DEPARTMENT OF ELECTRICAL AND ELECTRONIC ENGINEERING EXAMINATIONS 2007 '

MSc and EEE/ISE PART IV: MEng and ACGI

### Corrected Copy

#### ADVANCED DATA COMMUNICATIONS

Monday, 23 April 10:00 am

Time allowed: 3:00 hours

There are FOUR questions on this paper.

Answer THREE questions.

All questions carry equal marks. The maximum mark for each subquestion is shown in brackets.

Any special instructions for invigilators and information for candidates are on page 1.

Examiners responsible

First Marker(s):

M.K. Gurcan

Second Marker(s): C. Ling

Instructions to the candidates:

Assume that the target argument of the Q function is 13.8 dB and 15 dB for average error rates of  $10^{-6}$  and  $1.8 \times 10^{-8}$  respectively when using M-ary pulse amplitude modulation (PAM) and quadrature amplitude modulation (QAM) systems.

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- 1. Answer the following subquestions.
  - (a) Prove that  $\phi_1\left(t\right) = \sqrt{\frac{2}{T}}\cos\left(2\pi\left(f_c + \frac{k}{T}\right)t\right) \quad \text{for } 0 \le t \le T \text{ and}$   $\phi_2\left(t\right) = \sqrt{\frac{2}{T}}\sin\left(2\pi\left(f_c + \frac{k}{T}\right)t\right) \quad \text{for } 0 \le t \le T$

are orthonormal basis functions for any integer  $k = 1, \dots, N$ .

(b) Consider the orthonormal basis functions

$$\begin{array}{ll} \phi_1\left(t\right) &=& \left\{ \begin{array}{ll} \sqrt{\frac{2}{T}} & & \text{for } 0 \leq t \leq \frac{T}{2} \\ 0 & & \text{otherwise} \end{array} \right., \text{ and} \\ \phi_2\left(t\right) &=& \left\{ \begin{array}{ll} \sqrt{\frac{2}{T}} & & \text{for } \frac{T}{2} \leq t \leq T \\ 0 & & \text{otherwise} \end{array} \right., \end{array}$$

and also the vectors

$$\begin{aligned} \mathbf{x}_1 &= \left(A\sqrt{\frac{T}{2}}, A\sqrt{\frac{T}{2}}\right) \\ \mathbf{x}_2 &= \left(A\sqrt{\frac{T}{2}}, -A\sqrt{\frac{T}{2}}\right). \end{aligned}$$

Plot the time waveforms  $x_1(t)$  and  $x_2(t)$  which are constructed using the above vectors and orthonormal basis functions. Calculate the signal energies  $\varepsilon_1$  and  $\varepsilon_2$  and also the Euclidean distance between  $x_1(t)$  and  $x_2(t)$ .

- (c) Consider an AWGN system with a SNR  $\frac{\bar{e}_x}{\sigma^2}$  of 22 dB, a target probability of error  $P_e=10^{-6}$ , and a symbol rate  $\frac{1}{T}=8$  KHz.
  - i. Find the maximum data rate  $R = \frac{b}{T}$  kHz that can be transmitted when using
    - A. Pulse Amplitude Modulation (PAM).
    - B. Quadrature Amplitude Modulation (QAM).
  - ii. What is the Nearest Neighbour Union Bound (NNUB) normalized probability of error  $\bar{P}_e$  for the systems used in part 1.c. above ?
- (d) A speech signal is sampled at a rate of 8 kHz, using 8 bits/sample. The Pulse Code Modulation (PCM) encoded data is transmitted through an AWGN baseband channel via an M-level PAM encoder. Determine the symbol data rate required for transmission when
  - i. M = 4,
  - ii. M=8, and
  - iii. M=16.

