Paper Number(s): E2.3

IMPERIAL COLLEGE OF SCIENCE, TECHNOLOGY AND MEDICINE UNIVERSITY OF LONDON

DEPARTMENT OF ELECTRICAL AND ELECTRONIC ENGINEERING EXAMINATIONS 2001

EEE PART II: M.Eng., B.Eng. and ACGI

POWER, FIELDS AND DEVICES

Monday, 18 June 2:00 pm

There are NINE questions on this paper.

There are three sections. Answer FIVE questions including at least ONE question from each of sections A, B and C.

Use a separate answer book for each section.

Time allowed: 3:00 hours

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Examiners:

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Juhasz, C., Leaver, K.D. and Juhasz, C.

Information for Candidates

Maxwell's equations:

$$\nabla \cdot \mathbf{D} = \rho$$
 ; $\mathbf{D} = \varepsilon \mathbf{E}$ $\nabla \cdot \mathbf{B} = 0$; $\mathbf{B} = \mu \mathbf{H}$
$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$$

$$\nabla \times \mathbf{H} = \mathbf{J} + \frac{\partial \mathbf{D}}{\partial t}$$

Physical constants and material parameters:

$$\epsilon_0 = 8.854 \text{ x } 10^{-12} \text{ F/m}$$

$$\mu_0 = 4\pi \text{ x } 10^{-7} \text{ H/m}$$

$$e = 1.602 \text{ x } 10^{-19} \text{ C}$$

$$kT = 0.025 \text{ eV at } 290 \text{ K}$$
 In SiO₂ $\epsilon = 4 \epsilon_0$ In silicon $\epsilon = 11.7 \epsilon_0$

Section A

Use a separate answer book for each section

1. (a)	Sketch the shape of the torque versus speed graph of a 3-phase induction machine. Explain in physical terms the shape of the curve at, just above and just below synchronous speed.	
		[5]
	Light.	
(b)	A 3-phase induction machine is connected to a 400 V 50 Hz supply. It has equivalent circuit parameters as follows:	
•	Number of pole-pairs, $P = 2$; Stator resistance, $R_S = 0.1 \Omega$; Rotor resistance, $R_R = 0.1 \Omega$; Magnetising reactance, $X_M = 10 \Omega$; Magnetising loss resistance, $R_M = 20 \Omega$; Stator leakage reactance, $X_S = 0.5 \Omega$;	
Re	Free L Rotor leakage reactance, $X_R = 0.5 \Omega$;	
	(i) Calculate the impedance of the machine for a slip of 0.04	[4]
	(ii) Calculate the stator current	[2]
	(iii) Calculate the rotor current	[3]
	(iv) Calculate the torque developed	
		[3]
	(v) Calculate the efficiency of the machine.	[3]

2.	(a)	Sketch the cross-section of a 3-phase generator and describe its features. Comment on the features of the construction that ensure that the generated voltage is sinusoidal.	[7]
	(b)	Three impedances of $8+j3$ Ω are connected in star configuration to a 400 V, 3-phase, 50 Hz supply.	
		(i) Calculate the phase current	503
			[3]
		(ii) Calculate the real power consumed	[2]
	(c)	The load in part (b) is found to be unbalanced. One impedance is 5% greater than stated and one is 5% less. Calculate the current that flows in the neutral line.	[5]
	(d)	The unbalanced impedances of part (c) are reconnected into delta. Calculate one of the line currents	
			[3]

3.	(a)	Explain why a switch-mode power supply, SMPS is more efficient than a linear voltage regulator.	[2]
	(b)	Sketch the circuits of both a buck and a boost SMPS. Sketch the shape of the current that flows in the inductor, diode and capacitor for each circuit assuming the inductor to be in continuous conduction mode.	[8]
	(c)	A boost converter is required to converter 5 V to 12 V. The capacitor has an effective series resistance (ESR) of 30 m Ω and has a capacitance that can be considered very large. The inductor has a value of 500 μ H. The switching transistor is operated at 25 kHz.	
		(i) Calculate the required duty-cycle.	[2]
		(ii) Calculate the ripple of the inductor current.	[2]
		(iii)Assuming continuous conduction, determine average value of inductor current when the output current is 5 A	[2]
		(iv)Determine whether the circuit is in fact in continuos conduction mode.	[2]
		(v) Calculate the output voltage ripple.	[2

