

2010 Mathematics

Intermediate 1 Units 1, 2 & 3 Paper 2

Finalised Marking Instructions

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Part One: General Marking Principles for Mathematics Intermediate 1 Units 1, 2 & 3 Paper 2

This information is provided to help you understand the general principles you must apply when marking candidate responses to questions in this Paper. These principles must be read in conjunction with the specific Marking Instructions for each question.

- Marks for each candidate response must <u>always</u> be assigned in line with these general marking principles and the specific Marking Instructions for the relevant question. If a specific candidate response does not seem to be covered by either the principles or detailed Marking Instructions, and you are uncertain how to assess it, you must seek guidance from your Team Leader/Principal Assessor. You can do this by posting a question on the Marking Team forum or by e-mailing/phoning the emarker Helpline. Alternatively, you can refer the issue directly to your Team Leader by checking the 'Referral' box on the marking screen.
- 2. Marking should always be positive ie, marks should be awarded for what is correct and not deducted for errors or omissions.
- **3.** Award one mark for each 'bullet' point shown in the Marking Instructions.
- 4. Working subsequent to an error must be followed through with the possibility of awarding all remaining marks for the subsequent working, provided the question has not been not simplified as a result of the error. In particular, the answer to one part of a question, even if incorrect, must be accepted as a basis for subsequent dependent parts of the question. Full marks in the dependent part(s) may be awarded provided the question has not been not simplified.
- 5. Solutions which seem unlikely to include anything of relevance must nevertheless be followed through. Candidates still have the opportunity of gaining one mark or more provided the solution satisfies the criteria for the marks.
- **6.** The following should not be penalised:
 - working subsequent to a correct answer (unless it provides firm evidence that the requirements of the question have not been met)
 - omission or misuse of units (unless marks have been specifically allocated for the purpose in the Marking Instructions)
 - bad form, eg sin $x^{\circ} = 0.5 = 30^{\circ}$
 - legitimate variation in numerical values/algebraic expressions
- 7. Full credit should only be given where the solution contains appropriate working. Where the correct answer may be obtained by inspection or mentally, credit may be given, but reference to this will be made in the Marking Instructions.
- **8.** In general only give credit for answers if working is shown. A wrong answer without working receives no credit unless specifically mentioned in the Marking Instructions. The rubric on page one of the question paper states that 'full credit will be given only where the solution contains appropriate working'.
- 9. Sometimes the method to be used in a particular question is explicitly stated; no credit should be given where a candidate obtains the correct answer by an alternative method.
- 10. Where the method to be used in a particular question is not explicitly stated, full credit must be given for alternative methods which produce the correct answer.

- 11. Do not penalise the same error twice in the same question.
- 12. Do not penalise a transcription error unless the question has been simplified as a result.
- Where a solution has been scored out and not replaced then provided the solution is legible marks should be awarded in line with the Marking Instructions for that question.
- **14.** Where more than one solution is given, mark them all and award the least mark.
- 15. The symbols \checkmark and \times are used in the Marking Instructions to give guidance regarding the awarding of marks for specific candidate responses to some questions, eg 'award $2/4 \checkmark \times \times \checkmark$ ' indicates that the 1st & 4th marks should be awarded but the 2nd & 3rd marks should not.

Part Two: Mathematics Intermediate 1: Paper 2, Units 1, 2 and 3

Question	Expe	Expected Answer/s		Additional Guidance	
1	Ans: •¹ •²	220 km know how to find distance: $80 \times 2\text{h}45\text{m}$ calculate distance: $80 \times 2.75 = 220$	2	 Correct answer without working award 2/2 Answers acceptable for partial credit (no working necessary) (a) 196 [80 × 2·45] award 1/2 ✓ × (b) 13200 [80 × 165] award 1/2 ✓ × (c) 29(·09)[80 ÷ 2·75] award 1/2 × ✓ 	
2	Ans: •¹ •²	£702 find monthly premium: $1.30 \times 45 = 58.5(0)$ find annual premium: $58.5(0) \times 12 = 702$	2	 Correct answer without working award 2/2 Answer acceptable for partial credit (no working necessary) 15·6(0) [1·30 × 12] award 1/2 2nd mark is not available if there is invalid subsequent working 45702 [702 + 45000] award 1/2 45058·5 [58·5 + 45000] award 1/2 	
3	Ans: •¹ •²	9×10^{-2} mm find thickness of one sheet: $45 \div 500 = 0.09$ express answer in standard form: 9×10^{-n} consistent power of ten: 9×10^{-2}	3	 Correct answer without working award 3/3 Some common answers (no working necessary) 0.9×10⁻¹ award 2/3 ✓×✓ 2.25×10⁴ [45×500] award 2/3 ×✓✓ 9×10⁻³cm, 9×10⁻⁵m with units shown award 3/3 500÷45 = 11·1= 1·1×10 n = 1·1×10(1) award 2/3 ×✓✓ but 11·1= 1×10 n = 1×10(1) award 1/3 ××✓ 	

