12}}{3 \times 10^{-2}} \right]$$

$$= 9 \times 10^9 \times 10^{-10} \left[ \frac{10}{4} - \frac{20}{5} + \frac{10}{3} \right]$$

$$= \frac{9 \times 10^{-1} \times 11}{6}$$
$$= 16.5 \times 10^{-1} = 1.65 \text{ V}$$

13. The arrangement of n metal plates separated by dielectric acts as parallel combination of (n-1) capacitors.

Therefore, 
$$C = \frac{(n-1)K\epsilon_0 A}{d}$$
  
Here,  $C = 100 \text{ pF}$ 

$$=100\times10^{-12} \text{ F}$$

$$K = 4, \ \varepsilon_0 = 8.85 \times 10^{-12} \,\mathrm{C}^2/\mathrm{Nm}^2$$

$$A = \pi r^2 = 3.14 \times (1 \times 10^{-2})^2$$

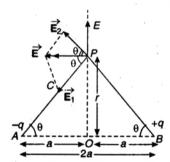
$$d = 1 \,\mathrm{mm} = 1 \times 10^{-3}$$

$$(n-1) \times 4 \times 8.85 \times 10^{-12}$$

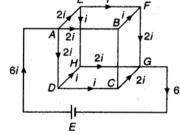
$$\therefore \ 100 \times 10^{-12} = \frac{\times 3.14 \times (1 \times 10^{-2})^2}{1 \times 10^{-3}}$$
or
$$n = \frac{1111.156}{111.156}$$

14. Consider an electric dipole consisting of two point charges -q and +q separated by a small distance AB = 2a with centre at O.

≈ 10



As shown in figure, on equatorial line, the resultant electric field  $\vec{E}$  of  $\vec{E}_1$  and  $\vec{E}_2$  is parallel to the axis of the dipole but opposite to the direction of the dipole moment p as it is directed from negative charge to positive charge.



15.

Let ABCLEFGH be the skeleton cube formed by joining twelve equal wires each of resistance r. Let the current enters the cube at corner A and after passing through all twelve wires, let the current leaves at G, a corner diagonally opposite to corner A.

For the sake of convenience, let us suppose that the total current is 6i. At A, this current is divided into three equal parts each (2i) along AE, AB and AD as the resistance along these paths are equal and their end points are equidistant from exit point G. At the points E, B and D, each part is further divided into two equal parts each part equal to i. The distribution of current in the various arms of skeleton cube is shown according to Kirchhoff's first law. The current leaving the cube at G is again 6i.

Applying Kirchhoff's second law to the closed circuit ADCGA, we get

$$2ir + ir + 2ir = E$$
or
$$5ir = E \qquad ...(i)$$

where *E* is the emf of the cell of neglegible internal resistance.

If R is the resistance of the cube between the diagonally opposite corners A and G, then according to Ohm's law, we have

$$6i \times R = E$$
 ...(ii)

From Eqs. (i) and (ii), we have

or 
$$R = \frac{5}{6}r$$
Here, 
$$r = 6\Omega$$

$$R = \frac{5}{6} \times 6$$
or 
$$R = 5\Omega$$

- 6. If the voltage of the DC source is increased then both conductor and semiconductor registers same current i.e., semiconductor is in forward biased condition and it conducts. So, ammeters connected to both semiconductor and conductor will register the same current.
- Consider a conductor of length l and of uniform area of cross-section A.
  - ... Volume of the conductor = Al

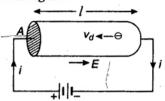
If n is the number of free electrons per unit volume of the conductor, then total number of free electrons in the conductor = Aln. If e is the charge on each electron, then total charge on all the free electrons in the conductor, q = Alne.

Let a constant potential difference V is applied across the ends of the conductor with the help of a battery.

The electric field set up across the conductor is given by

$$E = V/l$$

Due to this field, the free electrons present in the conductor will begin to move with a drift velocity  $v_d$  towards the left hand side as shown in figure.



Therefore, time taken by the free electrons to cross the conductor,

$$t = \frac{l}{v_d}$$

Hence, current  $i = \frac{q}{t} = \frac{Alne}{l/v_A}$ 

or 
$$i = Anev_d$$

Here, i = 1 A,  $n = 8 \times 10^{28} \text{ electron/m}^3$ 

$$A = 5 \times 10^{-7} \text{ m}^2$$

$$\Rightarrow$$
 1 = 8 × 10<sup>28</sup> × 1.6 × 10<sup>-19</sup> × 5 × 10<sup>-7</sup> ×  $\nu_d$ 

or 
$$v_d = \frac{1}{8 \times 10^{28} \times 1.6 \times 10^{-19} \times 5 \times 10^{-7}}$$

Now, 
$$t = \frac{l}{v_d}$$
  
=  $8 \times 10^{28} \times 1.6 \times 10^{-19} \times 5 \times 10^{-7}$   
=  $64 \times 10^2$   
=  $6.4 \times 10^3$  s

**18.** The resistance  $R_t$  of a metal conductor at temperature  $t \, ^{\circ}$ C is given by

$$R_t = R_0(1 + \alpha t + \beta t^2)$$

where  $\alpha$  and  $\beta$  are temperature coefficients of resistance.  $R_0$  is the resistance of conductor at 0°C. Their values vary from metal to metal. If the temperature t °C is not sufficiently large which is so in the most practical cases, the above relation may be expressed as

$$R_t = R_0(1 + \alpha t) \qquad ...(i)$$
Given, 
$$\alpha = 0.00125/K$$

$$R_{200} = 1 \Omega$$

From Eq. (i), we have

$$1 = R_0(1 + 0.00125 \times 300)$$
 ...(ii)

and, 
$$2 = R_0(1 + 0.00125 \times T)$$
 ...(iii)

$$\therefore \frac{2}{1} = \frac{1 + 0.00125 \times T}{1 + 0.00125 \times 300}$$

or 
$$2.75 = 1 + 0.00125 \times T$$

or 
$$T = \frac{1.75}{0.00125}$$

$$= 1400 K$$

19. As the coil is rotated, angle  $\theta$  (angle which normal to the coil makes with  $\vec{\mathbf{B}}$  at any instant t) changes, therefore magnetic flux  $\phi$  linked with the coil changes and hence an emf is induced in the coil. At this instant t, if e is the emf induced in the coil, then

$$e = -\frac{d\phi}{dt} = -\frac{d}{dt} (NAB \cos \omega t)$$

where N is number of turns in the coil.

or 
$$e = -NAB \frac{d}{dt} (\cos \omega t)$$

$$= -NAB (-\sin \omega t) \omega$$

or 
$$e = NAB \omega \sin \omega t$$
 ...(i)

The induced emf will be maximum

When  $\sin \omega t = \text{maximum} = 1$ 

$$e_{\text{max}} = e_0 = NAB \omega \times 1$$

or  $e = e_0 \sin \omega t$ 

٠.

Therefore, e would be maximum, hence current is maximum (as  $i_0 = e_0/R$ ), when  $\theta = 90^\circ$ , *i.e.*, normal to plane of coil is perpendicular to the field or plane of coil is parallel to magnetic field.