Section B

Use a separate answer book for each section

- 4. (a) Using the appropriate Maxwell equation, together with the definition of electric field as the negative gradient of potential, show that the electrostatic potential in a dielectric medium of constant permittivity satisfies Laplace's equation $(\nabla^2 V = 0)$. [4]
 - (b) At the interface between a dielectric and a perfect conductor, the electric field on the dielectric side is normal to the conductor surface. Under what conditions will this also be true for a conductor with finite resistance?
 - (c) The figure below shows a length of coaxial transmission line. The line is shorted at the left-hand end by a conducting disk, and a constant potential difference V₀ is applied between the centre and outer conductors at the right-hand end. The inner conductor has finite resistance, but the outer conductor and the shorting disk may be assumed to be perfect conductors.

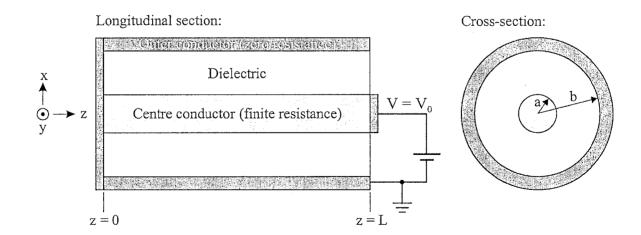
It is suggested that the potential V in the dielectric should vary as:

$$V = V_0 \frac{z}{L} \frac{\ln(b/r)}{\ln(b/a)}$$

where L is the length of the line, a and b are radii of the inner and outer conductors, and $r = (x^2 + y^2)^{1/2}$ is the radial distance from the z-axis.

Show that the above potential function is a solution of Laplace's equation, and that it satisfies the required boundary conditions on all conductor surfaces. [8]

Draw a longitudinal section showing electric field lines and equipotentials. You may neglect fringing effects at the open end. [6]



[2]

5. The electric field of a particular electromagnetic wave propagating in a highly conducting metal is given by:

$$\mathbf{E}(\mathbf{r},t) = \mathbf{E}_0 \hat{\mathbf{x}} \exp\{j(\omega t - \tau z)\}$$

with
$$\tau = \frac{1-j}{\delta}$$
 and $\delta = \sqrt{\frac{2}{\omega\mu\sigma}}$.

Here ω is the radian frequency of the wave, E_0 is the electric field amplitude at z=0, and μ and σ are the permeability and conductivity of the metal.

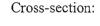
- (a) State the directions of propagation and polarization of the wave, and determine its phase velocity. What is the physical significance of δ ? [6]
- (b) Using a suitable Maxwell equation, derive an expression for the magnetic field vector, and hence show that the intrinsic impedance of the metal is:

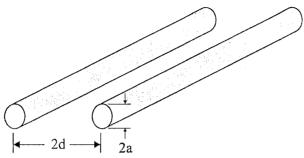
$$\eta_{\rm m} = (1+j)\sqrt{\frac{\omega\mu}{2\sigma}}$$
 [8]

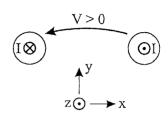
(c) A 100 MHz plane electromagnetic wave, travelling in air, is incident normally on a plane copper surface. Estimate the fraction of the power in the wave that is transmitted into the metal. The conductivity of copper is $5.8 \times 10^7 \ \Omega^{-1} \text{m}^{-1}$, and the impedance of free space is $377 \ \Omega$.

6. The figure below shows a twin-wire transmission line, comprising two cylindrical conductors of radius a. The conductor axes are separated by a distance 2d, and the surrounding dielectric medium has permittivity ε and permeability μ .

Twin-wire transmission line:







(a) The cross-section on the right shows a snapshot of the current direction and voltage polarity for a particular TEM wave travelling along the line. Redraw this cross-section, adding lines of electric and magnetic field. In what direction is the wave travelling, and what is its speed of propagation?