Que	estion	Expected Answer/s		Max Mark	Additional Guidance
4		Ans: •¹ •²	x > 13 collect constants: $5x > 65$ solve inequality for x : x > 13	2	 For answers without valid working award 1/2 eg (a) x > 13 without working
5		Ans: •¹ •² •³	table: 1400 1125 750 7200 know to divide Σ fx by 40: 7200 ÷ 40 divide Σ fx correctly and give	3	 Award of 1st mark: 1400, 1125, 750 and 7200 need not appear in table but must be shown in working 2nd mark may only be awarded for attempting ∑ fx ÷ 40 3rd mark may only be awarded for
			answer in full: 180000 or 180 thousand		correctly dividing Σ fx and giving answer in full 4. With Without evidence evidence for 1st for 1st mark mark 180 000 3/3 $\checkmark \checkmark \checkmark$ 2/3 $\times \checkmark \checkmark$ 180[7200÷40] 2/3 $\checkmark \checkmark \checkmark$ 1/3 $\times \checkmark \checkmark$ 1 200 000 [7200÷6 = 1200] 2/3 $\checkmark \times \checkmark$ 1/3 $\times \times \checkmark$ 1 200 [7200÷6] 1/3 $\checkmark \times \times$ 0/3

Que	estio	n	Expected Answer/s	Max Mark	Additional Guidance	
6	a		Ans: $ \begin{array}{c cccc} x & -9 & 0 & 6 \\ \hline y & -1 & 2 & 4 \end{array} $ • calculate y when $x = -9$: -1 • calculate y when $x = 0$ and 6: 2 and 4	2		
	b	i	Ans: straight line graph of $y = \frac{1}{3}x + 2$ • 1 correctly plot all three points from the table • 2 draw straight line through the three points shown in the table	2	 If the line y = 1/3x + 2 is drawn (even if this is not consistent with the points in the table) award 2/2 [minimum acceptable length: line joining (-9,-1) to (3,3)] Where the points in the table satisfy y=x, the points are plotted and a line is drawn through them award 1/2 Where the three points plotted are consistent with the table and are not collinear, the 2nd mark is unavailable Where (y, x) is consistently plotted, answer should be followed through with the possibility of awarding the 2nd mark 	
6	b	ii	Ans: straight line graph of $x = 4$ • 1 draw the line $x = 4$	1	 If line is definitely correct award 1/1; if line is definitely wrong award 0/1; in other cases key in – (dash) and when you finish marking click on the 'Exception Script SQA' icon. Beware: answer may not be visible until you zoom in. Where (y,x) is consistently plotted in b(i), the mark is only available for drawing the line y=4. 	

Question	Expected Answer/s		Max Mark	Additional Guidance	
7	Ans:	39 cm	4		
	•1	find dimensions of screen: 33 and 21		1.	Correct answer without working award 4/4
	•2	correct form of Pythagoras Theorem: $33^2 + 21^2$		2.	Final answer may be rounded or truncated.
	•3	calculate sum (or difference) of squares: 1530		3.	Final mark is not available if there is invalid subsequent working e.g. $39 \div 2 = 19.5$
	•4	calculate square root of sum (or difference) of squares: 39(·1)		4. (a) (b) (c) (d) 5.	Some common answers (working must be shown) $\sqrt{(37^2 + 25^2)} = 45, 44.7, 44.6()$ award $3/4 \times \sqrt{\sqrt{\sqrt{(35^2 + 23^2)}}} = 42, 41.9, 41.8()$ award $3/4 \times \sqrt{\sqrt{\sqrt{(33^2 - 21^2)}}} = 25, 25.5, 25.4()$ award $3/4 \times \sqrt{\sqrt{\sqrt{(37^2 - 25^2)}}} = 27, 27.3, 27.2()$ award $2/4 \times \sqrt{\sqrt{(37^2 - 25^2)}} = 27, 27.3, 27.2()$ award $2/4 \times \sqrt{\sqrt{(37^2 - 25^2)}} = 27, 27.3, 27.2()$ Example of alternative strategy involving trigonometry \bullet^1 33 and 21 \bullet^2 a° = tan ⁻¹ ($^{21}/_{33}$) = 32.47° \bullet^3 cos32.47° = $^{33}/_x$ \bullet^4 $x = ^{33}/_{\cos 32.47^9} = 39(.1) Do not penalise inadvertent use of radians or grads if trigonometry is used.$

