

MTH4101

Calculus II, Spring 2013

Problem sheet for Tutorial 5

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- The questions are designed to help you with material covered in Week 5. You will get help with them in the tutorial on 14 or 15 February.
- You should write up your solution to the starred question (*) clearly and hand it in to your personal tutor in your assigned tutorial on 28 February or 1 March for feedback. Remember to put your full name and student number on the top of your solution. Your marked solution to the feedback question will be returned to you in your tutorial on 7 or 8 March.
- It is important that you try to do all of the questions.
- There are no tutorials for Calculus II during the midterm test week of 18–22 February.
- The midterm test for Calculus II will take place in the afternoon of Wednesday, 20 February 2013 in the computer labs. Details are on the course website.
- 1: Write out the first three terms of each of the following series and then find the sum:
 - (a) $\sum_{n=0}^{\infty} \left(\frac{2}{5^n} \frac{(-1)^n}{3^n} \right)$, [2008 exam question] (b) $\sum_{n=1}^{\infty} \frac{4}{(4n-3)(4n+1)}$.
- 2: Determine whether the following series converge (giving the sum) or diverge:

(a)
$$\sum_{n=0}^{\infty} \left(\frac{1}{\sqrt{2}}\right)^n$$
, (b) $\sum_{n=1}^{\infty} \ln\left(\frac{n}{n+1}\right)$.

- (*) 3: Use the *n*th term test or the integral test to determine whether the following series converge or diverge:
 - (a) $\sum_{n=2}^{\infty} \frac{\sqrt{n}}{\ln n}$, (b) $\sum_{n=1}^{\infty} n \sin \frac{1}{n}$, (c) $\sum_{n=1}^{\infty} n^2 e^{-n^3}$.