**20.** 
$$E = at + \frac{1}{2}bt^2$$
 ...(i)

Differentiating Eq. (i), w.r.t., t we have

$$\frac{dE}{dt} = a + bt$$

When  $t = t_n$ , i.e., neutral temperature, then

$$\frac{dE}{dt} = 0$$

$$0 = a + bt_n$$
or
$$t_n = -\frac{a}{b}$$

The temperature of inversion

$$t_i = 2t_n - t_0$$
$$= 2t_n - 0$$
$$= -\frac{2a}{b}$$

Thermoelectric power

$$P = \frac{dE}{dt} = a + bt$$

**21.** Cyclotron frequency is given by

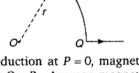
$$v = \frac{qB}{2\pi m}$$

$$v = \frac{1.6 \times 10^{-19} \times 6.28 \times 10^{-4}}{2 \times 3.14 \times 1.7 \times 10^{-27}}$$

$$= 0.94 \times 10^{4}$$

$$\approx 10^{4} \text{ Hz}$$

22.



Magnetic field induction at P = 0, magnetic field induction at  $O = B_0$ . Average magnetic field induction from P to  $O = \frac{0 + B_0}{2} = \frac{B_0}{2}$ 

Force experienced by a charge while moving along the axis of wire, i.e., from P to O will be

$$= \frac{B_0}{2} \times q \times v$$
$$= \frac{1}{2} B_0 q v$$

**23.** When two solenoids of inductance  $L_0$  are connected in series at large distance and current i is passed through them, the total flux linkage  $\phi_{\text{total}}$  is the sum of the flux linkages  $L_0i$  and  $L_0i$ . i.e.,

$$\phi_{\text{total}} = L_0 i + L_0 i$$

If L be the equivalent inductance of the system, then

$$\phi_{\text{total}} = Li$$

$$Li = L_0 i + L_0 i$$

or 
$$L = 2L_0$$

When solenoids are connected in series with one inside the other and senses of the turns coinciding, then there will be a mutual inductance L between them. In this case the resultant induced emf in the coils is the sum of the emf's  $e_1$  and  $e_2$  in the respective coils, i.e.,

$$e = e_1 + e_2$$

$$= \left( -L_0 \frac{di}{dt} \pm L_0 \frac{di}{dt} \right)$$

$$+ \left( -L_0 \frac{di}{dt} \pm L_0 \frac{di}{dt} \right)$$

where (+) sign is for positive coupling and (-) sign for negative coupling.

But, 
$$e = -L \cdot \frac{di}{dt}$$
  

$$\therefore -L \frac{di}{dt} = -L_0 \frac{di}{dt} - L_0 \frac{di}{dt} \pm 2L_0 \frac{di}{dt}$$
i.e.,  $L = L_0 + L_0 + 2L_0$   
 $= 4L_0$  (for positive coupling)

When solenoids are connected in series with one inside the other with senses of the turns opposite, then their is negative coupling.

So, 
$$L = L_0 + L_0 - 2L_0$$
  
= 0

**24.** The impedance (*Z*) of an *R-L-C* series circuit is given by

$$Z = \sqrt{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2}$$

As frequency of alternating emf applied to the circuit is increased,  $X_L$  goes on increasing and  $X_C$  goes on decreasing. For a particular value of  $\omega$  (=  $\omega_r$  say)

$$i.e.,$$
  $\omega_r L = \frac{1}{\omega_r C}$  or  $\omega_r = \frac{1}{\sqrt{LC}}$  or  $2\pi v_r = \frac{1}{\sqrt{LC}}$  or  $v_r = \frac{1}{2\pi\sqrt{LC}}$ 

$$v = \frac{1}{2 \times 3.14 \times \sqrt{5 \times 80 \times 10^{-6}}}$$

$$= \frac{1}{2 \times 3.14 \sqrt{(400 \times 10^{-6})}}$$

$$= \frac{1}{2 \times 3.14 \times 2 \times 10^{-2}}$$

$$= \frac{100}{3.14 \times 4}$$

$$= \frac{25}{3.14} = \frac{25}{3.14} = \frac{25}{3.14} = \frac{1}{3.14} = \frac{1}{3$$

**25.** The induced emf e in the secondary is given by

$$e = -\frac{d\phi}{dt} = -M \frac{dI}{dt}$$
or
$$|e| = M \frac{dI}{dt}$$

$$|e| = 5 \times \frac{10}{5 \times 10^{-4}}$$

$$= 1 \times 10^{5} \text{ V}$$

**26.** A series resonance circuit admits maximum current, as

$$P = i^2 R$$

So, power dissipated is maximum at resonance.

So, frequency of the source at which maximum power is dissipated in the circuit is

$$v = \frac{1}{2\pi\sqrt{LC}}$$

$$= \frac{1}{2\times 3.14\sqrt{25\times 10^{-3}\times 400\times 10^{-6}}}$$

$$= \frac{1}{2\times 3.14\sqrt{10^{-5}}}$$
= 50.3 Hz

27. To see interference, we need two sources with the same frequency and with a constant phase difference. In the given waves,

$$X_1 = a_1 \sin \omega t$$
  
and  $X_4 = a_1 \sin (\omega t + \delta)$   
have a constant phase difference  $\delta$ , interference is possible between them.

so

For  $X_1 = a_1 \sin \omega t$ ,

and 
$$X_2 = a_2 \sin 2\omega t$$
,

frequency is not equal and there is no constant phase difference.

$$X_1 = a_1 \sin \omega t$$
,

$$X_3 = a_1 \sin \omega_1 t,$$

frequency is different and there is no constant phase difference.

#### The equation of nth principal maxima for wavelength λ is given by

$$(a + b) \sin \theta = n\lambda$$

where a is the width of transparent portion and b is that of opaque portion. The width (a + b) is called the grating element.

The spectral lines will overlap, *i.e.*, they will have the same angle of diffraction if

$$\lambda_1 = \lambda_2$$

When a line of wavelength  $\lambda_1$  in order  $n_1$  coincides with a line of unknown wavelength  $\lambda_2$  in order  $n_2$ , then

or 
$$n_2 \lambda_2 = n_1 \lambda_1$$
$$\frac{\lambda_1}{\lambda_2} = \frac{n_2}{n_1}$$

**29.** Given, 
$$\frac{I_{\text{max}}}{I_{\text{min}}} = 9 = \frac{(a_1 + a_2)^2}{(a_1 - a_2)^2}$$

$$\therefore \frac{a_1 + a_2}{a_1 - a_2} = 3$$

or 
$$2a_1 = 4a_2$$
or 
$$a_1 = 2a_2$$

$$\Rightarrow \frac{a_1}{a_2} = 2$$

Again, intensity ratio at the screen due to two slits

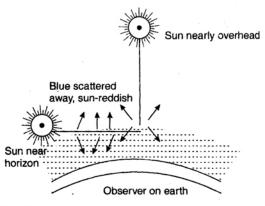
$$\frac{I_1}{I_2} = \frac{a_1^2}{a_2^2} = \frac{4}{1}$$

Hence, amplitude ratio is 2 and intensities at the screen due to two slits are 4 units and 1 units, respectively.

**30.** At the time of sunrise and sunset, the sun is near the horizon. The rays from the sun have to travel a larger part of the atmosphere, As  $\lambda_b < \lambda_r$ , and intensity of scattered light  $\propto \frac{1}{\lambda^4}$ ,

therefore, most of the blue light is scattered away, only red colour, which is least

scattered enters our eyes and appears to come from the sun. Hence, the sun looks red both at the time of sunrise and sunset.



**31.** The magnetic moment of the ground state of an atom is

$$\mu = \sqrt{n(n+2)} \, \mu_B$$

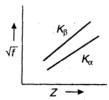
where  $\mu_B$  is gyromagnetic moment. Here, open sub-shell is half-filled with 5 electrons. i.e., n = 5

$$\mu = \sqrt{5(5+2)} \cdot \mu_B$$
$$= \mu_B \sqrt{35}$$

**33.** Moseley studied the *X*-ray spectra of various elements. The spectral line observed were of (i) short wavelength – K series and (ii) long wavelength – L series.  $K_{\alpha}$  line is most intense in the K-series. Moreover, he observed that the wavelength of the  $K_{\alpha}$  line decreases with increase in the atomic number of the element as the target. If a graph is plotted between the square root of the frequency and the atomic number of the element emitting the line, it is a straight line

$$\sqrt{f} \propto Z$$

Where  $\sqrt{f}$  is the frequency of the radiation and Z is the atomic number of the element.



