Structural Inorganic Chemistry

Molecular v. extended solids

Types of solids

- crystalline, long range order (>10³ atoms)

- amorphous, short range order (~ 100 Å)

special type :glass, characterised by the glass transition temperature, T_g

Crystalline

- ionic NaCl



- covalent diamond, SiC

- metallic Cu, fcc



Inorganic structures

Ionic model

- electrostatic forces between ions
- close packing of ions
- ions as hard spheres

Coulombs law

$$F = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q_1 Q_2}{r^2}$$

Electrostatic energy

$$U = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q_1 Q_2}{r}$$

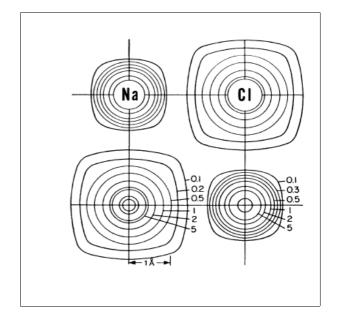
Hence close packing

Ions as hard spheres

Closed "shells" np⁶

Electron density map from x-ray diffraction of NaCl

Witte and Wölfel Rev. Mod. Phys 30, 51 (1958)



Building up inorganic structures

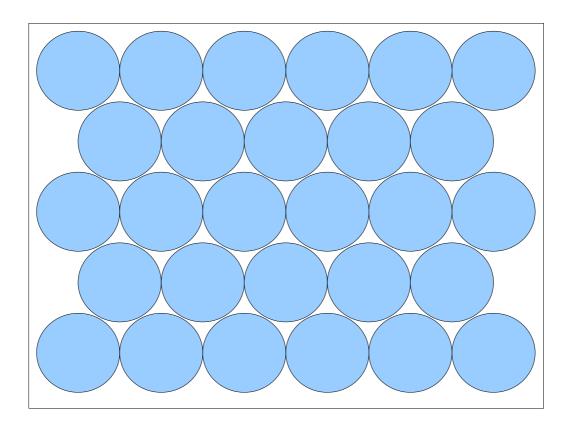
Two ideas

- closed packed layers of spheres occupy 74% of space
- filling of interstitial sites