[6]

(b) The capacitance C per unit length of the line in part (a) is:

$$C = \frac{\pi \varepsilon}{\cosh^{-1}(d/a)}$$

Derive an expression for the characteristic impedance of the line in terms of C and the speed of propagation. Hence determine the minimum achievable impedance with air as the dielectric.

[6]

(c) Explain briefly the principles underlying the method of images.

[4]

The twin-wire line of part (a) is transformed to a single-wire line by replacing one of the conductors with a ground plane. The distance from the axis of the remaining conductor to this plane is d. What is the characteristic impedance of the new line? Justify your answer.

[4]

Section C

Use a separate answer book for each section

7. (a) Explain briefly what is meant by *channel length modulation*, and give, with reasons, the range of values of transistor voltages over which it occurs.

The SPICE model of channel length modulation is:

$$I_D = I_{DSS}(1 + \Lambda V_{DS})$$

where I_{DSS} and Λ are constants. Show that this identical to the assumption that the length that is pinched-off varies inversely as $(1+(\Lambda V_{DS})^{-1})$.

Why does the SPICE model include the factor ($1+\Lambda V_{DS}$) in voltage ranges in which channel length modulation does *not* occur?

How is the Early voltage V_A related to the SPICE parameters?

[13]

(b) A single-stage common-source integrated nMOS amplifier is designed to give a voltage gain of 20. The change in g_m with respect to gate voltage for MOSFETs in the chip is 0.03 S/V, their gate length is 0.7 μ m, and their overlap capacitance is due to a physical overlap of 0.05 μ m length.

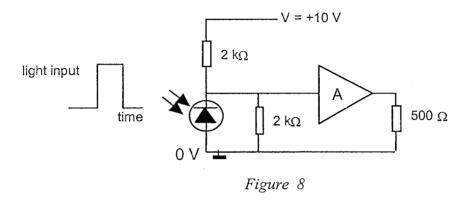
Find the input capacitance of the MOSFET amplifier in this circuit, assuming that the mobility of electrons is 0.08 m²/Vs in the channel.

[7]

8. (a) State the dependence on bias voltage of both the junction and diffusion capacitances of an ideal abrupt p-n diode. Hence show why in normal use one of these can usually be neglected compared to the other. You may assume the following equation:

$$W_n + W_p = \left[\left(\frac{2\epsilon_{si} (V_o - V)}{e} \right) \right] \left(\frac{1}{N_D} + \frac{1}{N_A} \right)^{1/2}$$

In the circuit of Fig. 8 a photodiode integrated with an amplifier is used to detect pulses of light having a negligible risetime.



Draw an AC equivalent circuit, assuming an ideal amplifier, and calculate the capacitance of the diode needed to ensure a 3dB bandwidth of 100MHz.

Photodiodes are available with capacitances specified at zero bias of 2.5 pF, 4.0 pF and 10 pF. Which, if any, of these would give the required bandwidth, assuming they each have a grading constant of 1/2, and a built-in voltage of 0.9 V?

[12]

(b) A junction diode has a reverse current of $3x10^{-7}$ A at -22 V bias, and is connected in parallel with a 2 k Ω resistor.

Calculate the value of the shot and thermal noise source strengths at room temperature in the frequency band between $100~\mathrm{MHz}$ and $120~\mathrm{MHz}$, when the total quiescent current through the two components is $1.5~\mathrm{mA}$, both :

- (1) in the diode's forward direction, and
- (2) in the diode's reverse direction.

You may ignore flicker noise.

[8]

9. The equation

$$\frac{dQ}{dt} = -\frac{Q}{\tau} + I_B$$

describes the transient behaviour of a bipolar transistor when biased in the active region in the circuit of *Figure 9*.

(a) Explain briefly where the charge Q is stored.

What equivalent circuit components relate to the quantity τ , and what physical quantities determine its value?

Explain carefully why the base current and not the emitter or collector current appears in the above equation. [10]

(b) The voltage source in Figure 9 is switched instantaneously from a positive value V_1 to a negative value $-V_2$ at time t = 0. Both V_1 and V_2 are much greater than 0.7 V.