**34.** Balmer series is the series in which the spectral lines correspond to the transition of

electron from some higher energy state to the lower energy state corresponding to  $n_f = 2$ .

Therefore, for Balmer series,  $n_f = 2$  and  $n_i = 3, 4, 5, \dots$ 

Frequency, of 1st spectral line of Balmer series

$$f = RZ^{2}c\left(\frac{1}{2^{2}} - \frac{1}{3^{2}}\right)$$

$$f = RZ^{2}c \times \frac{5}{36} \qquad ...(i)$$

Frequency of 2nd spectral line of Balmer

$$f' = RZ^2c\left(\frac{1}{2^2} - \frac{1}{4^2}\right)$$
$$f' = RZ^2c \times \frac{3}{16}$$

From Eqs. (i) and (ii), we have

or

$$\frac{f}{f'} = \frac{20}{27}$$

$$f' = \frac{27}{20} f = 1.35 f$$
**35.** The relativistic kinetic energy of a particle of

rest mass 
$$m_0$$
 is given by
$$K = (m - m_0) c^2$$

$$m = \frac{m_0}{\sqrt{1 - (v^2/c^2)}}$$
, where m is the mass of the

particle moving with velocity v.

$$K = \left[ \frac{m_0}{\sqrt{1 - (v^2/c^2)}} - m_0 \right] c^2 z$$

According to problem,

kinetic energy = rest energy
$$\begin{bmatrix} & & & & \\ & & & & \\ & & & & \end{bmatrix}$$

 $v = \frac{\sqrt{3c}}{2}$ 

$$\left[ \frac{m_0}{\sqrt{1 - (v^2/c^2)}} - m_0 \right] c^2 = m_0 c^2$$

or 
$$\frac{m_0 c^2}{\sqrt{1 - (v^2/c^2)}} = 2m_0 c^2$$

or 
$$\frac{1}{1 - (v^2/c^2)} = 4$$
  
or  $4v^2/c^2 = 3$ 

...(i)

...(ii)

37.

**36.** If a charge particle of mass m and charge q is accelerated through a potential difference V. and E is the energy acquired by the particle.

then 
$$E = aV$$

If  $\nu$  is velocity of particle, then

or 
$$E = \frac{1}{2} m v^2$$
$$v = \sqrt{\frac{2E}{m}}$$

Now, de-Broglie wavelength of particle is

$$\lambda = \frac{h}{mv} = \frac{h}{m\sqrt{(2E/m)}}$$

Substituting the value of E, we get

$$\lambda = \frac{h}{\sqrt{2mqV}}$$

For electron,  $\lambda_e = \frac{h}{\sqrt{2m_e eV}}$ 

For proton,  $\lambda_p = \frac{h}{\sqrt{2m_n eV}}$ 

$$\frac{\lambda_e}{\lambda_p} = \sqrt{\frac{m_p}{m_e}}$$
The particles are moving with velocities 0.8 c

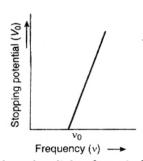
and -0.4 c in the laboratory frame, say S' frame. Let S be a reference frame in which the particle with velocity -0.4 c is at nest. Then, the velocity of S' (laboratory) relative to S is v = 0.4 c. Therefore, the particle which in S' has velocity u' = +0.8 c has a velocity in S given by

$$u = \frac{u' + v}{1 + \frac{u' v}{c^2}}$$

$$= \frac{0.8 c + 0.4 c}{1 + \frac{(0.8 c)(0.4 c)}{c^2}}$$

$$= \frac{1.2 c}{1 + 0.32} = 0.9 c$$
sion of photoelectron

38. The emission of photoelectron takes place only, when the frequency of the incident light is above a certain critical value, characteristic of that metal. The critical value of frequency is known as the threshold frequency for the metal of the emitting electrode.



Suppose that when light of certain frequency is incident over a metal surface, the photoelectrons are emitted. To take photoelectric current zero, a particular value of stopping potential will be needed. If we go on reducing the frequency of incident light, the value of stopping potential will also go on decreasing. At certain value of frequency  $v_0$ , the photoelectric current will become zero, even when no retarding potential is applied. This frequency  $v_0$  corresponds to the threshold for the metal surface. The emission of photoelectrons does not take place, till frequency of incident light is below this value.

**39.** Experimental measurements show that volume of a nucleus is proportional to its mass number A. If R is the radius of the nucleus assumed to be spherical, then its volume  $\left(\frac{4}{3}\pi R^3\right) \propto A$ 

or 
$$R \propto A^{1/3}$$
  
or  $R = R_0 A^{1/3}$ 

where  $R_0$  is an empirical constant whose value is found to be  $1.1 \times 10^{-15}$  m.

**40.** Radiocarbon dating relies on a simple natural phenomenon. As the earth's upper is bombarded by cosmic radiation, atmospheric nitrogen is broken down into an unstable isotope of carbon-carbon 14 (C-14).

The unstable isotope is brought to earth by atmospheric activity, such as storms, and becomes fixed in the biosphere. Because it reacts identically to C-12 and C-13, C-14 attached to complex organic molecules through photosynthesis in plants and becomes their molecular makeup. Animals eating those plants in turn absorb carbon-14 as welll as stable isotopes. This process of ingesting C-14 continues as long as the plant or animal remains alive.

The C-14 within an organism is continually decaying into stable carbon isotopes, but organism is absorbing more C-14 during its life, the ratio of C-14 to C-12 remains about same as the ratio in the atmosphere. When the organism dies, the ratio of C-14 within its carcass begins to gradually decrease.

# Chemistry

- **41.** Frenkel defects arises when an ion is missing from its normal position and occupies an interstitial site between the lattice points.
- **42.** The 8:8 type of packing is present in cesium chloride (CsCl). In this structure each Cs<sup>+</sup> ion is surrounded by 8Cl<sup>-</sup> ions and each Cl<sup>-</sup> ion is also surrounded by 8Cs<sup>+</sup> ions.
- **43.** When a solid melts, its entropy (S) increases because on changes from solid to liquid disorder or randomness of molecules increases.
- 44. The Gibbs-Helmholtz equation is as:

$$G = H + T \left( \frac{\partial G}{\partial T} \right)_{p}$$

Dividing above equation by  $T^2$ 

$$\frac{G}{T^2} = \frac{H}{T^2} + \frac{1}{T} \left( \frac{\partial G}{\partial T} \right)_P$$

This on rearrangement becomes

$$\left[\frac{\partial (G/T)}{\partial T}\right]_{p} = -\frac{H}{T^{2}}$$

$$H = -T^{2} \left[\frac{\partial (G/T)}{\partial T}\right]_{p}$$

where H = enthalpy

**45.** The condition for spontaneity in an isothermal process is that  $\Delta G$  should be negative.

$$\Delta G = \Delta A + P \cdot \Delta V$$

$$\Delta G = \Delta A + W \qquad (: W = P \cdot \Delta V)$$

.. For spontaneity in an isothermal process:

$$\Delta A + W < 0$$

**46.** 
$$2C(s) + 2O_2(g) \longrightarrow 2CO_2(g);$$
  
 $\Delta H = -787 \text{ kJ} ...(i)$ 

$$H_2(g) + \frac{1}{2}O_2(g) \longrightarrow H_2O(l);$$

$$\Delta H = -286 \,\text{kJ} \, ...(ii)$$

$$C_2H_2(g) + 2\frac{1}{2}O_2(g) \longrightarrow 2CO_2(g) + H_2O(l);$$

$$\Delta H = -1310 \text{ kJ} \dots (iii)$$

Add the Eqs. (i) and (ii) and subtract Eq. (iii) from them.,

$$2C + H_2 \longrightarrow C_2H_2 - 787 - 286 + 1310$$
  
 $2C + H_2 \longrightarrow C_2H_2 - 1073 + 1310$   
 $2C + H_2 \longrightarrow C_2H_2 + 237$ 

Hence, the heat of formation of acetylene is + 237 kJ.

