Paper Number(s): E3.13

IMPERIAL COLLEGE OF SCIENCE, TECHNOLOGY AND MEDICINE UNIVERSITY OF LONDON

DEPARTMENT OF ELECTRICAL AND ELECTRONIC ENGINEERING **EXAMINATIONS 2002** 

EEE PART III/IV: B.Eng., M.Eng. and ACGI

## **ELECTRICAL ENERGY SYSTEMS**

Thursday, 25 April 10:00 am

There are SIX questions on this paper.

Answer FOUR questions.

**Corrected Copy** 

Time allowed: 3:00 hours.

Examiners responsible:

First Marker(s):

Pal,B. and Popovic,D.

Second Marker(s): Popovic, D. and Pal, B.

Special instructions for invigilators:	None
Information for candidates:	None

- 1. (a) Describe briefly the influence of voltage magnitude, voltage angle and reactive power transfer on real power transfer between two active sources connected by an inductive reactance.
  - (b) For the system shown in Figure 1, all quantities are per-phase per-unit values. Calculate the reactive power injected by a capacitor at bus 2 so that  $|V_2| = 1$ pu. In this case, what is the phase angle of the voltage at bus 2? [12]

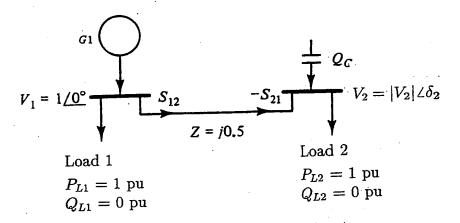


Figure 1.1

- 2. A 300km, 500kV three-phase transmission line has a series reactance  $x=0.34\Omega/\mathrm{km}$  and a shunt admittance  $y=j4.5\cdot 10^{-6}\mathrm{S/km}$ . Line losses are neglected.
  - (a) Calculate surge impedance  $Z_c$ , propagation constant  $\gamma l$ , the ABCD parameters, the wavelength  $\lambda$  of the line, and the surge impedance loading in MW.
    - [8] Ilate the
  - (b) Rated line voltage is applied to the sending end of the line. Calculate the receiving-end voltage when the receiving end is terminated by
    - (i) an open circuit [3]
    - (ii) the surge impedance of the line
      (iii) one-half of the surge impedance.
      [3]
  - (c) Calculate the theoretical maximum real power that the line can deliver when rated voltage is applied to both ends of the line.

[3]

3. For the power system shown in Figure 2, the per-unit admittance matrix  $Y_{BUS}$  is given by

$$Y_{BUS} = \left[ \begin{array}{ccc} 3 - j9 & -2 + j6 & -1 + j3 \\ -2 + j6 & 2.5 - j7.5 & -0.5 + j1.5 \\ -1 + j3 & -0.5 + j1.5 & 1.5 - j4.5 \end{array} \right].$$

The per-unit bus voltages and injections are also given in the Figure.

- (a) For each bus k, specify the bus type, and determine which of the variables  $V_k$ ,  $\delta_k$ ,  $P_k$  and  $Q_k$  are input data and which are unknowns.
- (b) Assume an initial estimate of  $V_2 = 1\angle 0^o$  and  $\delta_3 = 0^o$ , and calculate the bus real and reactive power mismatches to be used in the first iteration of the Newton-Raphson power flow method.
- (c) Set up the linearized system of equations  $J \triangle x = \triangle y$  that are solved at each iteration of the Newton-Raphson power flow method. Do not solve the equations. [5]

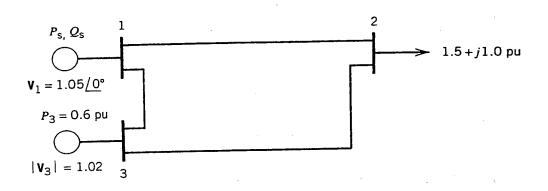


Figure 3.1

(a) Why is it so important to optimally allocate power generations to various units in a power system?

[5]

(b) Three units with the following specifications are listed:

Unit 1: Coal fired:

Max output = 1200 MW

Min output = 350 MW

Input-output curve:

$$H_1 = 510 + 7.2P_1 + 0.00142P_1^2$$
 (Mbtu/h)

Unit 2: Oil fired:

Max output = 1000 MW

Min output = 300 MW

Input-output curve:

$$H_2 = 310 + 7.85P_2 + 0.00142P_2^2$$
 (Mbtu/h)

Unit 3: Oil fired:

Max output = 800 MW

Min output = 200 MW

Input-output curve:

$$H_3 = 178 + 7.97P_3 + 0.00482P_3^2$$
 (Mbtu/h)

Fuel costs for the three units are 1.2 R/Mbtu, 1.0 R/Mbtu and 1.1 R/Mbtu respectively. 'R' is any fictitious currency symbol.

