Paper Number(s): **E4.18**AM5

IMPERIAL COLLEGE OF SCIENCE, TECHNOLOGY AND MEDICINE UNIVERSITY OF LONDON

DEPARTMENT OF ELECTRICAL AND ELECTRONIC ENGINEERING EXAMINATIONS 2001

MSc and EEE PART IV: M.Eng. and ACGI

RADIO FREQUENCY ELECTRONICS

There are SIX questions on this paper.

Answer FOUR questions.

Time allowed: 3:00 hours

Examiners: Papavassiliou, C. and Payne, A.J.

- 1. A certain circuit will be used as a filter between a generator of amplitude V_g and impedance Z_g and a load Z_L . This circuit can be represented by an ABCD matrix.
- a) State the definition of the ABCD matrix. From this definition directly compute the voltage transfer function $G=V_L/V_G$ of the circuit of figure 1. in terms of its ABCD parameters, as well as Z_g and Z_L .

[5 marks]

b) From the definition of the ABCD matrix directly compute the current transfer function $H=I_L/I_G$ of the circuit in figure 1. in terms of its ABCD parameters, as well as Z_g and Z_L .

[5 marks]

c) From your answers in questions a) and b) above compute the power gain of this network.

[5 marks]

d) Using component ABCD matrices compute the voltage and current gain of the tee network in fig. 2. Compute its input impedance if it is terminated in a load Z_L . Show it performs an impedance matching function, but do not compute the component values necessary to implement a particular impedance matching transformer.

[10 marks]

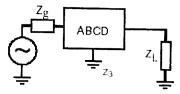


Figure 1: A 2-port network connected as a filter

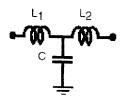


Figure 2: A Tee network filter

- 2. High speed diodes manufactured on an Integrated Circuit substrate often have one of their terminals, usually the cathode, connected to the substrate. The substrate is, however, also the ground plane for the microstrip lines used for interconnection and impedance matching. We are required to design a monolithic microwave switch using a grounded cathode diode as depicted in figure 3.
- a) Describe an impedance transformation approach to make this diode appear in series, so that the switch depicted in figure 4. can be implemented. Implement this impedance transformation approach using microstrip lines. If the phase velocity on a substrate is 1x10⁸ m/s what is the required physical length of these lines for a 10 GHz operating frequency?

[5 marks]

b) The diode must be switched on and off to perform the couple/isolate functions of the switch in figure 4. Design appropriate microstrip networks to supply the necessary bias. Note that your circuit should be such that the supply is completely invisible at signal frequencies.

[7 marks]

c) With the aid of a diagram show how we can implement DC isolation between the power supply and the external circuits connected to the two terminals of the switch.

[5 marks]

d) Compute the insertion loss, $\left|\frac{1}{S_{21}}\right|^2$ of your switch when used between 50 Ω lines. Explain how you can minimise the insertion loss of this switch by properly choosing the impedance of your transmission line transformers. What is the minimum insertion loss of this diode in the ON state given that the diode ON resistance is 15 ohms, and the fabrication process permits you to manufacture transmission lines of Z_0 between 20 and 125 ohms?

[8 marks]

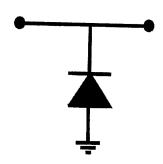


Figure 3: A diode is only available as a shunt connected element



Figure 4: Desired connection for the diode

3. A mobile telephone operator needs you to specify the required transmitter power, and physical size of a base station antenna in order to implement error free communications between the base station and mobile terminals. The following specifications are available:

System				
Operating frequency	1.8GHz			
Data bandwidth	56 kBit/s			
Analogue Bandwidth	10 kHz			
Range	10km			
Mobile Terminal				
Antenna effective aperture	16.67 cm ²			
Antenna Noise temperature	300 K			
Receiver path noise figure	15dB			
Transmitter power	10 mW			
Base Station				
Antenna temperature	150 K			
Receiver path noise figure	5dB			
Antenna aperture efficiency	50%			
Antenna Electrical efficiency	90%			

a) What is the required S/N at the end of the receiver path in order to implement error free communications under the system specifications?

[5 marks]

b) Assume the base station is in receive mode, and that a minimum S/N=15dB above the theoretical minimum is required for error free reception. What must the base station antenna effective aperture be to ensure error free reception? What is its physical size? What is its directivity? What is its polar extent, given that its azimuthal extent is 50 degrees?