Excellent descriptive value

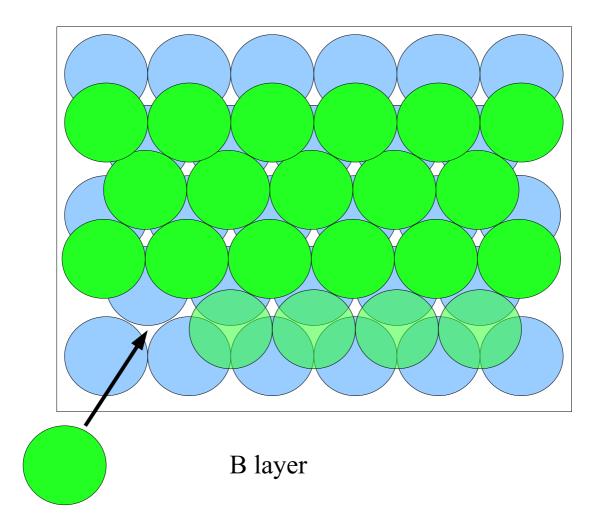
Limited predictive use

First layer



A layer

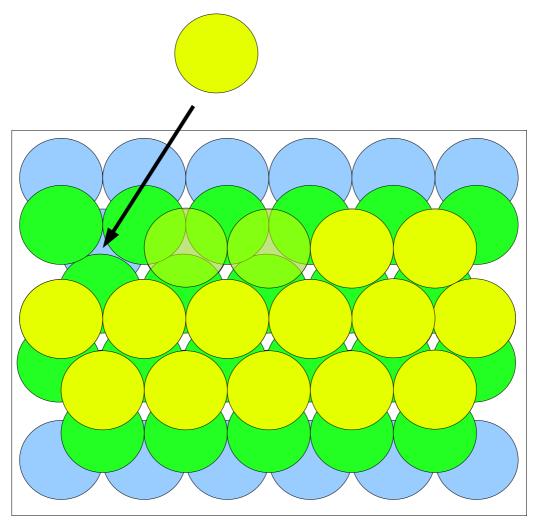
Second layer



Third layer

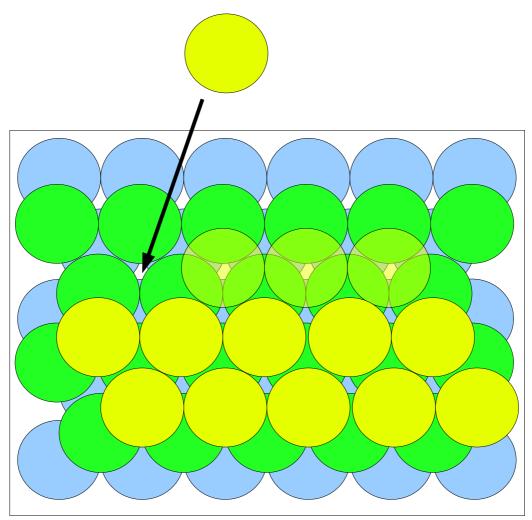
Two possibilities

Above original A layer



AB AB AB AB Hexagonal close packing, hcp

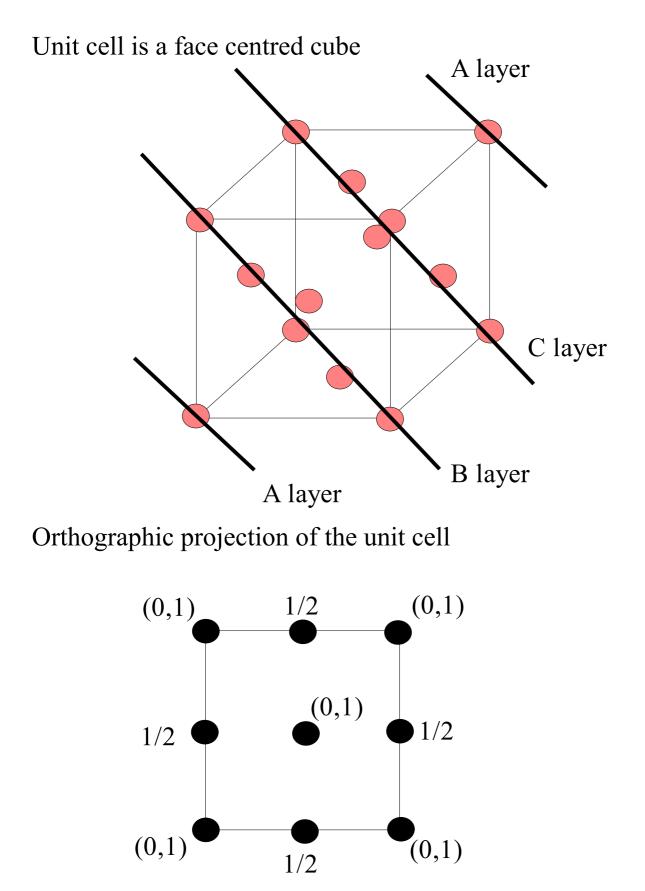
Above holes common to A and B layers



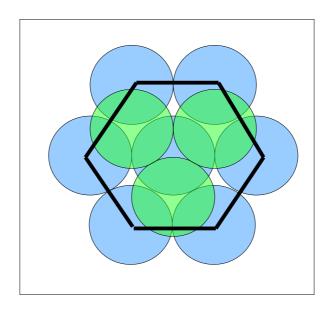
C layer

ABC ABC ABC Cubic close packing, ccp

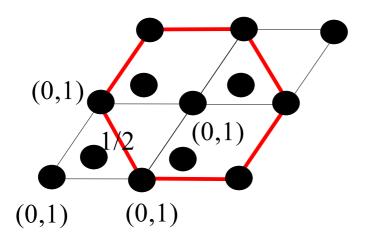
Relationship between close packing and unit cell Cubic close packing



