

MTH4100

Exercise sheet 4

Calculus 1, Autumn 2012 Prof. Bill Jackson

These questions are designed to help you understand the material covered in week $n, n \in \mathbb{N}$ lectures. Exercise sheets will typically be handed out in the Tuesday lecture of week n+1. You will get help on them in the exercise class on Tuesday or Wednesday of the same week. You should write up your solution to the starred question (*) clearly and hand it in to your assigned helper during your week n+2 exercise class for feedback. Put your full name and student number on the top of your solution. It is important that you try to do all of the numbered questions, not just the starred question.

1. Let

$$f(x) = \frac{-x^2 + \alpha}{2x + 4} \quad .$$

where α is a real constant.

- (a) Find the asymptotes to f(x).
- (a) Sketch the graph of f(x) for $\alpha = 1$.
- (*)2. Find any horizontal, vertical, or oblique asymptotes of

[2007 exam question]

$$f(x) = \frac{2x^2}{x - 7} \quad .$$

3. (a) Define g(5) in a way that extends

[2008 exam questions]

$$g(x) = \frac{4x^2 - 100}{4x - 20}$$

to be continuous at x = 5.

(b) For what value of a is

$$f(x) = \begin{cases} x^2 - 1, & x < 3 \\ 2ax, & x \ge 3 \end{cases}$$

continuous at every $x \in \mathbb{R}$? Justify your answer.

(c) Can $f(x) = x(x^2 - 1)/|x^2 - 1|$ be extended to be continuous at x = 1 or x = -1? Give reasons for your answers.