Que	estion	Expected Answer/s		Max Mark	Additional Guidance
8 8	estion		the state of the		 4·14 (no working necessary) award 3/3 Alternative strategy ¹ calculate saving in dollars: 35 × 1·62 - 50 = 6·7(0) ² know how to convert saving into sterling: 6·7(0) ÷ 1·62 ³ convert saving in sterling: 4·14 or 4·13 Some ways of obtaining 4·13 as answer (a) 35- 30·864(= 4·136) = 4·13 award 3/3 (b) 35- 30·87 = 4·13 award 2/3 ✓×✓ (c) 4·13 with no working award 2/3 The 2nd mark is only available where the answer to the division has to be rounded or truncated to the nearest penny eg Do not award the mark for 50 ÷ 1·6 = 31·25 (a) 35÷1·62 = 21·60 award 1/3 ×✓× (b) 50 - 35÷1·62 = 28·40 award 2/3 ✓×✓ (c) 35 - 35÷1·62 = 13·40
					award 2/3 ✓×✓

Question	Expected Answer/s	Max Mark	Additional Guidance	
Question 9	Expected Answer/s Ans: £40.95 • 1 • 2 know how to calculate interest: $^{1.3}/_{100} \times 4200 \times ^{9}/_{12}$ (award 1 for $^{1.3}/_{100} \times 4200$ or $^{9}/_{12} \times 1.3$ or $^{9}/_{12} \times 4200$) • 3 carry out percentage and fraction calculations correctly: $^{4}0.95$		 Correct answer without working award 3/3 If answer is 4240·95 [4200 + 40·95] (no working necessary) (a) award 3/3 if candidate states that interest is 40·95 (b) award 2/3 if candidate does not state that interest is 40·95 Acceptable answers for partial credit (no working necessary) (a) 54·6(0) [1·3% of 4200] award 1/3 (b) 0·975 [9/12 × 1·3] award 1/3 	
			 (c) 3150 [9/12 × 4200] award 1/3 (d) 491·4(0) [54·6(0) × 9] award 1/3 4. 3rd mark is not available where premature rounding leads to an incorrect answer e.g. 9/12 × 1·3 = 0·975 → 0·98/100 × 4200 = 41·16 	

Question	Expected	d Answer/s	Max Mark	Additional Guidance
10	$ \begin{array}{ccc} & 13 \\ \bullet^2 & & \text{km} \\ & \text{an} \\ & \sqrt{(} \\ \bullet^3 & & \text{ca} \\ & \text{co} \\ & 7 \cdot 2 \\ & \boxed{(} () \\ \bullet & \bullet \\ \end{array} $	now to divide 1369 by 25: $669 \div 25$ now to find square root of: swer to above: $(1369 \div 25)$ lculate $\sqrt{(1369 \div 25)}$ prrectly:	3	 Correct answer without working award 3/3 54·76, 54·8 or 54·7 (no working necessary) award 1/3 Some common answers (working must be shown) (a) 54·76 ÷ 4 = 13·69 award 2/3 (b) 1369 ÷ 100 = 13·69 award 0/3 Alternative strategy find L×L×25 for any L: eg 4×4×25 = 400 show that 7<l<8: 7×7×25="1225" 8×8×25="1600</li" and="" eg=""> find length of base: 7·4 </l<8:>
11	$ \begin{array}{ccc} & \text{of} \\ & 9 \\ & & 10 \\ & 90 \\ & & & \\ & & & & \\ & & & & \\ & & & &$	now to express 90 as a fraction $\frac{750}{750}$; $\frac{90}{750}$ now to multiply fraction by $\frac{90}{750} \times 100$; rry out all calculations prectly:	3	 Correct answer without working award 3/3 3rd mark is only available for calculations of the form ^a/_b × c where a,b,c = 90 or 750 or 100 or 660 or 840 Some common answers (working must be shown) (a) 833(·3) [⁷⁵⁰/₉₀ × 100] award 2/3 × √ √ (b) 8·3(3) [⁷⁵⁰/₉₀] award 0/3 (c) 675 [⁹⁰/₁₀₀ × 750 or ⁷⁵⁰/₁₀₀ × 90] award 1/3 × × √ (d) 88 [⁽⁷⁵⁰⁻⁹⁰⁾/₇₅₀ × 100] award 2/3 × √ √ (e) 8112 [⁽⁷⁵⁰⁺⁹⁰⁾/₇₅₀ × 100] award 2/3 × √ √