Hexagonal close packing



Orthographic projection

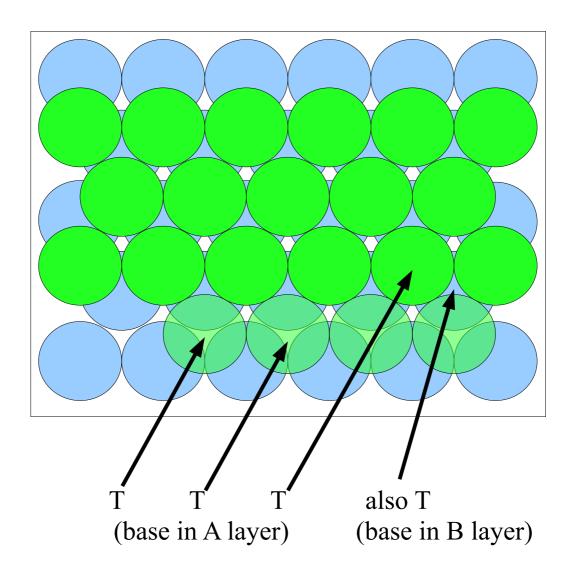


Unit cell has atom positions labelled

Interstitial sites

Tetrahedral

Between two layers AB, or BA, BC and CB

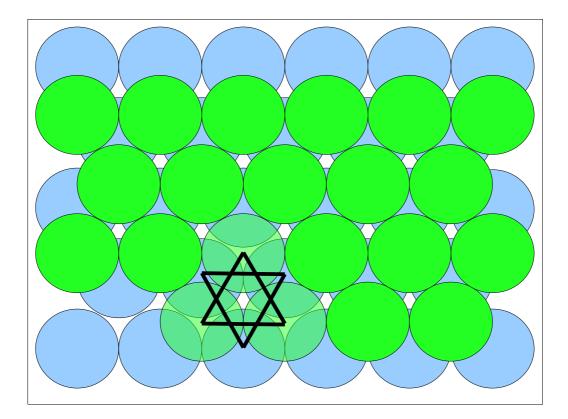


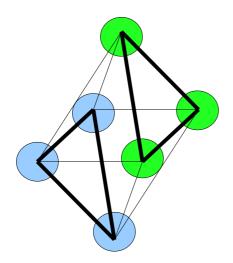
Two sites for every close packed ion.

Octahedral

Between two layers AB, or BA, BC and CB

Harder to spot





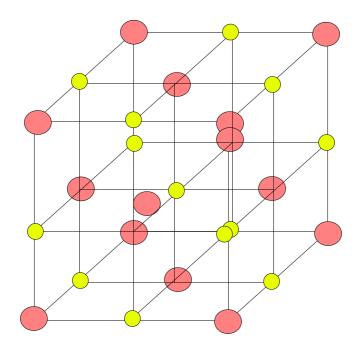
One for each close packed ion

Structures

Type and fraction	сср	hcp
All tetrahedral	Fluorite, CaF ₂	(not known)
All octahedral	Rock salt, NaCl	Nickel arsenide NiAs
¹ / ₂ tetrahedral	Zinc blende, ZnS	Wurtzite, ZnS
¹ / ₂ octahedral	CdCl ₂	CdI ₂

Rock salt structure

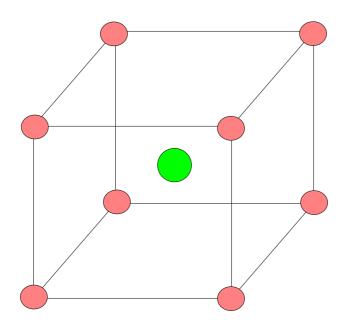
Interpenetrating fcc



NB

Caesium chloride structure

Not close packed, occupies 68% of space



Not body centred cubic

Definitions

Unit cell

The smallest repeating unit which shows the full symmetry of the crystal structure. Translates it to build up the entire structure

Asymmetric unit

Smallest collection of atoms which can be used to generate the entire structure when the symmetry operations contained within the space group are applied

Space group

A three dimensional point group: Add elements of translation to the point group. Also contains the elements:

rotation + translation = screw axis mirror + translation = glide plane Combine 32 point groups with these elements gives 230 space groups

Point group

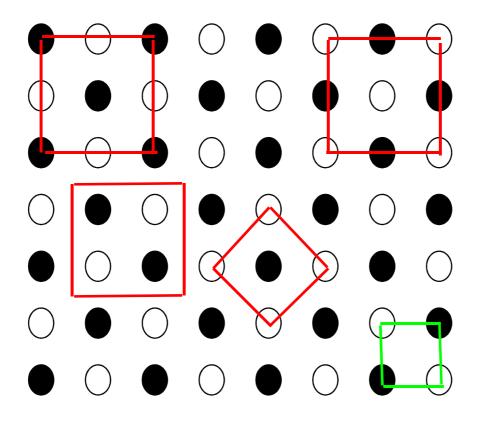
A collection of symmetry elements obeying the mathematical axioms of a group: closure, identity, associative, inverse. 32 groups in all

