

5. (a) Define the electric current  $I$  through a surface  $A$ . Define the symbols involved. [2]
- (b) Define the current density  $\mathbf{J}$  in terms of the drift velocity of the carriers, the charge of the carriers, and the number of charge carriers per unit volume. [2]
- (c) Write down an expression relating the electric current  $I$  and the current density  $\mathbf{J}$ . [2]
- (d) Write down Ohm's law, relating the current density and the electric field. [2]
6. (a) Write down an expression for the Lorentz force on a charge  $q$  moving at velocity  $\mathbf{v}$ . [2]
- (b) State Gauss's law for magnetism in differential form. [2]
- (c) Write down Faraday's law in integral form. [2]

## SECTION B

7. (a) A sphere of radius  $R_1$  has a charge  $+Q$  uniformly distributed throughout its volume. Surrounding the sphere and concentric with it is a thin spherical shell of radius  $R_2$  which carries a charge  $-Q$  uniformly distributed over its surface. Using Gauss' law, determine the electric field as a function of the distance  $r$  from the centre of the spheres in the following three cases:
  - i.  $r < R_1$  [4]
  - ii.  $R_1 < r < R_2$  [4]
  - iii.  $R_2 < r$  [4]
- (b) Determine the electrostatic energy  $U$  of a thin spherical shell of radius  $R$  which carries a charge  $Q$  uniformly distributed over its surface [Hint: imagine to assemble the spherical shell by superimposing shells of radius  $R$  and infinitesimal charge  $dq$ .]. [8]
8. (a) Explain what is meant by "capacitor", and define the capacitance of a capacitor. [4]
- (b) Consider a charged spherical capacitor, consisting of two spherical conducting shells with diameters  $a, b$  ( $a < b$ ) and charges  $+Q$  and  $-Q$  respectively.
  - i. Determine the electric potential everywhere in the space between the two "plates". [3]
  - ii. Determine the capacitance  $C$  of the spherical capacitor. [4]
  - iii. Determine the electric field everywhere in the space between the two "plates", and the associated energy density. [4]
  - iv. Either by direct integration of the energy density of the electric field, or otherwise, determine the total energy stored in the capacitor. [5]