Determine the economic operating point for these three units when delivering a total of 2000 MW.

 $\lceil 15 \rceil$ 

5. (a) What are the various methods of voltage control?

[6]

(b) Generator A of rating 200 MW and generator B of rating 350 MW have governor droops of 5 per cent and 8 per cent, respectively, from no load to full load. They are the only supply to an isolated system whose nominal frequency is 50 Hz. The corresponding generator speed is 3000 rpm. Initially, generator A is at 0.5 p.u load and generator B is at 0.65 p.u. load, both running at 50 Hz. Find the no-load speed of each generator if it is disconnected from the system. Also determine the output of B when A reaches its rating.

[14]

- 6. (a)  $V_a$ ,  $V_b$  and  $V_c$  are phase voltages and  $V_0$ ,  $V_1$  and  $V_2$  are sequence components in a three phase system. If  $S_{ph}$  and  $S_s$  are powers in phase and symmetrical components respectively, show that  $S_{ph} = 3S_s$ .
  - (b) Equipment ratings for the five-bus power system shown in Figure 3 are as follows: Generator G1: 50 MVA, 12 kV, X'' = 0.2 per unit Generator G2: 100 MVA, 15 kV, X'' = 0.2 per unit Transformer T1: 50 MVA, 12 kV Y/138 kV Y, X = 0.1 per unit Transformer T2: 100 MVA, 15 kV Y/138 kV Y, X = 0.1 per unit Each 138-kV line:  $X_l = 40\Omega$ .

A three-phase short circuit occurs at bus 5, where the pre-fault voltage is 15kV. Pre-fault load current is neglected.

- (i) Draw the positive-sequence reactance diagram in per-unit on a 100-MVA, 15kV base.
- (ii) Determine the Thévenin equivalent at the fault. [4]
- (iii) Determine the subtransient fault current in per-unit and in kA. [2]

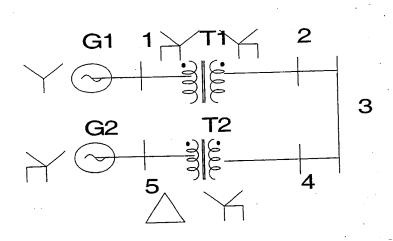


Figure 6.1

So

2

3

3

2

3

20

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Model Answers and Mark Schemes

First Examiner:

D. POPOVIC (Ques 1, 2, 3) B. PAL (Ques 4, 5, 6)

Paper Code: E3, 13

Second Examiner: B. PAL

D. POPOVIĆ

Question Number etc. in left margin

Mark allocation in right margin

a) Z= 174.9 A Xl = V+2 l = 10,3711 m 8l=1(pl), pl=0.3711 A = D = cos (pl) = 0.9319 10° pu

B=12cnn(51) = 1274.9 rin (0.3711) = 199.691

 $C = j \frac{1}{4c} nin (pl) = j 1.319.10^{-3} N$ 

 $\lambda = \frac{2\pi}{15} = 5079 \text{ km}$ 

 $51L = \frac{V_{\text{taked}}^2}{2} = \frac{500^2}{2749} = 909.4 \, \text{HW} (3\phi)$ 

6) (i)  $V_R = \frac{V_S}{A} = \frac{500}{0.9319} = 536.5 \text{ kV}$ 

(ii) Ve = Vs = 500 KV

(iii) V<sub>2</sub> = cos(sl) V<sub>2</sub> + j = cos(sl) \frac{1}{1} \frac{1}{2} \f = [cos(pl) + 12 nin(pl)] VR

=> VR = 500 cos 0,3711 + 12 min 0,3711 = 423.4 KV

c) Theoretical maximum real power;

 $P_{\text{max}} = \frac{V_{\text{S}} V_{\text{R}}}{\chi'} = \frac{500.500}{99.69} = 2508 \text{ MW}$ 

5

2

2

1

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Model Answers and Mark Schemes

First Examiner: D. PO POVIC (Ques 1, 2, 3)

B. PAL (Ques 4, 5, 6)

E3.13 Paper Code:

3

Second Examiner: B. PAL D. POPOVIĆ

Question Number etc. in left margin

Mark allocation in right margin

input data bus time a) UNLHOWN Vi, Ji Pr. Q1 Swing V2. 02 P2, Q2 load 2 generator B. Vs 5, Q3