47. 
$$NH_4Cl(s) \longrightarrow NH_4^+(aq) + Cl^-(aq)$$

$$\Delta H = + 3.5 \text{ kcal/mol}$$

This is the endothermic reaction hence, increasing the temperature will shift the equilibrium to the right.

48. Arrhenius equation is written as:

$$K = Ae^{-E_{\alpha}/RT}$$

Taking logarithm, above equation may be written as:

$$\ln K = \ln A - \frac{E_a}{R} \times \frac{1}{T}$$

$$\ln K_1 = \ln A - \frac{E_a}{R} \times \frac{1}{T} \qquad \dots (i)$$

$$\ln K_2 = \ln A - \frac{E_a}{R} \times \frac{1}{T_2} \qquad \dots (ii)$$

Subtracting the Eq. (i) from Eq. (ii)

$$\ln K_2 - \ln K_1 = \frac{E_a}{R} \left[ \frac{1}{T_1} - \frac{1}{T_2} \right]$$

$$\ln \frac{K_2}{K_1} = \frac{E_a}{R} \left[ \frac{1}{T_1} - \frac{1}{T_2} \right]$$

49. 
$$H_2 + I_2 \rightleftharpoons 2HI$$

$$\begin{array}{cccc} 1 & 1 & 0 \\ (1-0.8) & (1-0.8) & 2 \times 0.8 \\ = 0.2 & = 0.2 & = 1.6 \end{array}$$

$$K_{c} = \frac{[\text{HI}]^{2}}{[\text{H}_{2}][\text{I}_{2}]}$$
$$= \frac{1.6 \times 1.6}{0.2 \times 0.2}$$

$$K_c = 64$$

**50.** 
$$H_2(g) + I_2(g) \longrightarrow 2HI(g)$$

The equilibrium constant  $(K_p)$  changes with the change in temperature.

**Note:** Variation of equilibrium constant with temperature can be express as:

$$\log \frac{K_2}{K_1} = \frac{\Delta H}{2.303 R} \left[ \frac{T_2 - T_1}{T_1 \cdot T_2} \right]$$

**51.** 
$$W = 60 \text{ g}$$
  $i = 5 \text{ A}$ 

Equivalent weight of Ca =  $\frac{\text{atomic weight}}{\text{valency}}$ =  $\frac{40}{2}$  = 20

According to first law of Faraday electrolysis:

$$W = Zit = \frac{\text{equivalent weight}}{96500} \times i \times t$$

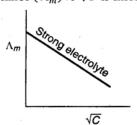
$$60 = \frac{20}{96500} \times 5 \times t$$

$$t = \frac{96500 \times 60}{20 \times 5} \text{ s}$$

$$= \frac{96500 \times 60}{20 \times 5 \times 60 \times 60} \text{ h}$$

$$= 16.08 \text{ h}.$$

**52.** For strong electrolytes the plot of molar conductance  $(\Lambda_m) vs \sqrt{C}$  is linear.



Variation of molar conductance  $(\Lambda_m)$  with  $\sqrt{C}$  for strong electrolyte.

53. From Kohlrausch's law:

$$\Lambda_m^{\infty} = \nu_+ \lambda_+^{\infty} + \nu_- \lambda_-^{\infty}$$

$$\Lambda_{m}^{\infty} (CaCl_{2}) = \lambda_{Ca^{2+}}^{\infty} + 2\lambda_{Cl}^{\infty}$$

$$= 118.88 \times 10^{-4} + 2 \times 77.33 \times 10^{-4}$$

$$= 118.88 \times 10^{-4} + 154.66 \times 10^{-4}$$

$$= 273.54 \times 10^{-4} \text{ m/s mho mol}^{-1}$$

- 54. The substances which have lower reduction potentials are stronger reducing agent. The reduction potential of zinc is lowest among these hence, it is the strongest reducing agent.
- **55.** The structural formula of epoxide is  $\begin{pmatrix} CH_2 \\ CH_2 \end{pmatrix}$  O

It consists three membered ring with two carbon and one oxygen.

In the Grignard reaction magnesium metal forms an organometallic bond.

$$RX + Mg \xrightarrow{Dry \text{ ether}} R - Mg - X$$
Grignard reagent

**57.** Phenol is more acidic than ethanol due to resonance stabilisation of phenoxide ion.

 Aldol condensation is given by acetaldehyde due to the presence of α-hydrogen atom.

$$\begin{array}{cccc} \text{CH}_3\text{CHO} + \text{H} \cdot \text{CH}_2\text{CHO} & \xrightarrow{\text{Dil. NaOH}} \\ & \text{CH}_3\text{--CH}\text{--CH}_2\text{--CHO} \\ & | & \text{OH} \\ & \text{aldol} \\ \text{O} & | & | & | \end{array}$$

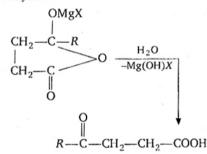
- **59.**  $H_3C CH_2 CH_2 CH_2 CH_2 CH_3$ methyl 4-oxohexanoate
- The addition of α, β-unsaturated carbonyl compound, with conjugated diene is called Diel's-Alder reaction.

**61.** In the Rosenmund's reaction the acid chlorides are converted to corresponding aldehydes by catalytic reaction. This reaction is carried in the presence of palladium deposited over barium sulphate.

$$\begin{array}{c} O \\ \parallel \\ CH_3-C-Cl+H_2 \end{array} \xrightarrow{Pd, \ BaSO_4} \begin{array}{c} CH_3CHO \\ acetyl \ chloride \end{array} \xrightarrow{Pd, \ BaSO_4} \begin{array}{c} CH_3CHO \\ + HCl \end{array}$$

62. 
$$\begin{matrix} CH_2 - C \\ | \\ CH_2 - C \\ | \\ C \end{matrix} > O + RMgX \longrightarrow 0$$

succinic anhydride



- **63.** (+) and (-) Tartaric acid does not possess any element of symmetry.
- 64. The strength of carboxylic acid depends upon the nature of the electron withdrawing halogen atom. Greater the electron withdrawing influence of the halogen atom stronger will be the acid. The electron withdrawing effect of the halogen decreases as:

Hence, CH<sub>2</sub>(I) COOH is the weakest acid among these.

65. Urea on slow heating gives biuret.

$$H_2N \cdot CONH \cdot H + H_2N \cdot CONH_2 \xrightarrow{\Delta}$$

$$H_2NCONH \cdot CONH_2 + NH_3$$
biuret ammonia

**66.** Transesterification is the process of conversion of one ester to another ester.

$$R \stackrel{O}{\underset{ester}{\parallel}} R - C \stackrel{O}{\underset{ester}{-}} OR' + R'' - OH \stackrel{H^+, R''ONa}{\underset{Reflux}{-}} O$$

$$R - C - OR'' + R' OH$$

$$CH_3COOC_4H_9 + C_2H_5OH \xrightarrow{H^+, C_2H_5ONa}$$
*Reflux*

67. The order of base strength of amines in aqueous solution is as:

$$(CH_3)_2NH > CH_3NH_2 > (CH_3)_3N$$

Tertiary amine is less basic than primary and secondary amine due to steric effect of three methyl group present on nitrogen atom.