[10 marks]

c) Assume the base station is in transmit mode. What is the minimum transmit power which will result in error-free reception at the mobile terminal? You may assume the same, as in part (b), S/N ratio for error free reception.

[10 marks]

$$(k_B = 1.38 \cdot 10^{-23} \text{ J/K})$$

4.	An	ideal	transconductor	is	defined	by	the	following	equations:
----	----	-------	----------------	----	---------	----	-----	-----------	------------

 $I_I = 0$

 $I_2 = g V_I$

a) Write the Y matrix for an ideal transconductor.

[2 marks]

b) Write the Y matrix for the circuit in fig. 5a, where two transconductors, of transconductance g and -g are connected so that the input of one is the output of the other. This circuit is one of many possible implementations of a gyrator, which we will symbolise as K(K=1/g) (fig 5b). From the Y matrix derive the ABCD matrix for this gyrator. What is its bandwidth?

[4 marks]

c) Derive the ABCD matrix for a cascade of two gyrators, K_1 and K_2 . From your answer draw and clearly label an equivalent circuit for this configuration.

[5 marks]

d) Derive the *ABCD* matrices, and draw and clearly label equivalent circuits for each of the networks in figure 6.

[8 marks]

e) Deduce, draw and clearly label equivalent circuits for a series LC network substituted for \mathbf{Z} in fig 6a, and a parallel LC network substituted for \mathbf{Z} in fig 6b, both terminated at \mathbf{Z}_{T} .

[6 marks]

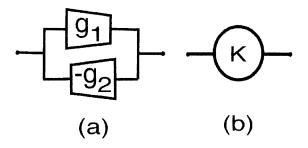


Figure 5 A gyrator (a) implementation, (b) symbol

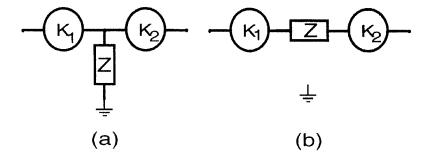


Figure 6 Gyrated circuit elements (a) shunt, (b) series

- 5) In an RF application we need to isolate our circuit from microwave oven interference, and thus decide to use a 2.45 GHz band reject filter with 100 MHz bandwidth. We will base the design on the 3rd order 1dB Chebyshev normalised lowpass prototype of figure 7.
- a) Using this prototype design a 2.45 GHz lumped band reject filter with a stop band of 100 MHz to operate between 50 Ohm source and load.

[10 marks]

b) How can the filter components be implemented using transmission lines? Assume you are working with balanced lines so that both series and shunt connections are allowed. Write equations for these components in terms of the line segment impedances and lengths. Draw a schematic for the filter clearly illustrating the appearance of the filter if made using balanced lines.

[5 marks]

c) Implement the filter using only microstrip resonators and microstrip lines. Write expressions for, but do not compute line lengths and impedances.

[10 marks]

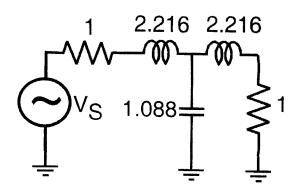


Figure 7: Filter prototype of question 5.

- 6) The network in figure 8 is often used as an impedance matching transformer between real impedances R and R_{in} .
- a) Derive expressions for the components of the impedance matching network in figure 8. You are given the terminating resistances, the frequency of operation, and the desired fractional 3dB bandwidth of the match.

[10 marks]

b) What is the range of ratios between R and R_{in} that you can achieve with this transformer?

[10 marks]

c) How do you need to modify the component values you calculated in (a) to accommodate complex terminating impedances?

[5 marks]

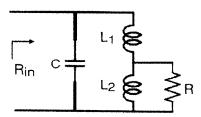


Figure 8: An impedance matching circuit.