[5]

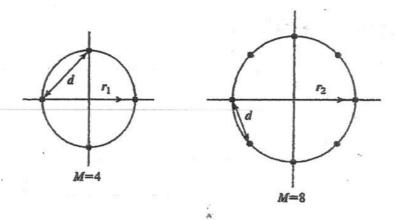
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[1]

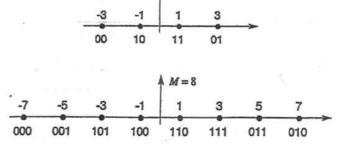
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[3]

- 2. Answer the following subquestions.
  - (a) Consider the four-level and eight-level phase modulation system constellations shown in the following figure



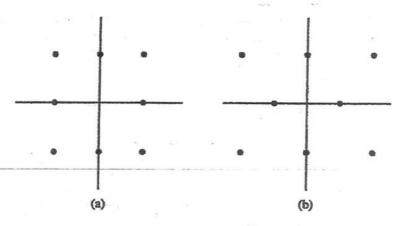
- i. Determine  $r_1$  and  $r_2$  if the minimum distance between two adjacent points in the two constellations is to be d.
- ii. From this result, determine the additional transmitted energy required when using the 8-PSK system if the same error probability is to be achieved when using a 4-PSK system. You may assume that only errors associated with adjacent points are significant.
- (b) Consider the four-level and eight-level PAM signal constellations shown in the following figure



[3]

[4]

(c) Consider the two 8-point QAM signal constellations shown in the following figure



The minimum distance between adjacent points is 2A. Determine the average transmitted energy for each constellation assuming that the signal points are equally probable. Which constellation is more power efficient?

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- 3. Answer the following subquestions.
  - (a) A voice-band telephone transmission is limited to the frequency range 300  $\!\!\!\leq f \leq$ 3000 Hz. Arrive at a symbol rate and the size of power efficient constellation to achieve a data rate of 9600 bits/sec explaining carefully the reasons for your choice. If a square-root raised cosine pulse,  $g_{T}\left(t\right)$ , is used for the transmitter pulse select the roll-off factor.
  - (b) In a binary PAM system, the input to the detector is

$$y_m = x_m + n_m + i_m$$

where  $x_m \in \{\pm 1\}$  is the desired signal,  $n_m$  is a zero-mean Gaussian random variable of variance  $\sigma_n^2$  and  $i_m$  represents the Inter-Symbol-Interference (ISI) due to channel distortion. The ISI term is a random variable which takes the values  $\frac{1}{2}$ , 0,- $\frac{1}{2}$  with probabilities  $\frac{1}{4}$ ,  $\frac{1}{2}$ ,  $\frac{1}{4}$  respectively. Determine the average probability of error as a function of  $\sigma_n^2$ .

(c) Consider a communication channel with the pulse energy, p, and sampled autocorrelation function Q(D) given as follows

$$\begin{split} |p|^2 &= 1 + aa^* & 0 \le |a| < 1 \\ Q(D) &= \frac{a^*D^{-1} + |p|^2 + aD}{|p|^2}. \end{split}$$

- i. Assume that the matched filter bound is  $SNR_{MFB}$ . Find the coefficients for the zero forcing equaliser,  $W_{ZFE}\left(D\right)$ , and minimum mean square error linear equalizer,  $W_{MMSE-LE}(D)$ . Use the variable  $b = |p|^2 \left(1 + \frac{1}{SNR_{MER}}\right)$  in your expression for  $W_{MMSE-LE}(D)$ .
- ii. Find the roots  $r_1$ ,  $r_2$  of the polynomial

$$aD^2 + bD + a^*.$$

Show that  $(b^2 - 4aa^*)$  is always a positive real number provided  $|a| \neq 1$ . Let  $r_2$  be the root for which  $|r_2| \leq |r_1|$ . Show that  $r_1r_2^* = 1$ .

iii. Use the previous results to show that for the MMSE-LE

$$W_{MMSE-LE.}(D) = \frac{|p|}{a\left(r_1-r_2\right)} \left(\frac{r_1}{D-r_1} - \frac{r_2}{D-r_2}\right).$$

iv. For the channel considered in part c.i above, show that the canonical factorization is

$$Q(D) + \frac{1}{SNR_{MFB}} = \gamma_0 (1 - r_2 D^{-1}) (1 - r_2^* D).$$

What is  $\gamma_0$  in terms of a and b?

[2] v. Find the feedback B(D) and feedforward W(D) filter coefficients for the MMSE [2] DFE.