68. When aqueous solution of benzene diazonium chloride is boiled, it gives phenol.

69. Carbylamine reaction is given by aliphatic and aromatic primary amine hence, it can be used for the distinguish of primary amine with secondary and tertiary amine. In this reaction a primary amine reacts with chloroform and alcoholic KOH to give poisonous substance isocyanide.

$$RNH_2$$
 + CHCl<sub>3</sub> + 3KOH(alc)  $\xrightarrow{\Delta}$  primary amine

Benzaldehyde reacts with ammonia to form hydrobenzamide.

$$C_6H_5CH = O + H_2 N H + O = CH - C_6H_5 \longrightarrow$$

$$C_6H_5CH = N + O + C_6H_5 + 3H_2O$$

$$C_6H_5CH = N$$

Hydrobenzamide

71. Key Idea:

No. of hybrid orbital =  $\frac{1}{2}$  [No. of  $e^-$  in V-shell of atom + No. of monovalent atoms – charge

No. of 2 3 4 5 6 7 hybrid orbital Type of sp  $sp^2$   $sp^3$   $sp^3d$   $sp^3d^2$   $sp^3d^3$ hybridi-

Hybridisation in TeCl<sub>4</sub>:

sation

on cation + charge on anion]

No. of hybrid orbital = 
$$\frac{1}{2}[6 + 4 + 0 + 0] = 5$$

Hence, TeCl<sub>4</sub> shows sp<sup>3</sup>d hybridisation.

- 72. HgCl<sub>2</sub> compound is easily volatile. They are insoluble in water and soluble in acids.
- **73.**  $^{235}_{92}U + ^{1}_{0}n \longrightarrow ^{90}_{36}Kr + ^{144}_{56}Ba + 2 ^{1}_{0}n$

**Note:** In the nuclear reaction atomic number and mass are conserved.

74. AgCl dissolves in the solution of NH<sub>3</sub> but not in water because Ag<sup>+</sup> forms a complex ion with NH<sub>3</sub>.

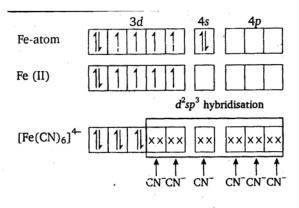
$$AgCl + 2NH_3 \longrightarrow [Ag(NH_3)_2]Cl$$
 diamine silver (l) chloride

75. Ethylenediamine tetra-acetic acid is a hexadentate ligand because it has six donor centers.

76. A coordinate bond is a dative covalent bond in which two atoms form bond and one of them provides both electrons.

$$X: + Y \longrightarrow X: Y$$
 or  $X \longrightarrow Y$ 

77. Ferrocyanide ion [Fe(CN)<sub>6</sub>]<sup>4-</sup> is diamagnetic in nature hence K<sub>4</sub>[Fe(CN)<sub>6</sub>] complex has zero magnetic moment.



- 78. The IUPAC name of [Ni(PPh<sub>3</sub>)<sub>2</sub>Cl<sub>2</sub>]<sup>2+</sup> is dichloro bis (triphenylphosphine) nickel (II)
- 79. VOSO<sub>4</sub> is paramagnetic as well as coloured compound.

The oxidation state of vanadium in VOSO<sub>4</sub> is +4.

$$V[Z = 23] = [Ar] 3d^3 4s^2$$
  
 $V^{4+}[Z = 23] = [Ar] 3d^1 4s^0$ 

It has one unpaired electron hence, it is paramagnetic in nature.

80. On an X-ray diffraction photograph the intensity of the spots depends on the electron density of the atoms/ions.

### Mathematics

**81.** : 
$$\alpha = \frac{3\pi}{4}$$

and we know that  $f'(3) = \tan \alpha$ =  $\tan \frac{3\pi}{4}$ 

**82.** : 
$$f(x) = x^2 e^{-2x}$$

$$f'(x) = 2x e^{-2x} - 2x^2 e^{-2x}$$
$$= 2x(1-x)e^{-2x}$$

Put f'(x) = 0 for maxima or minima, we get  $2x(1-x)e^{-2x} = 0$ 

$$x = 0, 1$$

Now, 
$$f''(x) = 2x(-1)e^{-2x} + 2(1-x)e^{-2x} - 2 \cdot 2x(1-x)e^{-2x}$$

$$-2 \cdot 2x(1-x)e^{-x}$$

$$f''(0) = 0 + 2e^{-x} = 2$$

and 
$$f''(1) = -2e^{-2} + 0 - 0 = -\frac{2}{e^2} < 0$$

f(x) is maximum at x = 1.

Thus, maximum value of  $f(x) = 1 \cdot e^{-2} = \frac{1}{e^2}$ 

**83.** 
$$(x+y)\sin u = x^2y^2$$
 ...(i

On differentiating partially w.r.t. x of Eq. (i), we get

$$(1+0)\sin u + (x+y)\cos u \frac{\partial u}{\partial x} = 2xy^2$$

$$\Rightarrow x\sin u + (x^2 + xy)\cos u \frac{\partial u}{\partial x} = 2x^2y^2$$

...(ii)
On differentiating partially w.r.t. y of Eq. (i),
we get

$$(0+1)\sin u + (x+y)\cos u \frac{\partial u}{\partial y} = 2x^2y$$

$$\Rightarrow y \sin u + (xy + y^2) \cos u \frac{\partial u}{\partial y} = 2x^2y^2$$

...(iii)

On adding Eqs. (ii) and (iii), we get
$$(x+y)\sin u + (x+y)\left\{x\frac{\partial u}{\partial x} + y\frac{\partial u}{\partial y}\right\}\cos u$$

$$= 4x^2y^2$$

$$\Rightarrow x^2y^2 + (x+y)\left\{x\frac{\partial u}{\partial x} + y\frac{\partial u}{\partial y}\right\}\cos u$$
$$= 4x^2y^2$$

$$\Rightarrow (x+y)\left(x\frac{\partial u}{\partial x}+y\frac{\partial u}{\partial y}\right)\cos u=3x^2y^2$$

$$\Rightarrow (x+y)\left(x\frac{\partial u}{\partial x}+y\frac{\partial u}{\partial y}\right)\cos u$$

 $=3(x+y)\sin u$ 

$$\Rightarrow x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = 3 \tan u$$

**84.** Given that, 
$$x = t^2 + 1$$
 and  $y = t^2 - t - 6$ 

$$\frac{dx}{dt} = 2t \quad \text{and} \quad \frac{dy}{dt} = 2t - 1$$

Now, 
$$\frac{dy}{dx} = \frac{dy/dt}{dx/dt} = \frac{2t-1}{2t}$$
  
when, it meet x-axis, then

when, it meet x-axis, then 
$$t^2 - t - 6 = 0$$

$$\Rightarrow (t+2)(t-3)=0$$

$$\Rightarrow \qquad t = 3, -2$$

$$\therefore \left(\frac{dy}{dx}\right)_{\text{at } t = 3} = \frac{6-1}{6} = \frac{5}{6} = m_1 \text{ (say)}$$

and 
$$\left(\frac{dy}{dx}\right)_{\text{at }t=-2} = \frac{5}{4} = m_2 \text{ (say)}$$