RF

Question 1

$$\begin{array}{c} \lambda \\ \lambda \\ \vdots \\ \lambda \\ \end{array} = \begin{bmatrix} A & B \\ C & D \end{bmatrix} \begin{bmatrix} v_2 \\ -i_2 \end{bmatrix}$$

$$V_1 = V_8 - Z_5 \dot{l}_1 \Rightarrow \dot{l}_1 = \frac{V_8 - V_1}{Z_8}$$

$$V_2 = -Z_L i_2 = -V_2 = -V_2$$

$$V_1 = AV_2 - B\dot{\iota}_2 = AV_2 + B\frac{V_2}{Z_1}$$
 (3)

$$L_1 = CV_2 - DI_2 \Rightarrow \frac{V_8 - V_1}{Z_5} - CV_2 + D\frac{V_2}{Z_1} \Rightarrow$$

$$\frac{\sqrt{8}}{Z_{5}} = \frac{A V_{2}}{Z_{5}} + \frac{B V_{2}}{Z_{5}} + \frac{C V_{2}}{Z_{L}} + \frac{O V_{2}}{Z_{L}} \Rightarrow$$

$$\forall g = V_2 \cdot \left(A + \frac{B}{Z_L} + CZ_S + DZ_S - \sum_{L} \right) =$$

$$\frac{V_2}{V_2} = \left(A + \frac{B}{Z_L} + CZ_S + 2Z_S\right)^{-1} = G$$
 [5]

$$L_1 = CV_2 - Di_2 = -CZ_1I_2 - DI_2 = >$$

$$I_1 = I_2(-CZ_1-D) \Rightarrow I_2 - \frac{1}{CZ_1+D} = H LSI$$

$$= \begin{bmatrix} 1 - \omega^2 \lambda_1 C & \beta \omega \lambda_1 \end{bmatrix} \begin{bmatrix} 1 & \beta \omega \lambda_2 \end{bmatrix} = \begin{bmatrix} 1 - \omega^2 \lambda_1 C & \beta \omega \lambda_1 + \lambda_2 - \beta \omega \lambda_2 \lambda_2 C \end{bmatrix}$$

$$G = \left(\frac{A+B}{RL} + CRs + D\frac{Rs}{RL}\right)^{-1} =$$

$$= \left(1 - \omega^2 L C + j \omega \left(\frac{L_1 + L_2}{R_L} - j \omega^2 L_1 L_2 C\right) + \frac{1}{R_L} +$$

$$\int \omega R_s C + (1 - \omega^2 L_2 C) \frac{R_s}{R_L}$$

An impedance metching, network would

present Tin = Zs

$$Z_{in} = \frac{V_{i}}{I_{i}} \frac{AZ_{L} + B}{CZ_{L} + D} = \frac{(-\omega^{2} \lambda_{i}C)Z_{L} + j\omega(k_{2} + k_{2}) - j\omega^{3}k_{2}k_{i}C}{j\omega Z_{L}C + (1-\omega^{2}k_{2}C)}$$

[0]

Question 2

2) Ploice it between two &yroctors.

LII

7/4 4 7/4

[2]

$$f = 10^{10} \text{ Hz}$$
 $= 10^{10} \text{ cm/sec}$ $= 10^{10} \text{ cm/sec}$ $= 10^{10} \text{ cm/sec}$ $= 10^{10} \text{ cm/sec}$

b) Need to supply DC bear though a 1/4

Piece of line:

Sign F Signal.

[7]

2/4 for DC bear

13]

2/4 open to establish se ground

c). Need to introduce two corpacitors,

d) if the crode appears is:

 $\frac{Z_0}{Z_0} = \frac{Z_0}{Z_0}$ $\frac{Z_1}{Z_0}$ $\frac{Z_1}{Z_0}$ $\frac{Z_1}{Z_0}$ $\frac{Z_0}{Z_0}$

oz, in reduced units it is a

 $2 = \frac{\chi_T^2}{\chi_{\alpha} \chi_{\alpha}} = 1$

A series impedance hors x y metrix. (in red. units)

Y= (Y-4) and the Szi element is:

 $S_{24} = \frac{-2421}{1+411+422-\Delta 4} = \frac{24}{1+24+24^2} = \frac{1}{521} - \frac{1}{24} + \frac{1}{24} = \frac{1}{24}$

since $y = Z_p Z_p$ to minimise the loss

to minimise $J = \frac{1}{|S_2|} = \frac{2L - 4(2+24) - 1 - 24 - 24^2}{24}$

= -1 x1 c.e. Lis monotonically decreasing

with y. Then we need to use the minimum

possible Zr for the gyrators, Zr=200



then
$$Y = 10 \times 50 = 1.25$$
 (20)2 =

and
$$L = (1+24+24)^{\frac{1}{2}}$$
 7.0225 = 8.46 dB.