[2]

[2]

[3]

[3]

[2]

[2]

[2]

- 4. Answer the following subquestions.
  - (a) The data rate, R = b/T, of a multi-tone system with a set of 8 sub channels is to be maximized. In the system, 1/T is the symbol rate, and the term b

$$b = \frac{1}{2} \sum_{n=1}^{8} b_n = \frac{1}{2} \sum_{n=1}^{8} \log_2 (1 + \varepsilon_n g_n)$$

is the largest number of bits that can be transmitted over the parallel set of 8 channels. In the equation for b, the term  $g_n = |H_n|^2/\sigma_n^2$  represents the subchannel signal-to-noise ratio when the transmitter applies unit energy to that subchannel. The terms  $\varepsilon_n$ ,  $|H_n^2|$  and  $\sigma_n^2$  correspond to the energy, the channel gain and noise variance in the  $n^{th}$  subchannel respectively. Using Lagrange multiplier method show that the following set of linear equations

 $\begin{bmatrix} 1 & 0 & 0 & \cdots & -1 \\ 0 & 1 & 0 & \cdots & \vdots \\ \vdots & \vdots & \vdots & \ddots & -1 \\ 1 & 1 & \cdots & 1 & 0 \end{bmatrix} \begin{bmatrix} \varepsilon_1 \\ \varepsilon_2 \\ \vdots \\ \varepsilon_8 \\ K \end{bmatrix} = \begin{bmatrix} -1/g_1 \\ -1/g_2 \\ \vdots \\ -1/g_8 \\ 8\overline{\varepsilon}_x \end{bmatrix}$ 

provide solutions for energy distributions in each subchannel, where K is a constant and  $8\bar{\varepsilon}_x = \sum_{n=1}^8 \varepsilon_n$ .

- (b) While the SNR gap may be fixed for often-used constellations in multi-tone modulation systems, this gap is a function of two other parameters.
  - i. What are these two parameters?

[1] [1]

[2]

[6]

- ii. Based on your answer to part b.i above, how can the gap be reduced?
- iii. A 16 (b = 4,) QAM channel having SNR = 25dB is to have an average error probability,  $\bar{P}_e = 10^{-6}$ . What is the margin for this transmission system?
- (c) An N=8 dimensional multi-tone modulation signal is transmitted over a channel with the gain

$$H\left(f\right) = 1 + 0.5e^{j2\pi f}.$$

The signal SNR is  $\bar{\varepsilon}_x |h|^2 / \sigma^2 = 10$  dB and the average energy  $\bar{\varepsilon}_x = 1$ . Assuming that target argument of Q-function is 9 dB, calculate the average number of bits  $\bar{b}$  per dimension if the total energy is distributed equally among each dimension.

[5]

[2]

- (d) For the channel in problem (4.c),
  - i. calculate the multi-channel signal-to-noise-ratio,  $SNR_{m,u}$ , for a set of parallel channels using the exact formula and the geometric mean  $SNR_{geo}$  for a gap value of  $\Gamma=8.8 \text{dB}$ .
  - ii. Compare the difference between he  $SNR_{MFB}$  and the exact  $SNR_{m,u}$  for the channels with the transfer functions  $1 + 0.5D^{-1}$  and  $1 + 0.9D^{-1}$ .

Examinations: A&C Session 2006-2007 Confidential MODEL ANSWER and MARKING SCHEME

First Examiner M.K. GULCAN

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Second Examiner T. STATHAKI

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CONSIDER  $\int_{0}^{\infty} |\xi| dt = \int_{0}^{\infty} |\xi|^{2} \cos^{2}(2\pi(f_{c} + \frac{1}{2})t) dt$   $= \int_{0}^{\infty} |\xi|^{2} \cos(4\pi(f_{c} + \frac{1}{2})t) + \cos(0) dt$   $= \int_{0}^{\infty} |\xi|^{2} \cos(4\pi(f_{c} + \frac{1}{2})t) + \cos(0) dt$   $= \int_{0}^{\infty} |\xi|^{2} \cos(4\pi(f_{c} + \frac{1}{2})t) + \int_{0}^{\infty} dt$ 