Power flow quations Pr = Vx EN Vn (Gracos (Je-Jn) + Bru min (Je-Jn)) QK = VK & Vn (GKn min (JK-Jn) - BKN COS (JK-Jn))  $\delta kn = \delta k - \delta n$ Ay = 4 - f(x)

$$J = \begin{bmatrix} P_2 \\ P_3 \\ Q_2 \end{bmatrix} = \begin{bmatrix} P_{G2} - P_{L2} \\ P_{G3} - P_{L3} \\ Q_{62} - Q_{L2} \end{bmatrix} = \begin{bmatrix} -1.5 \\ 0.6 \\ -1 \end{bmatrix} \mu \mu$$

P2(0) = V2 [V, (G21 C00 TE1 + B21 WIN TE1) + V2 G22 + V3 (623 C00 TE3 + B25 WINTER) K=2: =-0.11 py

k=3: P3(0) = V3 [V1 (G31 COO J31 + B31 rule J31) + V2 (632 coo J32 + B32 rule J32) + + V3 635 = - 0.02 pe

Q2(0) = V2[V1 (621 un d21 - B21 cos d21) - V2 B22 + V3 (623 un d23 - B23 costes)]  $= -0.35 \mu u$ 

 $\Delta P_2 = P_2 - P_2(0) = -1.5 + 0.11 = -1.39 \mu$ AP3 = B- B(0) = 0.6- (-0.02) = 0.62 pu AQ2=Q2-Q2(0)=-1-(-0,33)=-0.67 pu

Department of Electrical and Electronic Engineering Examinations 2002 Confidential D. POPOVIC (Ques 1, 2, 3) B. PAL (Ques 4, 5, 6) B. PAL (Ques 1, 2, 3) Model Answers and Mark Schemes First Examiner: Paper Code: E3.13 Second Examiner: D. POPOVIC (Ques 4, 5, 6) Question Number etc. in left margin Mark allocation in right margin (cont) 3 c) J. DX = AZ l  $\Delta X = \begin{bmatrix} \Delta \sqrt{2} \\ \Delta \sqrt{5} \\ \Delta V_2 \end{bmatrix}, \qquad \Delta Z = \begin{bmatrix} \Delta \tilde{P}_2 \\ \Delta \tilde{P}_3 \\ \Delta Q_2 \end{bmatrix} = \begin{bmatrix} -1, 39 \\ 0.62 \\ -0.67 \end{bmatrix}$ 20

## MODEL ANSWERS

## 3:13: Electrical Energy Systems Dr. Bikash Pal

Q4 (a)

In thermal power plants, fuels (oil, gas and coal) used are very costly. The price fluctuates with international market conditions couple with demand and supply. The amount of fuel used in generating power in the range of GW is astronomical. A slight variation in price causes billions of dollars of hike in fuel bills to the power companies. The cost of electric energy production rises accordingly. This has the knock on effect on the cost of finished products from industries where electricity is one of the key inputs. This suggests that various units in a system must share their outputs in an efficient manner. This is why it is so important to have optimum allocations of generation. [5 marks]

(b) Convert input-output curve into cost curve multiplying through fuel cost.

This would give rise to:

$$C_1 = 5C_1 = 510 + 8.64 P_1 + 0.001704 P_1^2$$
  
 $C_2 = 310 + 7.85 P_2 + 0.00142 P_2^2$  [2 marks]  
 $C_3 = 178 + 7.97 P_3 + 0.00482 P_3^2$ 

The incremental costs (R/MW) is

$$\frac{dC_1}{dP_1} = 8.64 + 0.003408 \quad P_1 = \lambda$$

$$\frac{dC_2}{dP_2} = 7.85 + 0.00284 \quad P_2 = \lambda$$

$$\frac{dC_3}{dP_3} = 7.97 + 0.00964 \quad P_3 = \lambda$$

$$P_1 + P_2 + P_3 = 2000$$
[3 marks]

Solve for 
$$P_1, P_2, P_3, \lambda$$

Ans: 
$$P_1 = 647 \cdot 1$$
,  $P_2 = 1054$  ,  $P_3 = 298$  ,  $(MW) \lambda = 10 \cdot 8$  [5]

Note Unit #2 exceeds maximum limit, hence  $P_2 = 1000MW$  ;

Unit #1 and 3 have to provide 1000 MW in optimal fashion

Following can be used to solve for  $P_1, P_3, \lambda$ 

$$\frac{dC_{-1}}{dP_{-1}} = 8.64 + 0.003408 \qquad P_{1} = \lambda$$

$$\frac{dC_{-3}}{dP_{-3}} = 7.97 + 0.00964 \qquad P_{3} = \lambda$$

$$P_{1} + P_{3} = 2000$$

ans; 
$$P_1 = 687.46 \text{ MW}$$
,  $P_3 = 312.53 \text{ MW}$ ;  $\lambda = 10.98$  [5 marks]

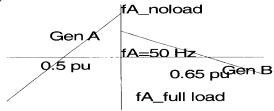
Q5 (a) The students are expected to write a couple of sentences on the following:

Injection of reactive power (shunt capacitors/reactors, series capacitors, synchronous compensators), tap changing transformers, booster transformer, phase shifting transformer,

Flexible AC transmission system (FACT) devices such as Static Var compensator (SVC), Static compensator (STATCOM), Unified power flow controllers (UPFC) etc. [6 marks]

(b) Generator A and B respectively loaded to 0.5 p.u. and 0.65 p.u of full load. This corresponds to 50 Hz or 3000 rpm.