Question 3.

a) From the Shoumon theorem, if Cir

the corporaty:

$$C = B \ln s / 1 = 2 = 2 = -1$$

it is quen: C=56 x103

[5]

8) By the fries formula,

Prec = Pr. Aestr AettR

7 = C = 0.167 m

the rouge is given as R= 10 m.

The mobile terminal power is Iw

and the antenna aperture is 16.67×104 m2.

then Prec = 10w × 16.67×10-4. Aett B.S. -

= AeHss . 5.877x10-12 (w)

The noise power received is just. PN=KTAB=

 $= 1.38 \times 10^{-23} \times 150^{+104} = 2.07 \times 10^{-17}$

therefore, the required signal power is:

Psig = PN. S/N . NF. SNR = 2.07 x10 1x 47 5 x3.16 x 31.6 =

= 3.82 x10-14 W

then, the bosestation effective opertuse is:

Acff x 5.37 x x 10-12 = 8.82 x 10-14 => Aeff = 0.164 m2

Since Aeff = Applys · 2 => Applys = 0.164m² = 0.328m²

The derectivity is: G = nee - Q where G is the going

and $G = 4\pi Reff \Rightarrow D = \frac{1}{m_{el}} \cdot \frac{4\pi Reff}{A^2} = \frac{1}{0.8} \frac{4\pi r_0.164}{(0.167)^2}$

then 0=83.6

In terms of the ourgular extent the directionly

US:

D & 41000. 4 8=30,

 $\theta = \frac{41000}{50 \times 83.6} = 10^{\circ}$

CIOI.

c) Once agazin, the received power is Pat = Pt. AeHr AeHR

R²,² to simplify coclailation, we already know Prec for Alie system, for (Donce): Prec = Ptrom x 8,82×10 4 w. the required received power is; Prec = k TANY B. S/Nec SNRMIN = 00 = 20 x Prec B.s

then the transmitter power is $P_7 = 200 \text{mW}$ ISI

Question 4

$$y = \begin{pmatrix} 0 & 0 \\ 9 & 0 \end{pmatrix}$$

B)
$$Y = \begin{pmatrix} 0-8 \\ 80 \end{pmatrix}$$
 (since the two nets are

connected opposite to each other; id they

metricas.

derentian of ABCD from 4:

$$\begin{pmatrix} V_1 \\ 1 \end{pmatrix} = \begin{pmatrix} A & B \\ C & \lambda \end{pmatrix} \begin{pmatrix} V_2 \\ -J_2 \end{pmatrix} \Rightarrow \begin{pmatrix} I & O_1 \\ Y_1, & Y_{12} \end{pmatrix} \begin{pmatrix} V_1 \\ V_2 \end{pmatrix} = \begin{pmatrix} A & B \\ C & \lambda \end{pmatrix} \begin{pmatrix} O_1 & I \\ -Y_{21} & -Y_{22} \end{pmatrix} \begin{pmatrix} V_1 \\ V_2 \end{pmatrix}$$

$$= \left(\begin{array}{c} A & B \\ C & D \end{array} \right) = \frac{1}{Y_{21}} \left(\begin{array}{c} 1 & O \\ Y_{11} & Y_{12} \end{array} \right) \left(\begin{array}{c} -Y_{22} & -I \\ Y_{21} & O \end{array} \right) = \frac{1}{Y_{21}} \left(\begin{array}{c} -Y_{22} & -I \\ -D & -Y_{11} \end{array} \right)$$

to the gyractor:
$$\begin{pmatrix} A & B \end{pmatrix} = \frac{1}{3}\begin{pmatrix} 0 & -1 \\ -8 & 0 \end{pmatrix} = \begin{pmatrix} 0 & -\frac{1}{8} \\ -8 & 0 \end{pmatrix}$$
The bandwadth is clearly infinite.