ALSO CONSIDER

$$\int_{0}^{T} g_{2}^{2}(t) dt = \int_{0}^{T} \frac{1}{T} \sin^{2}(2\pi)(f_{c} + \frac{1}{T}) dt$$

$$= \int_{0}^{T} \frac{1}{T} \cos(0) dt - \int_{0}^{T} \frac{1}{T} \cos(4\pi)(f_{c} + \frac{1}{T}) dt$$

$$= \frac{1}{T} \int_{0}^{T} -0 = 1$$

CONSIDER

$$\int_{0}^{T} |x| (t) |x| (t) dt = \int_{0}^{2} \frac{1}{T} \cos(2\pi (f_{c} + \frac{1}{T})t) \sin(2\pi (f_{c} + \frac{1}{T})t) dt$$

$$= \int_{0}^{T} \frac{1}{T} \sin(4\pi (f_{c} + \frac{1}{T})t) dt - \int_{0}^{T} \frac{1}{T} \sin \theta dt$$

The wave forms of (t) and of(t) are orthogonal.

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MODEL ANSWER and MARKING SCHEME

M.K. GULCAN First Examiner

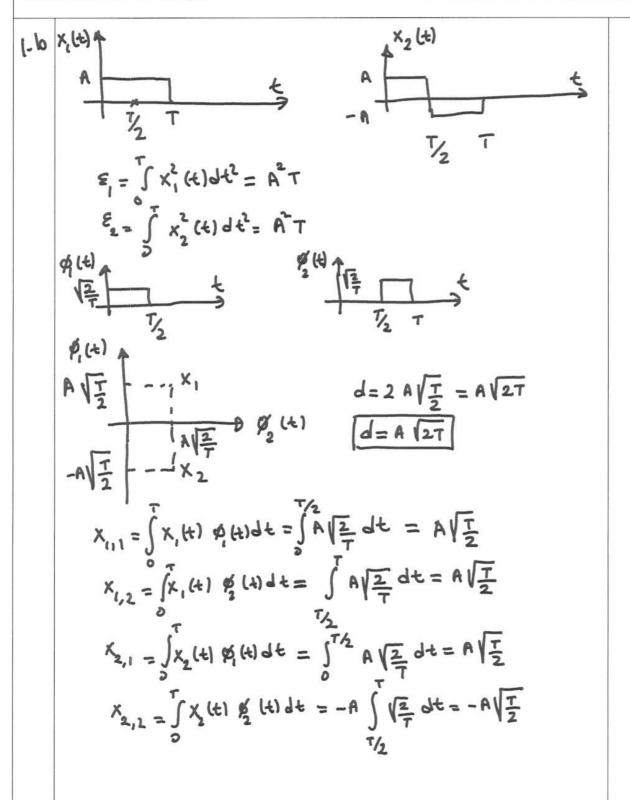
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Second Examiner T. STATHAKI

1.6 Page 2 out of Question

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# Examinations: A&C Session 2006-2017 Confidential MODEL ANSWER and MARKING SCHEME

First Examiner M.K. GULCAN

Paper Code 4.04

Second Examiner T. STATHAKI

Question 1. (Page 3 out of 17

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12

THE PE FORMULA FOR PAM, AND QAM IS
IDENTICAL

-6

 $\bar{P}_{e} \leq 2.Q \left(\sqrt{\frac{3 \text{ SNR}}{2^{2\bar{b}}-1}}\right) < 10^{-6}$ 

 $\frac{3.5NR}{2^{2\overline{b}}-1} = 13.8 dR$   $2^{2\overline{b}}-1 = 4.77 + 22 - 13.8 = 12.97 dS$   $\overline{b} = 2.19$ 

BATA RATE CORRESPONDS TO \$=2 IN ALE CASES. THUS

PAM  $R = \frac{6.N}{T} = 2 \times 1 \times 8 k = 16 \text{ kbps}$ 

QAM R=2 x2 x8 k= 32 Kbps.