Required angle = 
$$\pm \tan^{-1} \left\{ \begin{vmatrix} \frac{5}{6} - \frac{5}{4} \\ 1 + \frac{25}{24} \end{vmatrix} \right\}$$

$$= \pm \tan^{-1} \left\{ \frac{10}{49} \right\}$$

**85.** 
$$\int_{1}^{4} |x-3| dx$$

$$= \int_{1}^{3} (3-x) dx + \int_{3}^{4} (x-3) dx$$

$$\int x^{2} \int_{1}^{3} \left[ x^{2} \right]^{4}$$

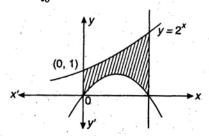
$$= \left[3x - \frac{x^2}{2}\right]_1^3 + \left[\frac{x^2}{2} - 3x\right]_3^4$$

$$= \left(9 - \frac{9}{2}\right) - \left(3 - \frac{1}{2}\right) + \left(\frac{16}{2} - 12\right) - \left(\frac{9}{2} - 9\right)$$

$$= \frac{9}{2} - \frac{5}{2} - 4 + \frac{9}{2} = 9 - 4 - \frac{5}{2}$$
$$= 5 - \frac{5}{2} = \frac{5}{2}.$$

$$= \int_0^2 [2^x - (2x - x^2)] dx$$

86. Required area



$$= \int_0^2 (2^x - 2x + x^2) \, dx$$

$$= \left[ \frac{2^x}{\log 2} - x^2 + \frac{x^3}{3} \right]_0^2$$

$$= \frac{4}{\log 2} - 4 + \frac{8}{3} - \frac{1}{\log 2}$$

$$= \left(\frac{3}{\log 2} - \frac{4}{3}\right)$$
 sq unit

**87.** 
$$\int_0^\infty \frac{dx}{(a^2 + x^2)} = \left[ \frac{1}{a} \tan^{-1} \frac{x}{a} \right]_0^\infty$$
$$= \frac{1}{a} \left\{ \tan^{-1} (\infty) - \tan^{-1} (0) \right\}$$

$$=\frac{1}{a}\left(\frac{\pi}{2}-0\right)=\frac{\pi}{2a}$$

**88.** 
$$\int e^{x} \left( \frac{1-x}{1+x^{2}} \right)^{2} dx$$
$$= \int e^{x} \frac{(1+x^{2}-2x)}{(1+x^{2})^{2}} dx$$

$$= \int e^x \left( \frac{1}{1+x^2} - \frac{2x}{(1+x^2)^2} \right) dx$$

$$= e^{x} \cdot \frac{1}{1+x^{2}} + \int \frac{2x e^{x}}{(1+x^{2})^{2}} dx$$

$$-\int \frac{2x e^x}{(1+x^2)^2} dx$$

$$= \frac{e^x}{1+x^2} + c$$

**89.** 
$$x \sin\left(\frac{y}{x}\right) dy = \left[y \sin\left(\frac{y}{x}\right) - x\right] dx$$

$$\Rightarrow \frac{dy}{dx} = \frac{y \sin\left(\frac{y}{x}\right) - x}{x \sin\left(\frac{y}{x}\right)} = \frac{\frac{y}{x} \sin\left(\frac{y}{x}\right) - 1}{\sin\left(\frac{y}{x}\right)}$$

Let 
$$\frac{y}{x} = u$$
 and  $\frac{dy}{dx} = x \frac{du}{dx} + u$   

$$\therefore \qquad x \frac{du}{dx} + u = \frac{u \sin u - 1}{\sin u}$$

$$\Rightarrow x \frac{du}{dx} = \frac{u \sin u - 1 - u \sin u}{\sin u}$$

$$\Rightarrow$$
  $-\sin u \, du = \frac{1}{x} \, dx$ 

On integrating both sides, we get

$$\cos u = \log x + c$$

$$\cos\left(\frac{y}{x}\right) = \log x + c$$

$$y(1) = \frac{\pi}{2}$$

$$\therefore \qquad \cos\frac{\pi}{2} = \log 1 + c \implies c = 0$$

Thus, 
$$\cos\left(\frac{y}{x}\right) = \log x$$

**90.** The equation of the family of circles of radius *r* is

$$(x-a)^2 + (y-b)^2 = r^2$$
 ...(i)

where a and b are arbitrary constants. On differentiating Eq. (i) w.r.t. x, we get

$$2(x-a) + 2(y-b)\frac{dy}{dx} = 0$$

$$\Rightarrow (x-a)+(y-b)\frac{dy}{dx}=0 \qquad ...(ii)$$

On differentiating Eq. (ii) w.r.t. x, we get

$$1 + (y - b) \frac{d^2y}{dx^2} + \left(\frac{dy}{dx}\right)^2 = 0$$

$$(y-b) = -\frac{1 + (dy/dx)^2}{d^2y/dx^2}$$
 ...(iii)

On putting the value of (y - b) in Eq. (ii), we get

$$(x-a) = \frac{\left[1 + \left(\frac{dy}{dx}\right)^2\right] \frac{dy}{dx}}{\frac{d^2y}{dx^2}} \qquad \dots \text{(iv)}$$

On putting the value of (y - b) and (x - a), in Eq. (i), we get

$$\frac{\left[1 + \left(\frac{dy}{dx}\right)^{2}\right]^{2} \left(\frac{dy}{dx}\right)^{2}}{(d^{2}y/dx^{2})^{2}} + \frac{\left[1 + \left(\frac{dy}{dx}\right)^{2}\right]^{2}}{(d^{2}y/dx^{2})^{2}} = r^{2}$$

$$\Rightarrow \qquad \left[1 + \left(\frac{dy}{dx}\right)^2\right]^3 = r^2 \left[\frac{d^2y}{dx^2}\right]^2$$

This is the required differential equation.

91. The given equation can be written as

$$(D^2 + 2D + 1)y = 2e^{3x}$$
, where  $\frac{d}{dx} = D$ 

Here,  $F(D) = D^2 + 2D + 1$  and  $Q = 2e^{3x}$ 

The auxiliary equation is

$$m^2 + 2m + 1 = 0 \implies (m+1)^2 = 0$$

$$\Rightarrow m=-1,-1$$

:. The CF = 
$$(c_1 + c_2 x)e^{-x}$$

and 
$$PI = \frac{1}{F(D)} 2e^{3x} = 2 \cdot \frac{1}{D^2 + 2D + 1} \cdot e^{3x}$$
  
=  $2 \cdot \frac{e^{3x}}{9 + 6 + 1} = \frac{e^{3x}}{8}$ 

Hence, the complete solution is

$$y = CF + PI$$

$$\Rightarrow$$
  $y = (c_1 + c_2 x)e^{-x} + \frac{e^{3x}}{8}.$ 

**92.** 
$$y dx + (x - y^3) dy = 0$$

Here, M = y and  $N = x - y^3$ . We have.

$$\frac{\partial M}{\partial y} = 1$$
 and  $\frac{\partial N}{\partial x} = 1$ , i.e.,  $\frac{\partial M}{\partial y} = \frac{\partial N}{\partial x}$ 

Hence, the given equation is exact.

Integrating M, i.e., y w.r.t. x, treating y as a constant, we get xy.

Again, the only terms in N which do not contain x are  $-y^3$ .

Integrating  $(-y^3)$  w.r.t. y we obtain  $-\frac{y^4}{4}$ .

