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BACHELOR IN COMPUTER APPLICATIONS

Term-End Examination

June, 2008

CS-60: FOUNDATION COURSE IN MATHEMATICS IN COMPUTING

Time: 3 hours Maximum Marks: 75

Note: Question No. 1 is **compulsory**. Attempt any **three** questions from Questions No. 2 to 6. Use of calculator is permitted.

- 1. (a) Fill in the blanks in the following questions:
 - (i) If a line makes angles α , β , γ with the coordinate axes, then

$$\sin^2\alpha + \sin^2\beta + \sin^2\gamma = \dots$$

- (ii) The length of the line whose projections on the axes are 2, 3, 6 is
- (iii) Volume of the sphere $x^2 + y^2 + z^2 + 2x 4y + 8z 2 = 0$ is
- (b) Find the roots of the equation

$$(x^2 - 5x)^2 - 30(x^2 - 5x) - 216 = 0$$

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- (c) Find the equations of the lines which pass through (4, 5) and make an angle of 45° with the line 2x + y + 1 = 0.
- (d) Find the equation of the circle which is concentric with $x^2 + y^2 8x + 12y + 43 = 0$ and passes through (6, 2).
- (e) Evaluate

$$\lim_{x \to 0} \frac{x + \sin x}{x^2 + x}$$

(f) State whether it is even or odd for the following functions:

(i)
$$f(x) = 7x^2 - 11$$

(ii)
$$f(x) = e^{3x} - e^{-3x}$$

(g) Verify $(A \cup B)^C = A^C \cap B^C$, where

$$A = \{1, 3, 4, 5, 9\}, B = \{2, 4, 6, 9, 10\}$$

$$U = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$$

(h) The power transmitted by a belt is proportional to

$$T\,v-\frac{Wv^3}{q}$$

where v = speed of the belt, T = tension on the driving side, and W = weight per unit length of belt. Find the speed at which the transmitted power is maximum.

(i) Evaluate

$$\int (\log x^3 + 9 \sin^3 x) (27 \sin^2 x \cos x + \frac{3}{x}) dx$$

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(j) If x and y are real, solve the equation

$$\frac{ix}{1+iy}=\frac{3x+4i}{x+3y}.$$

- (k) Determine the equation of a circle if its centre is (8, -6) and which passes through the point (5, -2).
- (1) Find the equation of a line perpendicular to the line 3x 4y + 7 = 0 and which passes through the point (-3, 2).
- (m) Find the value of the determinant :

(n) Solve the following equations by Cramer's rule:

$$x + y + z = 1$$

$$x + 2y = 3$$

$$x + 2y + z = 7$$

(o) Can Rolle's theorem be applied to the function

$$f(x) = \sin^2 x$$

on the interval $[0, \pi]$? Find 'c' in case it can be applied. 15×3=45

2. (a) Evaluate any one of the following:

(i)
$$\lim_{x \to 0} \frac{x - \sin x}{x^3}$$

(ii)
$$\lim_{x \to \infty} \left(1 + \frac{1}{x^2}\right)^x$$

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- (b) If $\sin y = x \sin (a + y)$, prove that $\frac{dy}{dx} = \frac{\sin^2 (a + y)}{\sin a}$
- (c) Find $\frac{dy}{dx}$ for each of the following, where (i) $y = \cos^{-1} (4x^3 - 3x)$ (ii) $y = x^{(x^3)}$ 3+3+4
- 3. (a) Integrate any one of the following :

(i)
$$\int e^{3x} \sin x \, dx$$

(ii)
$$\int \frac{1}{e^x - 1} dx$$

- (b) Evaluate $\int\limits_{1}^{4}e^{2x}\;dx$
- (c) Find the area lying between the parabola $y = 4x x^2$ and the line y = x. 3+3+4
- 4. (a) Express $\frac{(1+i)(2+i)}{3+i}$ in the form a + ib.
 - (b) Find the value of 'k' for which the function

$$f(x) = \begin{cases} \frac{\sin 5x}{3x}, & x \neq 0 \\ k, & x = 0 \end{cases}$$

is continuous at x = 0.

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(c) A curve is drawn to pass through the points given by the following table :

х	у
1	2
1.5	2.4
2	2.7
2.5	2.8
3	3
3.5	2.6
4	2.1

Estimate the area bounded by the curve, the x-axis and the lines x = 1, x = 4. 3+3+4

- 5. (a) Find the equation of the circle with centre (1, 1) and which touches the line x + y = 1.
 - (b) Find the focus, vertex, length of latus rectum, equation of the directrix of the parabola $y^2 = -4x$.
 - (c) Find the eccentricity, foci, length of the latus rectum of the ellipse

$$3x^2 + 4y^2 - 12x - 8y + 4 = 0.$$
 $3+3+4$

- **6.** (a) Find the equation of a sphere with centre (-1, 4, -5) and radius as 5 units.
 - (b) Find the equation of a right circular cylinder of radius 2 whose axis passes through (1, 2, 3) and has direction cosines proportional to 2, -3, 6.

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(c) Find the equation of a cone whose vertex is at the origin and the guiding curve is

$$\frac{x^2}{4} + \frac{y^2}{9} + z^2 = 1, \quad x + y + z = 1.$$

3+3+4