IN BOTH CASES

3. SNR = 4.77+22-11.76 = 15.01 d3

Pe < 2 Q(15.0138) = 1.8 x 10

Examinations: A&C Session 2006-2007 Confidential MODEL ANSWER and MARKING SCHEME First Examiner M.K. GULCAN Paper Code 4.04 Question 1.d Page 4 out of [7 Second Examiner T. STATHAKI Marks allocations in right margin **Question labels in left margin** BANDWIDTH REQUIRED FOR TRANSMISSION 1.7 M-ARY PAM SILNAL IS W= Rb HZ SMCE R = 8 × 10 SAMPLES X 8 bits
SAMPLE = 64×10 bits/sec WE OBTAIN M= { 10.66 \$45 W= 8

## Examinations: A&C Session 2006-2007 Confidential MODEL ANSWER and MARKING SCHEME

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Question 2. aPage 5 out of 17

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Marks allocations in right margin

2.9 USING THE PHYTHAGOREAN THEOREM FOR THE FOUR PHASE CONSTELLATION, WE FIND

$$L_1^+ L_2^- = q_2 \Rightarrow L^- = \frac{A}{\Lambda^2}$$

THE RADIUS OF THE 8-PSK CONSTELLATION IS FOUND USING THE COSINE RULE, THUS

$$d^2 = r_2^2 + r_3^2 - 2r_2^2 \cos(45) \Rightarrow r_2 = \frac{d}{\sqrt{2-\sqrt{2}}}$$

THE AVERAGE TRANSMITTED POWER OF THE 4-PSK AND THE 8-PSK CONSTELLATION IS GIVEN BY

$$P_{4,AV} = \frac{d^2}{2}$$
,  $P_{8,AV} = \frac{d^2}{2-\sqrt{2}}$ 

THUS THE ADDITIONAL TRANSMITTED POWER NEEDED BY THE 8-PSK SIGNAL IS

$$P = 10 \log_{10} \frac{2d^2}{(2-\sqrt{2})d^2} = 5.3329 dB$$

WE OBTAIN THE SAME RESULTS IF WE USE THE PROBABILITY OF ELROR GIVEN BY

WHERE OS IS THE SUR PER SYMBOL. IN
THIS CASE EQUAL ERROR PROBABILITY FOR THE
TWO SIGNALLING SCHEMES IMPLIES THAT.

= 20 log10 sin 1/4 = 5.329 dB.

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2.C

THE CONSTELLATION OF FIGURE 3.0 HAS FOUR
POINTS AT A DISTANCE 2A FROM THE BRIGIN AND
FOUR POINTS AT A DISTANCE 2 12A. THUS, THE
AVERAGE TRANSMITTED POWER OF THE CONSTELLATION
IS

THE SECOND CONSTELLATION HAS FOUR POINTS

AT A DISTANCE (7 A FROM THE ORIGIN, TWO
POINTS AT A DISTANCE (3 A AND TWO POINTS AT
A DISTANCE A. THUS THE AVERACE TRANSMITTED

POWER OF THE SECOND CONSTELLATION IS

SINCE POSE THE SECOND CONSTECLATION IS
MORE POWER EFFILIENT.

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Question 3.4 Page 8 out of 17

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3.9 THE BANDWIDTH OF THE CHANNEL IS

W= 3000-300=2700 HZ

SINCE THE MINIMUM TRANSMISSION BANDWIDTH

REQUIRED FOR BANDPASS SIGNALLING IS 2,

WHERE 2 IS THE RATE OF TRANSMISSION,

WE CONCLUDE THAT THE MAXIMUM VALUE

OF THE SYMBOL RATE FOR THE GIVEN CHANNEL

IS RMAX = 2700. IF AN M-ARY PAM

MODULATION IS USED FOR TRANSMISSION, THEN

IN ORDER TO ACKIEVE A BIT RATE OF 9600 by

WITH MAXIMUM RATE OF RMAX!

OF THE CONSTELLATION IS M= 2k=16. IN THIS

CASE THE SYMBOL RATE IS

R= 9600 - 2400 SYMBOLS/SEC

PND THE SYMBOL INTERVAL T= 1 = 1 = 2400 SEC.