Describe briefly two physical mechanisms that cause Q to decrease.

Sketch a graph of the dependence of the charge Q on time t, indicating on it the time at which the *collector* current reaches zero.

Show clearly the features on your graph which are related to τ , and V_1 and V_2 .

[7]

(c) Explain how the transistor turn-off time is affected by the values of V_1 and V_2 .

[3]

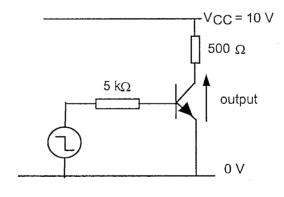


Figure 9

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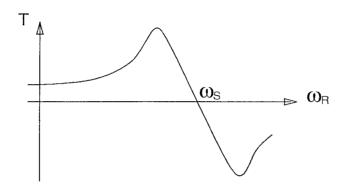
Answers

Section A - Power

Use a separate answer book for each section

1) (a) Sketch the shape of the torque versus speed graph of a 3-phase induction machine. Explain in physical terms the shape of the curve at, just above and just below synchronous speed.

[5]



At synchronous speed, the rotor bars rotate at the same speed as the magnetic field and so there is no change of flux linked with the bars; no induced EMF; no rotor current and no torque developed.

As the speed is decreased below synchronous speed, the rate of change of flux linkage increases in proportion; a proportionate current flows and a proportionate torque is developed. This holds until the frequency of the rotor voltage is such that the rotor becomes inductance dominated.

Above synchronous speed, a similar proportionate increase in torque is produced but the torque acts to decrease the speed.

(b) A 3-phase induction machine has equivalent circuit parameters as follow and is connected to a 400 V 50 Hz supply.

Number of pole-pairs, P = 2;

Stator resistance, $R_S = 0.1 \Omega$;

Referred Rotor resistance, $R_R = 0.1 \Omega$;

Magnetising reactance, $X_M = 10 \Omega$;

Magnetising loss resistance $R_M = 20 \Omega$;

Stator leakage reactance, $X_S = 0.5 \Omega$;

Referred Rotor leakage reactance, $X_R = 0.5 \Omega$;

(i) Calculate the impedance of the machine for a slip of 0.04

[4]

$$Z_{S} = R_{S} + jX_{S}$$

$$Z_{R} = \frac{R_{R}}{s} + jX_{R}$$

$$Z_{M} = R_{M} // jX_{M}$$

$$Z_{T} = Z_{S} + Z_{R} // Z_{M}$$

$$= 2.07 + j1.30 \Omega$$

$$= 2.45 \langle +32.2^{\circ} \Omega$$

(ii) Calculate the stator current

$$V_S = \frac{1}{\sqrt{3}} V_L$$

$$I_S = \frac{V_S}{Z_T}$$

$$= 94.3 \langle -32.2^{\circ} A$$

(iii) Calculate the rotor current

$$I_{R} = I_{S} \frac{Z_{M}}{Z_{R} + Z_{M}}.$$

$$= 78.8 \langle -21.3^{\circ} A$$

(iv) Calculate the torque developed

$$P_{Mech} = 3I_R^2 R_R \left(\frac{1}{s} - 1\right)$$

$$= 44.7 kW$$

$$\omega_R = (1 - s) \frac{\omega_E}{P}$$

$$= 150.8 rad / s$$

$$T = \frac{P_{Mech}}{\omega_R} = 296.5 Nm$$

(v) Calculate the efficiency of the machine.

$$P_{In} = 3 \operatorname{Re} \left\{ V_{S} I_{S}^{*} \right\}$$

$$= 55.3 \, kW$$

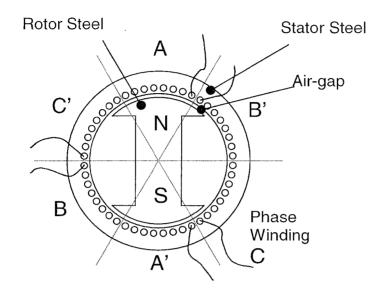
$$\eta = \frac{P_{Mech}}{P_{In}}$$

$$= 80.1 \%$$

[2]

2) (a) Sketch the cross-section of a 3-phase generator and describe its features. Comment on the features of the construction that ensure that the generated voltage is sinusoidal.