Hence, the solution of the given differential equation is

$$xy - \frac{y^4}{4} + c = 0$$

$$y^4 = 4xy + c$$

93. Required number of integral solution of

$$x_1 + x_2 + x_3 = 0 = {}^{15+3-1}C_{3-1}$$

**94.** : 
$$A = \{1, 2, 3, ..., n\}$$
 and  $B = \{a, b, c\}$   
:  $n(A) = n$  and  $n(B) = 3$ 

Number of onto function from A to B

$$= \sum_{r=1}^{3} (-1)^{3-r} {}^{3}C_{r} r^{n}$$

$$= (-1)^{2} {}^{3}C_{1}(1)^{n} + (-1)^{1} {}^{3}C_{2}(2)^{n} + (-1)^{0} {}^{3}C_{3}3^{n}$$

$$= 3^{n} - 3 \cdot 2^{n} + 3$$

$$= 3^{n} - 3(2^{n} - 1)$$

**95.** Let the total number of persons in the room = n.

 $\therefore$  Total number of handshakes =  ${}^{n}C_{2}$ .

But number of handshakes = 66.

$$\frac{n!}{2!(n-2)!} = 66$$

$$\Rightarrow \frac{n(n-1)}{2} = 66$$

$$\Rightarrow \qquad n^2 - n - 132 = 0$$

$$\Rightarrow \qquad n^2 - 12n + 11n - 132 = 0$$

$$\Rightarrow n(n-12)+11(n-12)=0$$

$$\Rightarrow (n-12)(n+11) = 0$$

$$\Rightarrow n = 12 \quad (\because n \neq -11)$$

**96.** The identify element for multiplication modulo 10, is 1 and 
$$3X_{10}$$
 7 = 1.

So, the inverse of 7 is 3.

 In out of 9 tickets, 5 tickets are odd numbers and 4 tickets are even number.

Required probability = 
$$\begin{cases} \frac{5C_1}{9C_1} \times \frac{4C_1}{8C_1} \times \frac{4C_1}{7C_1} \end{cases}$$

$$+\frac{{}^{4}C_{1}}{{}^{9}C_{1}} \times \frac{{}^{5}C_{1}}{{}^{8}C_{1}} \times \frac{{}^{3}C_{1}}{{}^{7}C_{1}}$$

$$=\frac{5}{9} \times \frac{4}{8} \times \frac{4}{7} + \frac{4}{9} \times \frac{5}{8} \times \frac{3}{7}$$

$$=\frac{80 + 60}{504} = \frac{140}{504}$$

$$=\frac{5}{12}$$

**98.** : 
$$P(A) = \frac{1}{12}$$
,  $P(B) = \frac{5}{12}$  and  $P(\frac{B}{A}) = \frac{1}{15}$ 

We know that

$$P\left(\frac{B}{A}\right) = \frac{P(A \cap B)}{P(A)} \implies \frac{1}{15} = \frac{P(A \cap B)}{\frac{1}{12}}$$

$$\Rightarrow P(A \cap B) = \frac{1}{180}$$

Also, 
$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$= \frac{1}{12} + \frac{5}{12} - \frac{1}{180}$$
$$= \frac{15 + 75 - 1}{180} = \frac{89}{180}$$

**99.** :  $f(x) = \frac{x}{2}$   $(0 \le x \le 2)$ 

Now, 
$$P(X > 1.5) = \int_{1.5}^{2} \frac{x}{2} dx$$
  
= 0.4375

and 
$$P(X > 1) = \int_{1}^{2} \frac{x}{2} dx = 0.75$$

Hence, 
$$P\left(\frac{X > 1.5}{X > 1}\right) = \frac{P(X > 1.5)}{P(X > 1)}$$
  
=  $\frac{0.4375}{0.75} = \frac{7}{12}$ 

**100.** Since,  $(n+1)p = \frac{101}{3}$  is not an integer.

Therefore, P(X=r) is maximum when  $r = \left\lceil \frac{101}{3} \right\rceil = 33$ .

**101.** : 
$$A(\theta) = \begin{bmatrix} 1 & \tan \theta \\ -\tan \theta & 1 \end{bmatrix}$$

Also, AB = I.

$$\Rightarrow B = A^{-1}$$

$$= \frac{1}{1 + \tan^2 \theta} \begin{bmatrix} 1 & -\tan \theta \\ \tan \theta & 1 \end{bmatrix}$$

$$= \frac{1}{\sec^2 \theta} \begin{bmatrix} 1 & -\tan \theta \\ \tan \theta & 1 \end{bmatrix}$$

$$\Rightarrow (\sec^2 \theta) B = \begin{bmatrix} 1 & -\tan \theta \\ \tan \theta & 1 \end{bmatrix}$$

102. 
$$\begin{vmatrix} 2x+1 & 4 & 8 \\ 2 & 2x & 2 \\ 7 & 6 & 2x \end{vmatrix} = 0$$

 $=A(-\theta).$ 

$$\Rightarrow \begin{vmatrix} 2x+10 & 2x+10 & 2x+10 \\ 2 & 2x & 2 \\ 7 & 6 & 2x \end{vmatrix} = 0$$

$$(R_1 \rightarrow R_1 + R_2 + R_3)$$

$$(2x+10)\begin{vmatrix} 1 & 1 & 1 \\ 2 & 2x & 2 \\ 7 & 6 & 2x \end{vmatrix} = 0$$

$$\Rightarrow (2x+10)\begin{vmatrix} 1 & 0 & 0 \\ 2 & 2x-2 & 0 \\ 7 & -1 & 2x-7 \end{vmatrix} = 0$$

$$\Rightarrow (C_3 \to C_3 - C_1 \text{ and } C_2 \to C_2 - C_1)$$

$$\Rightarrow (2x+10)(2x-2)(2x-7) = 0$$

$$\Rightarrow x = -5, 1, \frac{7}{2}$$

Hence, other roots are 1 and  $\frac{7}{2}$ .

103. The system of given equations are

$$Kx + 2y - z = 1$$
 ...(i)  
 $(K - 1)y - 2z = 2$  ...(ii)

and (K + 2)z = 3 ...(iii)

This system of equations has a unique solution, if

$$\begin{vmatrix} K & 2 & -1 \\ 0 & K-1 & -2 \\ 0 & 0 & K+2 \end{vmatrix} \neq 0$$

$$\Rightarrow (K+2) \begin{vmatrix} K & 2 \\ 0 & K-1 \end{vmatrix} \neq 0$$

$$\Rightarrow (K+2)(K)(K-1) \neq 0$$

$$\Rightarrow K \neq -2, 0, 1$$
i.e.,  $K = -1$ , is a required answer.

**104.** Since, the rank of matrix  $\begin{bmatrix} -1 & 2 & 5 \\ 2 & -4 & a-4 \\ 1 & -2 & a+1 \end{bmatrix}$  is

1, then
$$\begin{vmatrix} 2 & 5 \\ -4 & a - 4 \end{vmatrix} = 0$$

$$\Rightarrow 2a - 8 + 20 = 0$$

$$\Rightarrow 2a + 12 = 0$$

 $\Rightarrow$ 

**105.** If  $b^2 - 4ac \ge 0$ , then the equation  $ax^4 + bx^2 + c = 0$  has all roots real, if b < 0, a > 0, c > 0

a = -6

**106.**  $\log_3 x + \log_3 \sqrt{x} + \log_3 \sqrt[4]{x} + \log_3 \sqrt[8]{x} + \dots$ 

$$\Rightarrow \log_3 x + \frac{1}{2}\log_3 x + \frac{1}{4}\log_3 x + \frac{1}{8}\log_3 x$$

$$+ \dots = 4$$

$$\Rightarrow \log_3 x \left[1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \dots\right] = 4$$

$$\Rightarrow \log_3 x \left[\frac{1}{1 - 1/2}\right] = 8$$

$$\Rightarrow \log_3 x = 4$$

$$\Rightarrow x = 3^4 = 81$$

$$(x + \frac{1}{x})^3 + (x + \frac{1}{x}) = 0$$

107. 
$$\left(x + \frac{1}{x}\right) + \left(x + \frac{1}{x}\right) = 0$$

$$\Rightarrow \left(x + \frac{1}{x}\right) \left[\left(x + \frac{1}{x}\right)^2 + 1\right] = 0$$

From above it is clear that the number of real roots of given equation is 0.

