

Mathematics 012A
Test 2, November 10, 2006
Solutions

Part A	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
Answers	B	D	B	A	A	E	D	D	B	E	C	B	C	E	A	A	B	C	B	D

Part B

B1.
$$\frac{(8x^3y^{3/2})^{2/3}}{(4x^2y^{4/3})^{1/2}} = \frac{(4x^2y)}{(2xy^{2/3})} = 2xy^{\frac{1}{3}}$$

B2.
$$\begin{aligned} \frac{1}{\log_8 a} + \frac{1}{\log_4 a} &= \log_a 8 + \log_a 4 = \log_a 2^3 + \log_a 2^2 = 3\log_a 2 + 2\log_a 2 = 5\log_a 2 \\ &= \frac{5}{\log_2 a} \quad \text{so } M=5 \end{aligned}$$

B3. $\log_2 x + \log_2(x+6) = 4 \Rightarrow \log_2 x(x+6) = 4 \Rightarrow x(x+6) = 16 \Rightarrow x^2 + 6x - 16 = 0$
or $(x-2)(x+8) = 0 \Rightarrow x=2$ since $x=-8$ is inadmissible

B4. $f'(x) = 3x^2 - 12 = 3(x^2 - 4) = 3(x-2)(x+2)$ so $x=-2$ is a critical point
Consider $f(-3) = 14$, $f(-2) = 21$, $f(0) = 5$;
so $f_{\max} = 21$ at $x=-3$ and $f_{\min} = 5$ at $x=0$

B5. $4x^3 + 9x^2y + 3x^3y' - 3y^2y' = 0 \Rightarrow 3(x^3 - y^2)y' = -(4x^3 + 9x^2y) \Rightarrow y' = \frac{-(4x^3 + 9x^2y)}{3(x^3 - y^2)}$

B6. $A = xy$ where $2x + 3y = 1200$ or $y = \frac{1200 - 2x}{3} = 400 - \frac{2x}{3}$ so $A = x(400 - \frac{2x}{3})$
or $A = 400x - \frac{2x^2}{3}$ on $[0, 600]$ The endpoints can be ignored.
 $A' = 400 - \frac{4x}{3} = 0 \Leftrightarrow x = 300$, $y = 200$ so $A_{\max} = 60,000 \text{ m}^2$