then
$$V_1 = \frac{8^2}{8}, V_2$$
 $i_1 = -\frac{8^2}{8}, V_2$
 $I_2 = \frac{5^2}{8}, V_3$
 $I_3 = \frac{5^2}{8}, V_4$

$$\begin{array}{c} (k_1) & (k_2) & (k_3) \\ (k_4) & (k_4) & (k_5) \\ (k_7) & (k_7) & (k_7) (k_7) & (k_7) & (k_7) & (k_7) \\ (k_7) & (k_7) & (k_7) & (k_7) & (k_7) \\ (k_7) & (k_7) & (k_7) & (k_7) & (k_7) & (k_7) \\ (k_7) & (k_7) & (k_7) & (k_7) & (k_7) & (k_7) \\ (k_7) & (k_7) & (k_7) & (k_7) & (k_7) & (k_7) & (k_7) \\ (k_7) & (k_7) & (k_7) & (k_7) & (k_7) & (k_7) & (k_7) \\ (k_7) & (k_7) \\ (k_7) & (k_7) \\ (k_7) & (k_7) \\ (k_7) & (k_7) &$$

$$(ABCD) = (0 - \frac{1}{8})(\frac{1}{9})(0 - \frac{1}{82}) = \frac{1}{8}$$

$$= \begin{pmatrix} -\frac{1}{3}, & -\frac{1}{3}, & \begin{pmatrix} 0 & -\frac{1}{32} \\ -\frac{1}{3}, & 0 \end{pmatrix} - \begin{pmatrix} \frac{3}{32} \\ -\frac{1}{32}, & \frac{3}{32} \end{pmatrix} = \begin{pmatrix} \frac{3}{32} \\ 0 & \frac{3}{32} \end{pmatrix}$$

if it is terminated in ZT then

$$-V_2 = -Z_7 i_2$$
 and $i_1 = -\frac{8}{3^2} i_3$

$$V_{1} = \frac{8^{2}}{8}, V_{2} = \frac{4}{8^{2}}, i_{2} = \frac{8^{2}}{8^{2}}, V_{7}, i_{2} = \frac{4}{8^{2}}, i_{3} = \frac{4}{8^{2}}, i_{4} = \frac{4}{8^{2}}, i_{5} = \frac{4}{8^{2$$

$$= + \frac{8^2}{8^2}i, \chi_{\tau} + \frac{1}{8^2} \forall i,$$

and the equivalent circuit is:

$$Z = \frac{1}{8^2} \times \frac{1}{8^2} \times \frac{8^2}{8^2} \times \frac{1}{8^2} \times \frac{1}{8^2}$$

$$(ABCD) = \begin{pmatrix} 0 & -\frac{1}{8} \\ -\frac{1}{8} & 0 \end{pmatrix} \begin{pmatrix} 1 & Z \\ 0 & 1 \end{pmatrix} \begin{pmatrix} D & -\frac{1}{8} \\ -\frac{1}{8} & 0 \end{pmatrix} =$$

$$= \begin{pmatrix} 0 & -\frac{1}{3}, & 0 & -\frac{1}{3} \\ -\frac{9}{3}, & -\frac{9}{3}, & 7 \end{pmatrix} \begin{pmatrix} 0 & -\frac{1}{3} \\ -\frac{9}{2} & 0 \end{pmatrix} = \begin{pmatrix} \frac{9}{3} & \frac{9}{3}, & 0 \\ \frac{9}{3} & \frac{7}{3} & \frac{9}{3} & \frac{9}{3} \end{pmatrix}.$$

then V, = 82/8, V2 , V2 = - Zrl2.

and $i_1 = 8_1 8_2 V_2 Z - \frac{8_1}{8_2} i_2 = \left(8_1 8_2 Z + \frac{8_1}{8_2} \frac{1}{Z_7}\right) \frac{8_1}{8_2} V_1$

$$= 8^{2} Z + \left(\frac{8^{2}}{8^{2}}\right) \frac{1}{Z_{r}}$$

$$\int_{\mathbb{R}^{2}}^{2} \left(\frac{3^{2}}{8!} \right) \sqrt{\frac{3^{2}}{8!}}$$

[4]

[3]

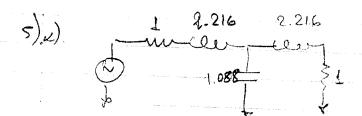
$$Z(LC) = j\omega L + \frac{1}{j\omega C} \Rightarrow 4 = 8^{\frac{7}{2}}j\omega L + \frac{8^{\frac{7}{2}}}{j\omega C}$$

is a parallel LC,
$$L' = \frac{C}{8^2}$$
, $C' = 8^2L$

the preallel LC maps to. Z'=1/32

$$\frac{1}{1+\frac{1}{2}} = \frac{1}{1+\frac{1}{2}} = \frac{1}{1+\frac{1$$

and the equivalent cercut is a series K with $L' = \frac{C}{8^2}$, $C' = 8^2 L$.