[7]



- The machine is constructed from laminated steel compressed into stacks.
- The stator stack has slots in the inside surface that carry the coils in which the EMF will be generated
- The coils are distributed around the whole circumference but grouped into phase windings
- The rotor carries a winding of DC current or a permanent magnet
- The stator and rotor are separated by an air-gap that is kept as small as practicable
- The air-gap field is radial and uniform under each rotor pole
- The induced EMF in a coil is trapezoidal
- By connecting several adjacent coils in series, a voltage is created that is a staircase approximation to a sinewave and is free of low-order harmonic distortion
- (b) Three impedances of 8+j3 Ω are connected in star configuration to a 400 V, 3-phase, 50 Hz supply.
 - (i) Calculate the phase current

[3]

$$\begin{split} V_P &= \frac{1}{\sqrt{3}} V_L \\ &= 230.9 \, V \\ I_P &= \frac{V_P}{Z} \\ &= 25.3 - j9.5 \, A \\ &= 27.0 \langle -20.55^\circ \, A \end{split}$$

(ii) Calculate the real power consumed

$$P = 3V_p I_p \cos(\phi)$$

$$= 3 \operatorname{Re} \left\{ V_p I_p^* \right\}$$

$$= 17.5 \, kW$$

(c) The load in part (b) is found to be unbalanced. One impedance is 5% greater than stated and one is 5% less. Calculate the current that flows in the neutral line.

[5]

[2]

Different angles of neutral current will result from different arrangements of the impedances. $I_A=25.3-i9.5\ A$

$$I_{B} = \frac{V_{P} \langle -120^{\circ}}{1.05 \times Z}$$
$$= -19.9 - j16.3 A$$

$$I_C = \frac{V_P \langle +120^\circ \\ 0.95 \times Z}{0.95 \times Z}$$

$$= -4.7 + j28.1 A$$

$$I_N = -I_A - I_B - I_C$$

$$=-0.8-j2.2 A$$

Different angles of neutral current will result from different arrangements of the impedances.

(d) The unbalanced impedances of part (c) are reconnected into delta. Calculate one of the line

[3]

Three possible answers given here:

$$V_{AB} = 400\langle 0^{\circ} V \rangle$$

$$V_{BC} = 400 \langle -120^{\circ} V$$

$$V_{CA} = 400\langle 120^{\circ} V$$

$$I_{AC} = \frac{V_{AB}}{Z}$$
$$= 43.8 - j16.4 A$$

$$I_{BC} = \frac{V_{BC}}{1.05 \times Z}$$
$$= -34.4 - j28.3 A$$

$$I_{CA} = \frac{V_{CA}}{0.95 \times Z}$$
$$= -8.1 + 48.6 A$$

$$\begin{split} I_A &= I_{AB} - I_{CA} \\ &= 51.9 - 65.1 \, A \\ &= 83.2 \langle -51.4^{\circ} \, A \\ I_B &= I_{BC} - I_{AB} \\ &= -78.2 - 11.9 \, A \\ &= 79.2 \langle -171.4^{\circ} \, A \\ I_C &= I_{CA} - I_{BC} \\ &= 26.3 + 76.9 \, A \\ &= 81.3 \langle +71.1^{\circ} \, A \end{split}$$

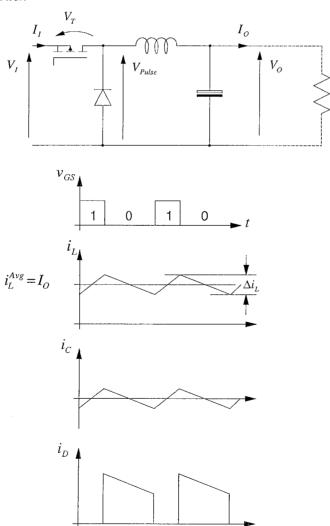
A switch-mode power supply uses a transistor in two states, fully on (e.g. ohimc region of a MOSFET) or fully off. The transistor only traverses the active region briefly between these two sates. Thus a coincidence of voltage across the transistor and current through it are avoided and power dissipation is low.