Que	estion	n Ex	Expected Answer/s		Additional Guidance	
12	a	•¹ •²	order numbers: 17 18 18 19 20 21 23 24 26 27 27 27 28 31 find median: 23.5	2	 Correct answer without working award 2/2 21 [numbers not ordered] (a) with valid working award 1/2 (b) without valid working award 0/2 If "correct" median is found from ordered list with one missing or one extra number award 1/2 Accept ordered list written in part (a) or part (b) 	
12	b	An	find range: 31 – 17 = 14	1		
12	c	•¹ •²	as: 5C collected more on average. Amounts collected by 5M are more varied. interpret statistics: 5C collected more. (or equivalent) interpret statistics: Amounts collected by 5M varied more. (or equivalent)	2	 Answer must be consistent with answers to parts (a) and (b) Do not accept e.g. 5C has a higher median 5M has a higher range 	

Questi	ion	Expected Answer/s		Max Mark	Additional Guidance
13		Ans:	29 m	3	
		•1	use correct sine ratio: $\sin 65^\circ = {}^{h}/_{32}$		1. Correct answer without working award 2/3
		•2	know how to solve equation: $h = 32 \times \sin 65^{\circ}$		2. Do not penalise inadvertent use of radians or grads 26(·458) (radians used) award 3/3 27(·284) (grads used) award 3/3
		•3	carry out trig. calculation: 29 (·0018)		3. Disregard premature rounding or truncation eg 32 × sin65° = 32 × 0·9 = 28·8 award 3/3
					 4. Where an incorrect trig ratio is used, working should be followed through with the possibility of awarding 2/3. [Disregard premature rounding or truncation] (a) 32 × cos65° = 13·5(23) award 2/3 ×√√ (b) 32 × cos65° = 32 × 0·4 = 12·8 award 2/3 ×√√ (c) 32 × tan65° = 68·6(24) award 2/3 ×√√ (d) 32 × tan65° = 32 × 2·1 = 67·2 award 2/3 ×√√

Question	Expe	Expected Answer/s		Additional Guidance		
			Mark			
14	Ans:	306 cm	5			
	•1•2	know how to calculate circumference of semi-circle: $\frac{1}{2} \times \pi \times 80$ (award 1 for $\frac{1}{2} \pi d$ or $\pi \times 80$ or $\frac{1}{2} \times \pi \times 40^2$)		 306 without working award 0/5 (a) 5th mark is only available where the candidate is required to round final answer or answer to circle calculation to nearest whole 		
	•3	know to add $\frac{1}{2}$ π d + 180: $\frac{1}{2} \times \pi \times 80 + 30 + 50 + 20 + 50 + 30$		number. (b) Versions of the answers below which are not rounded,		
	•4	carry out all calculations correctly: $305 \cdot 6(6)$ (must include a calculation involving π followed by an addition or a subtraction)		incorrectly rounded or not requiring to be rounded should not be awarded the 5 th mark. BEWARE: although $\pi \times 40^2$ needs to be rounded 3.14 × 40 ² does not .		
	•5	round to nearest centimetre: 306		 3. Some common answers (working must be shown) (a) 256 [½×π×80 + 130] award 4/5 √√√√ (b) 431 [π×80 + 180] award 4/5 ×√√√ (c) 2693 [½×π×40² + 180] award 4/5 ×√√√ (d) 3513 [½×π×40² + 20×50] award 4/5 ×√√√ (e) 5207 [π×40² + 180] award 3/5 ××√√ (f) 6027 [π×40² + 20×50] award 3/5 ×√√√ (g) 1251 [π×80 + 20×50] award 3/5 ×√√√ (i) 126 [½×π×80] award 3/5 √√×√√ (j) 251 [π×80] award 2/5 ×√×√√ (k) 2513 [½×π×40²] award 2/5 ×√××√ (l) 5027 [π×40²] award 1/5 ××××√ 		

Que	estio	n	Expe	cted Answer/s	Max Mark	Additional Guidance
15	a		Ans: •¹ •²	$\frac{1}{5}$ find probability: $\frac{3}{15}$ simplify fraction: $\frac{1}{5}$	2	 Correct answer without working award 2/2 Award 1/2 for 1:5, 3:15, 1 out of 5, 3 out of 15, 1 in 5, 3 in 15, 1-5, 3-15, 0·2(0), 20% Award 1/2 (no working necessary) for 1/4 [3/12], 4/5 [12/15]
	b		Ans: •¹ •²	experiment: $eg \frac{4}{16}$ continue until correct answer is found: 6	2	 The only acceptable valid methods are (a) Write down any fraction of the form 3+n/15+n e.g. 4/16 (b) write down any two fractions equivalent to 1/3 (c) evidence that 1/3 of any number >15 is more than 5 e.g. 1/3 of 16 = 5·3, 5r1, 5·1 (a) 6 without working award 1/2 (b) 6 with invalid working award 0/2 6/18 (no working necessary) award 1/2

TOTAL MARKS FOR PAPER 2 50

> TOTAL MARKS FOR PAPER 1 & 2 80

[END OF MARKING INSTRUCTIONS]