THE ROLL OF FACTOR & OF THE RAISED LOSING PULSE USED FOR TRANSMISSION IS DETERMINED BY NOTHING THAT 1200(1+K)=1350, AND HENCE, &= 0.125. TREREPORE, THE SQUARED ROOT RAISED LOSINE DUCSE CAN HAVE A ROLL-OFF &= 0.125.

Examinations: ADC Session 2006-200 Confidential MODEL ANSWER and MARKING SCHEME Paper Code 4.04 M.K. GULCAN First Examiner T. STATHAKI Question 3. 6 Page 9 Second Examiner Marks allocations in right margin Question labels in left margin HAUE

9 = { a+n-1/2 with PROB. 1/4

a+n+1/2 with PROB. 1/4

WITH PROB. 1/2 3.6 SYMMETRY B7 Pe = P(e|a=1) = P(e|a=-1), NENCE Pe=P(e|a=-1)=== P(n-1>0)++P(n-3>0) + 47(1-12>0)  $= \frac{1}{2} Q(\frac{1}{\sigma_{h}}) + \frac{1}{4} Q(\frac{3}{2\sigma_{h}}) + \frac{1}{4} Q(\frac{1}{2\sigma_{h}})$ 

# Examinations: AD C Session 2006-2007 Confidential MODEL ANSWER and MARKING SCHEME

First Examiner M.K. GULCAN

Paper Code 4.04

Second Examiner T. STATHAKI

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Marks allocations in right margin

3. 
$$\frac{2^{\frac{1}{2}}}{\sqrt{2^{\frac{1}{2}}}} = \frac{1}{|P|} \frac{1}{|Q(3)|} = \frac{|P|}{\alpha^{\frac{1}{2}} + |P|} + \alpha b = \frac{\sqrt{1 + \alpha \alpha^{\frac{1}{2}}}}{\sqrt{\frac{1}{2}} + (1 + \alpha \alpha^{\frac{1}{2}}) + \alpha b}$$

$$= \frac{|P|}{\alpha^{\frac{1}{2}} - |P|} \frac{1}{(1 + \frac{1}{2})} + \alpha b$$

$$= \frac{|P|}{\alpha^{\frac{1}{2}} - |P|} \frac{1}{(1 + \frac{1}{2})} + \alpha b$$

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### Examinations: A&C Session 2006-2007 Confidential MODEL ANSWER and MARKING SCHEME 4.04 M.K. GULCAN Paper Code First Examiner Question 3. C Page 11 out of 17 T. STATHAKI Second Examiner Marks allocations in right margin **Question labels in left margin** FINALLY 1, 15 COMPUTED 1, 13 = 1 (-b-\b2-4aa\*) (-b+ \b2-4aa\*) = 1 (b2-(12-4aa\*)2)=1 المان FOR MMSE-LE MWZE-CE = (P/ D) = (P/ D) (P-C) BY EXPANDING W INTO PARTIAL FRACTION Wmms=-ce (D): [P] [A + B ] WE FIND THAT $A = \frac{\Gamma_1}{\Gamma_1 - \Gamma_2} \quad AND \quad B = \frac{\Gamma_2}{\Gamma_2 - \Gamma_1}$ $m^{\text{WW}} \text{2E} - \text{FE}(D) = \frac{a(L - L^2)}{|D|} \left[ \frac{P - L^2}{L^2} - \frac{P - L^2}{L^2} \right]$

#### Examinations: Abc Session 2006-2007 Confidential MODEL ANSWER and MARKING SCHEME

First Examiner

M.K. GULCAN

Paper Code 4.04

Second Examiner T. STATHAKI

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I.

$$Q(D) + \frac{1}{SNR_{MES}} = \frac{\alpha}{|P|^2} (D-\Gamma_1) (1-D^{\top} T_2)$$

where 
$$C_{1}C_{2}^{*}=1$$
, Hence

$$\delta_{0} = -\frac{\alpha \Gamma_{1}}{(P)^{2}} = \frac{b + \sqrt{b^{2} - 4\alpha \alpha^{2}}}{2(1 + \alpha \alpha^{2})}$$

$$B(D) = 1 - D \int_{2}^{*} = 1 - \frac{-b + \sqrt{b^{2} - 4 \alpha \alpha^{*}}}{2 \alpha^{*}} D$$

### Examinations: ASC Session 2006-2007 Confidential MODEL ANSWER and MARKING SCHEME

M.K. GULCAN First Examiner

4.04 Paper Code

Second Examiner T. STATHAKI Question 4-a Page 13 out of 17

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Marks allocations in right margin

WE NEED TO MAXIMISE b= Zb, OVER by AM En.