A linear regulator uses a transistor to "drop" voltage between input and output and thus there is voltage across it while it carries current. The transistor is in its active region and dissipates considerable power.

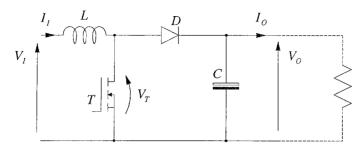
(b) Sketch the circuits of both a buck and a boost SMPS. Sketch the shape of the current that flows in the inductor, diode and capacitor for each circuit assuming the inductor to be in continuous conduction.

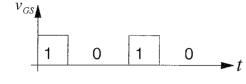
[8]

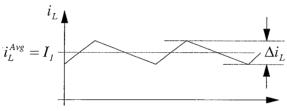
Buck

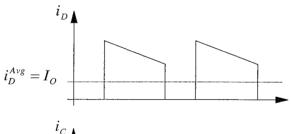


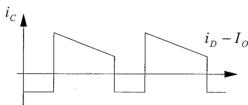












- (c) A boost converter is required to converter 5 V to 12 V. The capacitor is large valued and has an effective series resistance, ESR of 30 m Ω . The inductor is 500 μ H. The switching transistor is operated at 25 kHz.
 - (i) Calculate the required duty-cycle.

[2]

$$\frac{V_o}{V_I} = \frac{1}{1 - \delta}$$
$$\delta = \frac{V_o - V_I}{V_o}$$
$$= 0.58333$$

(ii) Calculate the ripple of the inductor current.

[2]

$$\Delta i_L = \frac{V_I}{L} \times \frac{\delta}{f}$$
$$= 0.2333 A$$

(iii) Assuming continuous conduction, determine average value of inductor current when the output current is $5\,\mathrm{A}$

[3]

$$i_D^{Avg} = I_O$$

$$i_D^{Avg} = i_L^{Avg} (1 - \delta)$$

$$i_L^{Avg} = \frac{I_O}{(1 - \delta)}$$

$$= 12 A$$

(iv) Determine whether the circuit is in fact in continuous conduction.

[1]

 $i_L^{Avg} > \frac{1}{2} \Delta i_L$ therefore the inductor current is continuous

(v) Calculate the output voltage ripple.

[2]

$$i_C^{ptp} = i_D^{ptp}$$

$$= i_L^{Avg} + \frac{1}{2}\Delta i_L$$

$$= 12.12 A$$

$$v_O^{ptp} = i_C^{ptp} R_{ESR}$$

$$= 364 mV$$

4 (a) Maxwell I:
$$\nabla \cdot \mathbb{P} = \nabla \cdot (\varepsilon E) = \rho$$

In a dielectric where $\varepsilon = \text{const.}$ and $\rho = 0$ this
becomes $\nabla \cdot E = 0$ and, since $E = -\nabla V$, we have
 $\nabla \cdot (\nabla V) = 0$ or $\nabla^2 V = 0$ [4]

(b) For perfect conductor,
$$E=0$$
 inside, and continuity of EN at boundary gives $EN=0$ ovtside.

For real conductor, still have continuity of EN ,

but $E=0$ inside only if no wrient [2]

[Otherwise EN outside = EN when EN is when EN at conductor surface.]

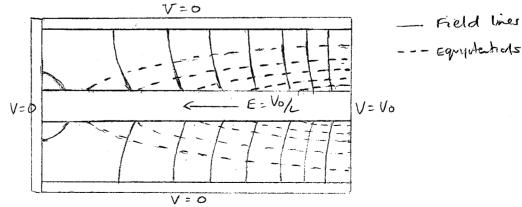
(c) Need to show
$$\frac{\partial^2 V}{\partial x^2} + \frac{\partial^2 V}{\partial y^2} + \frac{\partial^2 V}{\partial z^2} = 0$$
 for $V = Z \ln(b/r)$

$$\frac{\partial V}{\partial x} = -\frac{Z}{r} \frac{\partial r}{\partial x} = -\frac{XZ}{r^2} \qquad \frac{\partial^2 V}{\partial x^2} = -\frac{Z}{r} + \frac{2x^2Z}{r^4} \qquad \left(uxcd \frac{\partial r}{\partial x} = \frac{x}{r^2} \right)$$

$$\Rightarrow \frac{\partial^2 V}{\partial x^2} + \frac{\partial^2 V}{\partial y^2} = -\frac{ZZ}{r^2} + \frac{2x^2Z}{r^4} + \frac{2y^2Z}{r^4} = 0 \qquad \left(\frac{x^2 + y^2 = r^2}{r^4} \right)$$