- rotation axes 1,2,3,4 and 6
- inversion axes $\overline{1}, \overline{2}, \overline{3}, \overline{4}$ and $\overline{6}$
- mirror plane, *m*

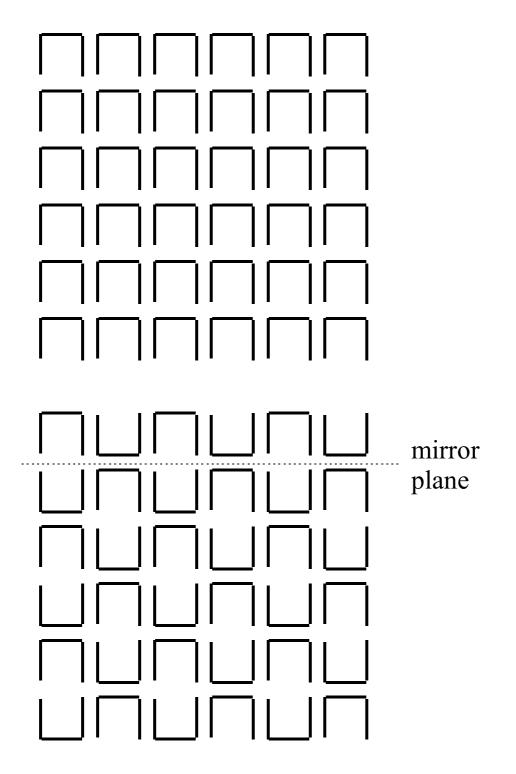
Note the absence of a fivefold rotation axis.

Unit Cell

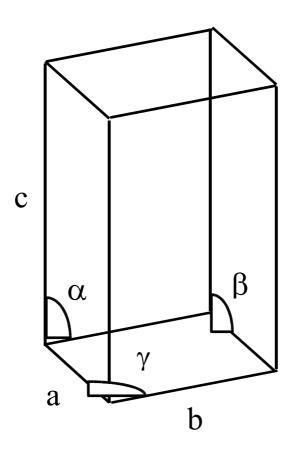
red = correct unit cells green = incorrect



Aymmetric unit



Lattice parameters

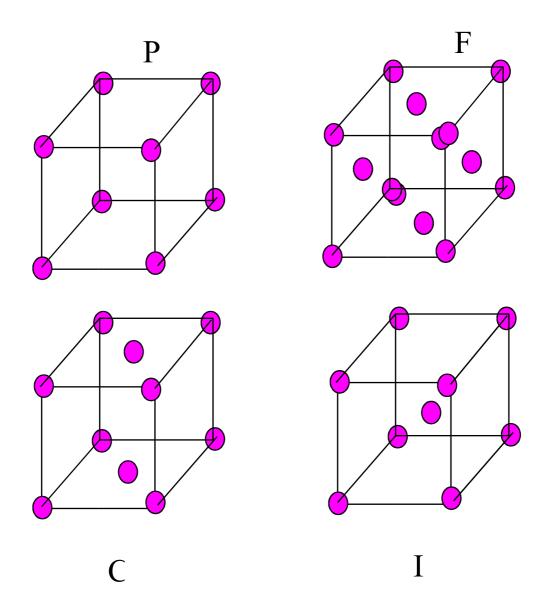


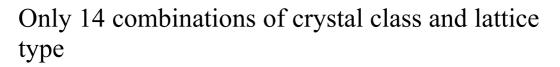
Crystal classes

triclinic	a≠b≠c	α≠β≠γ
monoclinic	a≠b≠c	$\alpha = \gamma = 90^{\circ} \neq \beta$
orthorhombic	a≠b≠c	$\alpha = \beta = \gamma = 90^{\circ}$
tetragonal	a=b≠c	$\alpha = \beta = \gamma = 90^{\circ}$
cubic	a=b=c	$\alpha = \beta = \gamma = 90^{\circ}$
hexagonal	a=b≠c	$\alpha = \beta = 90^{\circ} \gamma = 120^{\circ}$
trigonal	a=b=c	$\alpha = \beta = \gamma \neq 90^{\circ}$

Basic types of Cells

Primitive - contains only one lattice point





Bravais lattices