1/2.216 1/2.216. -11-11-

scale for Zong (regreency.

$$C_1 = \frac{G_1 - C_2}{50 \, \omega_0} = \frac{1}{27216} \frac{1}{50} \frac{1}{277108} = 14.3 \, pF$$

$$2_{12} = \frac{2.50}{1.088 \times 2\pi \times 108} = 289.5 \text{ pH}$$

to make it band reject, resonate these

=>
$$2'_{1} = \frac{1}{\omega_{0}^{2}C_{1}} - 293\overline{\rho}H = \lambda_{3}' + \frac{C_{1}'_{1}}{1+\omega_{1}}$$

$$C_2' = \frac{1}{\omega_0^2 \lambda_1'} = 14, 4 \text{ pF}$$

[s]

hub of
citor an
Her.
No. of the second secon
eff=l Zoc
Left = Zol
Lio I gyrafor
1 4
CioJ

Question 6.

 R_{iN} = $\{L_i\}$ $\{L_i\}$ $\{L_i\}$ $\{L_i\}$

Lunap de, Re unto son Reff = jwleke jwletke

then $Z_{eff} = j\omega L_2 - R_L j\omega R \qquad T = L_2$ $1 + j\omega L_2 \qquad 1 + j\omega R \qquad R_L$

Re Keff = $R_L \frac{\omega^2 \eta^2}{1 + \omega^2 \eta^2} = Reff$

Im Zeff = RL WT

this converts to a scriple impelance mutch

problem: (step down!)

Rin. C Z=-Ins Keff. Zeff

Zin = Re Keff

14 Qis specified,

$$Q^2 = \frac{R_{1N}}{Reft} - 1 \Rightarrow Q^2 Reff = R_{1N} - Reff \Rightarrow$$

But
$$ReH = R_1 \frac{\xi^2}{1+\xi^2}$$
 $(\xi = \omega \pi = \omega L_2)$
 $= (Q^2 + 1) \frac{\xi^2}{1+\xi^2} R_L = R_{1N} = (Q^2 + 1) \frac{\xi^2}{1+\xi^2} P = 1$

$$= \frac{\xi^{2}(Q^{2}+1)\rho-1}{R_{L}^{2}} = \frac{1}{(Q^{2}+1)\rho-1} = \xi^{2}$$

this defines L2.

The std impedance mutching with I note

Ques:

$$QReH = \omega \lambda$$
, $\Rightarrow QR_{\perp} \frac{\xi^2}{1+\xi^2} = \omega \lambda$

$$\Rightarrow \lambda' = Q R_{L} \frac{\xi^{2}}{\omega} \frac{1+\xi^{2}}{1+\xi^{2}}$$

Then $\omega \lambda_{1} = \omega \lambda_{1} - Im \text{ Leff} = \omega \lambda_{1} - R_{L} \frac{\xi}{1+\xi^{2}} = QR_{L} \frac{\xi^{2}}{1+\xi^{2}} - R_{L} \frac{\xi}{1+\xi^{2}} = R_{L} \frac{Q\xi(\xi-1)}{1+\xi^{2}}$

and
$$ev C = Q$$
 R_{in}

b) By the derivation of 12 we have: $\frac{\omega^{2} \lambda_{2}}{R^{2}} = \frac{1}{(Q^{2}+1)\rho - 1}$ The constraint on $p = \frac{R_{iN}}{R_{i}}$ is $(Q^2+1)Q \ge 1$ $p \ge \frac{1}{1+Q^2}$. No, surce 2, needs lo be en inductor if follows $\xi > 1 \Rightarrow \xi^2 > 1 \Rightarrow$ $\frac{1}{(Q^{2}+1)\rho-1} > 1 \Rightarrow 1 > (Q^{2}+1)\rho-1 \Rightarrow$ $(Q^2+1)\rho < 2$ $\Rightarrow \rho < \frac{2}{1+Q^2}$ $\frac{1}{1+Q^2}$ $\frac{2}{1+Q^2}$

c) By adding the negative of the inneg purt of the respective impelances.

T27