Also,
$$\frac{\partial V}{\partial z} = h(b/r)$$
, $\frac{\partial^2 V}{\partial z^2} = 0$ \Rightarrow $\nabla^2 V = 0$ as replaced.

when $r = \alpha$, $V = \frac{V_{0Z}}{L}$ v uniform Efield with $E = \frac{V_{0}}{L}$ in inner (real) conductor [



NB. My sketch world be better ? Page 1016

C23

[6]

So (a)
$$E = E_0 \hat{2} \exp j(\omega t - \frac{z}{8} + \frac{z}{6}) = E_0 \hat{2} = e$$

Where is $x = pstanged$, and property in $+ \pm dir^{2}$

Pluse velocity? $\beta = \omega t - \frac{2}{8} = cont$. $\Rightarrow \pm = \omega st + cont$.

So $V_P = \omega s$
 $S = Skin depth$; depth are which anythread of EM course extens conductor facts to $V_P = \omega s$
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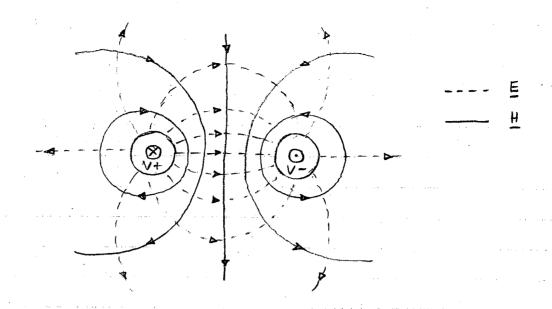
Page 2016

= 0.0027 %

G 2.3

[6]

6 (a)



Considery EXH eg at mid-point behven conductors

EXH Point into page → Proxyatu lum is -2

wave is TEM => Speed of project is $v = \frac{1}{\sqrt{GU}}$

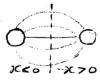
(b)
$$Z_0 = \int \frac{L}{c}$$
 and $v = \frac{1}{\sqrt{Lc}} \Rightarrow Z_0 = \frac{1}{vC}$

So
$$Z_0 = \sqrt{\epsilon \mu \cdot \frac{\cosh^{-1}(d/\omega)}{\pi \epsilon}} = \sqrt{\frac{\cosh^{-1}(d/\omega)}{\pi}}, \quad \gamma = \sqrt{\frac{\mu}{\epsilon}}$$

For air, $\eta = 377 \Omega$ and $\% \ge 1 \Rightarrow Z_0 \ge 120 \Omega$

(MIO.I : involves friendling a distribution of charges that satisfies bondary anditions of problem. Southi is then sum of potential due to change. Relies on

unique ess.



Considere tuin - wire line, dotted line is equiptertial

> Regin X>0 can be replaced by enderthe w/o affecting packed in x < 0

Also, for given a per wit length p.d. between each and and mid-line = 1 that between conductus

$$\Rightarrow$$
 For sigle-wie line $C = 2 \times \frac{\pi \epsilon}{\alpha \lambda^{-1}(d/a)}$

$$V = \frac{1}{\sqrt{\mu \epsilon}}$$
 stru true, $50 = \frac{1}{2\pi} \frac{\cosh^{-1}(d_{a})}{2\pi}$

[6]

[6]

[4]

[4]

E 2.3

Dectrin C: Devices: Answers.

7. (a) Channel length modulation: the effect on drain current of the princh-off occurring at the drain end of the Conducting channel when the drain-source voltage rises beyond 45-V7.