USING LA GRANGE MULTIPLIERS, THE LOCT FUNCTION TO MATIMIZE

SUBJECT TO THE CONSTRAINT IN

DIFFERENTIATING WAT EN PRODUCES

$$\frac{1}{2\ln(2)} = -\frac{\lambda T}{g_{1}}$$

MAXIMIZED WHEN

	Examinations: A a MODEL ANSWER and			200 /	Confidenti			
First I	Examiner M.K. GJLCAN		ode 4.0	4				
	d Examiner T. STATHAKI	Question 4. Q Page 14 out of 17						
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٠.٩	WHEN [1=1 (0 1 B)	THE M	HYIMUM	BATA	RATE			
	E, + 17 = K							
	E, + P = K Ez + P = K							
	i i							
	ZN+ gg = K							
	Ent g = K Ent Ezt + EN = N	Σ×						
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	Examinations: AS Session 2006-2007 Confidential MODEL ANSWER and MARKING SCHEME
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	nd Examiner T. STATHAKI Question 4.6 Page 15 out of 17
	tion labels in left margin  Marks allocations in right margin
4.6	i) THE GAP BEPENDS ON PE AND THE CODING EMPLOYED.
	i)). IMPROJE CODING SCHEME WHEN PE is fixed or accept a HIGHER Pe.
	ELL') ASSUMING QAM TRANSMISSION WE OBTAIN. TARGET ARCHMENT OF Q FUNCTION IS 13.8 dB for Pe = 10 <sup>-6</sup> .
	THE GAP VALUE 1 = 101.38 = 7.99 =) 1 = 8.82
	$rac{1}{2^{b}-1} = 25-8.8-11.718=4.518$
42	H(D)= 1+0.5D=) h=[1 0.5]
	$ h ^2 = \frac{2}{5}h_i^2 = (1)^2 + (0.5)^2 = 1.25$ $\sum_{x=1}^{2} \frac{1}{5}$
	SNL MEB = 10 dB SNR MEB = $10 = \frac{2}{5} \times 10^{2}$
	$0^{\frac{1}{2}} = \frac{1 \times 1.25}{10} = 0.125$
	$SNR^{U} = \frac{Q_{S}}{E^{U} + V_{I}}$

## ADC Session 2006-2007 Confidential **Examinations:** MODEL ANSWER and MARKING SCHEME Paper Code 4.04 M.K. GULCAN First Examiner Question 4. C Page 16 out of 17 Second Examiner T. STATHAKI Marks allocations in right margin Question labels in left margin FOR N= 8 n = 0 = 1 = 2 = 3 $\epsilon_n = 8/7 = 16/7 = 16/7 = 16/7$ | that 1.5 1.4 1.118 0.737 SNR, 20.6 17.9 11.43 4.97 b 1.566 1.479 1.205 0.761 WHERE Ton= 1 68 (1+ 5NRn) = 1 (052 (1+SNRn x3/Aro) Arg = 100.5 = 7.94 b= 1x1.566 + 2x1.479 + 2x1.205+2x0.761 b= 1.057.

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MODEL ANSWER and MARKING SCHEME

First Examiner M.K. GULCAN

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Marks allocations in right margin

4.2

SNR IS CLOSER TO SNR for 1+0.5D SEO SEO THAT IS RECAUSE IT SHOWS A FLATTER PESPONSE AND THE ROLL-Off IS NOT SEVERE. THIS IMPLIES THAT THE WORST SNR /TI IS BETTER FOR 1+0.5D CHANNEL, WHICH RESULTS IN A BETTER APPROXIMATION.