**108.** : *H* is the harmonic mean between *P* and *Q*.

$$H = \frac{2PQ}{P+Q}$$

$$\Rightarrow \frac{H}{P} = \frac{2Q}{P+Q} \text{ and } \frac{H}{Q} = \frac{2P}{P+Q}$$

$$\therefore \frac{H}{P} + \frac{H}{Q} = \frac{^{9}2Q}{P+Q} + \frac{2P}{P+Q} = \frac{2(P+Q)}{P+Q}$$

$$= 2.$$

109. 
$$(\vec{a} \cdot \vec{b}) \vec{b} + \vec{b} \times (\vec{a} \times \vec{b})$$
  

$$= (\vec{a} \cdot \vec{b}) \vec{b} + (\vec{b} \cdot \vec{b}) \vec{a} - (\vec{a} \cdot \vec{b}) \vec{b}$$

$$= \vec{a}$$

**110.** Since, the coordinates of *A*, *B* and *C* are (1, 2, -1), (2, 0, 3) and (3, -1, 2), then

$$\overrightarrow{\mathbf{AB}} = (2-1)\hat{\mathbf{i}} + (0-2)\hat{\mathbf{j}} + (3+1)\hat{\mathbf{k}}$$
$$= \hat{\mathbf{i}} - 2\hat{\mathbf{j}} + 4\hat{\mathbf{k}}$$

and 
$$\overrightarrow{AC} = (3-1)\hat{\mathbf{i}} + (-1-2)\hat{\mathbf{j}} + (2+1)\hat{\mathbf{k}}$$
  
 $= 2\hat{\mathbf{i}} - 3\hat{\mathbf{j}} + 3\hat{\mathbf{k}}$   
 $\cos \theta = \frac{(\hat{\mathbf{i}} - 2\hat{\mathbf{j}} + 4\hat{\mathbf{k}}) \cdot (2\hat{\mathbf{i}} - 3\hat{\mathbf{j}} + 3\hat{\mathbf{k}})}{\sqrt{1 + 4 + 16}\sqrt{4 + 9 + 9}}$   
 $= \frac{2 + 6 + 12}{\sqrt{21}\sqrt{22}} = \frac{20}{\sqrt{462}}$   
 $\Rightarrow \sqrt{462}\cos \theta = 20.$ 

111. Since,  $\vec{a}$  and  $\vec{b}$  are coplanar, therefore  $\vec{a} \times \vec{b}$  is a vector perpendicular to the plane containing  $\vec{a}$  and  $\vec{b}$ . Similarly,  $\vec{c} \times \vec{d}$  is a vector perpendicular to the plane containing  $\vec{c}$  and  $\vec{d}$ . Thus, the two planes will be parallel if their normals, i.e.,  $(\vec{a} \times \vec{b})$  and  $(\vec{c} \times \vec{d})$  are parallel.

$$\Rightarrow \qquad (\vec{\mathbf{a}} \times \vec{\mathbf{b}}) \times (\vec{\mathbf{c}} \times \vec{\mathbf{d}}) = \vec{\mathbf{0}}$$

112. Since, the diagonals of a parallelogram are  $3\hat{\mathbf{i}} + \hat{\mathbf{j}} - 2\hat{\mathbf{k}}$  and  $\hat{\mathbf{i}} - 3\hat{\mathbf{j}} + 4\hat{\mathbf{k}}$ . Then the sides of a parallelogram are  $\vec{\mathbf{a}} = 2\hat{\mathbf{i}} - \hat{\mathbf{j}} + \hat{\mathbf{k}}$  and  $\vec{\mathbf{b}} = \hat{\mathbf{i}} + 2\hat{\mathbf{j}} - 3\hat{\mathbf{k}}$ 

Now. 
$$\vec{a} \times \vec{b} = (2\hat{i} - \hat{i} + \hat{k}) \times (\hat{i} + 2\hat{i} - 3\hat{k}) = \hat{i} + 7\hat{i} + 5\hat{k}$$

Area of parallelogram =  $|\vec{\mathbf{a}} \times \vec{\mathbf{b}}| = \sqrt{1 + 49 + 25} = \sqrt{75}$ 

Area of parameter gram = 
$$|\mathbf{a} \times \mathbf{b}| = \sqrt{1 + 49 + 25} = \sqrt{3}$$
  
113. :  $\cos x + \cos^2 x = 1$ 

$$\Rightarrow \cos x = 1 - \cos^2 x$$
$$= \sin^2 x$$

$$\sin^{12} x + 3\sin^{10} x + 3\sin^8 x + \sin^6 x - 1$$
$$= \cos^6 x + 3\cos^5 x + 3\cos^4 x + \cos^3 x - 1$$

$$=(\cos^2 x + \cos x)^3 - 1 = 1 - 1 = 0$$

$$= (\cos^2 x + \cos x)^3 - 1 = 1 - 1 = 0$$
**114.**  $(\cos \alpha + i \sin \alpha)^{3/5} = [\cos 3\alpha + i \sin 3\alpha]^{1/5}$ 

$$= \left[\cos\frac{2n\pi + 3\alpha}{5} + i\sin\frac{2n\pi + 3\alpha}{5}\right]$$

Required product = 
$$\left(\cos\frac{3\alpha}{5} + i\sin\frac{3\alpha}{5}\right) \left(\cos\frac{2\pi + 3\alpha}{5} + i\sin\frac{2\pi + 3\alpha}{5}\right)$$

$$\times \left(\cos\frac{4\pi + 3\alpha}{5} + i\sin\frac{4\pi + 3\alpha}{5}\right) \left(\cos\frac{6\pi + 3\alpha}{5} + i\sin\frac{6\pi + 3\alpha}{5}\right)$$
$$\times \left(\cos\frac{8\pi + 3\alpha}{5} + i\sin\frac{8\pi + 3\alpha}{5}\right)$$

$$= \cos\left(\frac{3\alpha}{5} + \frac{2\pi}{5} + \frac{3\alpha}{5} + \frac{4\pi}{5} + \frac{3\alpha}{5} + \frac{6\pi}{5} + \frac{3\alpha}{5} + \frac{8\pi}{5} + \frac{3\alpha}{5}\right) + i\sin\left(\frac{3\alpha}{5} + \frac{2\pi}{5} + \frac{3\alpha}{5} + \frac{4\pi}{5} + \frac{3\alpha}{5} + \frac{6\pi}{5} + \frac{3\alpha}{5} + \frac{8\pi}{5} + \frac{3\alpha}{5}\right)$$

$$= \cos (4\pi + 3\alpha) + i \sin (4\pi + 3\alpha)$$
$$= \cos 3\alpha + i \sin 3\alpha$$

115. 
$$\frac{(1+i)^2}{i(2i-1)} = \frac{1+i^2+2i}{i(2i-1)} = \frac{2i}{i(2i-1)}$$
$$= \frac{2(2i+1)}{4i^2-1} = \frac{4i+2}{-4-1} = -\frac{4}{5}i - \frac{2}{5}$$

$$\therefore$$
 Imaginary part of  $\frac{(1+i)^2}{i(2i-1)} = -\frac{4}{5}$