Physice model: IDSS = Const L-Ld believe bed in the prinched off length. Setting this equal to given expression, L-Ld = (1 + 1 - VDS) Const. C.e. bed = 1 - (1+1 VDS) = [1+(1 VDS)-1]-1

SPICE model ensures continuité of the values across the triode and seturation regions, which are modeller by different exposions.

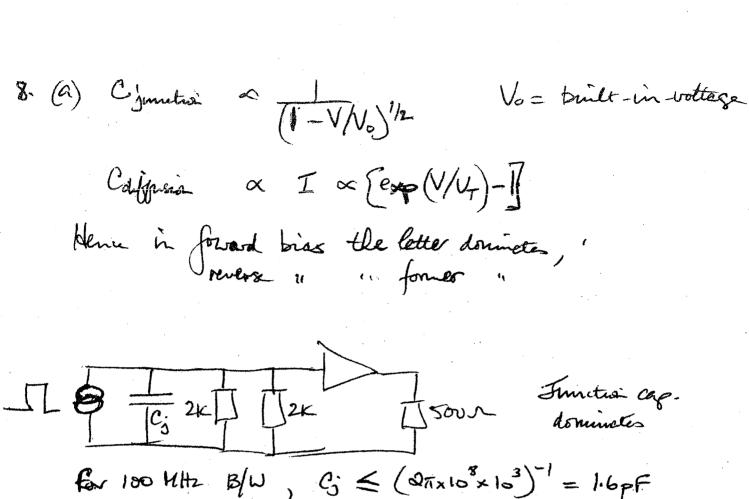
Early voltage V_A = value of V_{DS} at while I_D extrapolates to geno: i.e. $\Lambda_{V_A} = -1$.

(b) $\frac{g_m}{V_{qs}-V_T} = \rho \cos \frac{W}{L} = 0.03 \text{ S}, So C_{ox}WL = \frac{0.03}{0.08} \times 0.49 \times 10^{-12}$ = 0.184 pf

and Cgd = CoxxWx Loverlap = 0.184 x 0.05 pF = 0.013 pF 0.7 (Hiller appointance)

Hence effective injent capacitance = (1+A) x0.013 + 2 x 0.184 gf

= 0.396 pF.



For 100 HHz B/W, G ≤ (QTIX 10 × 103) = 1.6 pF

Now Voies = -5V, so zero-bias capacitance Cjo must be Cjo & 1.6pf (1+5/0.9) = 4.09pf

Hence oney oney 2 photodiodes arox.

in = DeIB - idea diodes e genetions in = 4kTgB - resistors (b) Shot horse arment Thermal "

Thermal "

Orini (resistor)

15K $\lambda_{n_i}^2 = \frac{4kT \times 0.2 \times 10^6}{15 \times 10^3} = 2.13 \times 10^{-19}$ Bd = OF/OV can D I = 1.5 mA $l_{n2} = 2ex/.5x10^{-3}x0.2x10^{6} = 9.6x10^{-17}$ inz (diode) cax(2) $I = 4 \times 10^{-7} A$ $i_{n2} \approx 4 \times 10^{-7} \times 2 e \times 0.2 \times 10^{6} = 2.86 \times 10^{-19}$

velues et frequences above a few humand kttz.

Par. 5 off

モノウ

q (a) Q i stored in hertoer best region. T is either best-ender equivalent arent time constant Vbe Cbe, Where Vb = 4 & G = TpIe Where Is is the transit time thro the pase or The Bx Tf Where B is awent gam dependent on doping in Emille above land recontinuat in the base ... soon students will reall this) If depends on bose will and diffusion coefficient. Clarge Q consists of eggled quantities Q of majority & missority carriers. The former can my be removed or injected via the base Contacts (because their motion—Dro! they muchin is apposed by the potential across that Junction \ Hence Q can be extrected by IB. (b) Q decreeses by (1) removal of majority charge via the base. (each relater to me of the 2 terms in the expretion given exponential witing constant T transister goes off here (Ic=0) (c) that of time of reiser by increasing V_1 (rhixe Q(0)) and decreased by increasing $|V_2|$ (factor extraction Q(0) vie F_B).

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