A typical representative (not complete or to scale) droop characteritic can be drawn to help solve the problem.



Say at this droop setting and power output of Gen A, the no load frequency is  $f_A^{'}$  and full load frequency is  $f_A^{''}$  and at 0.5 p.u it is as stated in the problem  $f_A$  (1.p.u or 50 Hz). For Gen B the no load frequency is  $f_B^{''}$  and full load frequency is  $f_B^{''}$  and at 0.5 p.u it is as stated in the problem  $f_B$  (1.p.u or 50 Hz). With the help of droop relationship, the following expression can be written:

$$\frac{100}{200} = \frac{f_{A}^{'} - f_{A}}{f_{A}^{'} - f_{A}^{''}} = \frac{f_{A}^{'} - f_{A}}{0.05}$$

$$f_{A}^{'} = 1.025 f_{A} \rightarrow 3075 rpm$$
[7 marks]

Similarly for Gen B

$$\frac{227.5}{350} = \frac{f_B^{'} - f_B}{f_B^{'} - f_B^{''}} = \frac{f_B^{'} - f_B}{0.08}$$
[3 marks]
$$f_B^{'} = 1.052 f_B \rightarrow 3156 rpm$$

 $f_A^{''}$  corresponding to 200 MW loading on Gen A can be found from the above expression to be  $0.975\,f_A$ . This has to be the frequency of Gen B as well. Corresponding to this frequency, the output of Gen B can be found from the solution of  $P_B$ 

$$\frac{227.5}{P_B} = \frac{1.052 f_B - f_B}{1.052 f_B - 0.975 f_B} = 0.675; \text{ [4 marks]}$$

$$P_B = 337MW$$

Q6

(a) The expression for power in a three-phase circuit is

$$S_{ph} = \begin{bmatrix} V_a & V_b & V_c \end{bmatrix} \begin{bmatrix} I_a \\ I_b \\ I_c \end{bmatrix}^* = V_{ph}^t I_{ph}^*$$
 [2 marks]

The phase and sequence components are connected through transformation matrix

$$T = \begin{bmatrix} 1 & 1 & 1 \\ 1 & a & a^{2} \\ 1 & a^{2} & a \end{bmatrix} \text{ i.e } V_{ph} = TV_{s} S_{ph} = (TV_{s})^{t} (TI_{s})^{*}$$

$$= (T^{t}T^{*})V_{s}^{t}I_{s}^{*} = 3S_{s} [4 \text{ marks}]$$

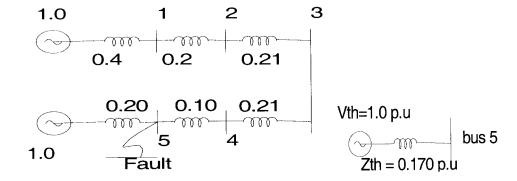
(b) The first task is to express every parameter in common base of 100 MVA and 15 kV on G2. For transmission line base kV 138. For G1 and T1 it is 12 kV.

The following relationship has to be used to arrive at p.u. value on a common base.

$$Z_{new}(pu) = Z_{old} * \frac{Base - MVA_{new}}{Base - MVA_{old}} \left( \frac{Base - kV_{old}}{Base - kV_{new}} \right)^2 pu$$

This produces positive sequence reactance in p.u for Gen #1: 0.40; Gen #2: 0.2; Transformer #1: 0.2; Transformer #2: 0.1pu,

- (i) Base impedance in ohm in 138kV line side is 138\*138/100; Positive sequence reactance of line in each segment ( between bus #2 & bus #3 and bus #2 & bus #4 is 0.21 p.u. [8 marks]
- (ii) The prefault voltage at bus 5 is 15kV and so it will be 1.0 p.u, since load current is neglected, the thevenin voltage would be 1.0 p.u, The Thevenin's reactance is 0.170 p.u. [4 marks]
- (iii) The fault current is 1/.170 = 5.89 pu. The base current at bus 5 is 100/(1.732\*15) kA = 3.85 kA; So the fault current in kA = 5.89\*3.85 = 22.67 kA. [2 marks] The positive sequence network and Thevenin equivalent is shown in the diagrams



The credits for drawing positive sequence diagram and Thevenin's diagram are included in the marking of part (i) and (ii)