

Mark Scheme (Results)

January 2009

GCE O Level

O Level Mathematics B (7361) Paper 1

Mathematics B 7361

Paper 1

1. (a) 0.0625 B1 1
 (b) 6.25% (o.e.) B1 ft 1
 2
 Total 2 marks

2. an attempt at the bisector of $\angle RPQ$ drawn M1
 bisector of $\angle RPQ$ drawn $\pm 1\text{mm}$ (ie no daylight) A1
 2
 Total 2 marks

3. $4x - \frac{x}{3} > 10 + 1$ (o.e.) M1
 $x > 3$ A1
 2
 Total 2 marks

4. (a) 75 mins B1 1
 (b) 45 mins B1 1
 2
 Total 2 marks

5. (a) 0 B1 1
 (b) 2 B1 1
 2
 Total 2 marks

6. $\frac{54}{A} = \frac{9^2}{4.5^2}$ (o.e.) M1
 13.5 cm^2 A1
 2
 Total 2 marks

7. $4x + x = 180$ M1
 36 A1
2
Total 2 marks
8. 11 and 29 clearly identified M1
40 A1
2
Total 2 marks
9. $w = 90^\circ$ B1
 $a = -1$ B1
2
Total 2 marks
10. $\frac{?}{1000} \times 360 = 126$ M1
 $? = \frac{126 \times 1000}{360}$ M1 dep
350 red cars A1
3
Total 3 marks

11. Either:

$$3x - 4 = 3 - 2x \quad \text{M1}$$

$$3x + 2x = 3 + 4 \quad (\text{isolating } x) \quad \text{M1 dep}$$

$$x = \frac{7}{5} \quad (\text{o.e.}) \quad \text{A1}$$

3

or:

$$(y + 4)/3 = (3 - y)/2 \quad (\text{allow one slip})$$

$$y = 1/5$$

substituting c's(1/5) into either equation M1

isolating x M1

$$x = \frac{7}{5} \quad (\text{o.e.}) \quad \text{A1}$$

Total 3 marks

12. (a) 9 km B1 1

$$(b) \cos 50 = \frac{c's(9)}{\text{distance to mast}} \quad (\text{o.e.}) \quad \text{M1}$$

$$14.0 \text{ km} \quad \text{A1} \quad 2 \quad 3$$

Alternatively:

$$PM/c's(9) = \tan 50 \quad (10.73...)$$

$$QM^2 = c's(9)^2 + c's(10.73)^2 \quad \text{M1}$$

$$14.0 \text{ km} \quad \text{A1}$$

Total 3 marks

13. (a) correct line drawn B1

both end points correctly identified
with appropriate symbols B1 2

(b) -1, 0 B1 1

3

Total 3 marks

14.	(a)	234	B1	1	
	(b)	$\frac{\Sigma \text{ of fish}}{11}$	(sum of 11 terms)	M1	
		266	A1	2	3
					Total 3 marks

15. either:

taking x out correctly as a factor
 $x(3x^2 + 2x - 1)$

M1

attempt at factorising c's trinomial quadratic
 $x(3x - 1)(x + 1)$

M1

$x(3x - 1)(x + 1)$

A1

3

or:

attempt at factorising c's trinomial cubic
 $(3x^2 - x)(x + 1)$

(o.e.) M1

taking x out correctly from their factored form
 $x(3x - 1)(x + 1)$

M1

$x(3x - 1)(x + 1)$

A1

Total 3 marks

16.	$3x^2 - 2 - \frac{1}{x^2}$	(at least 2 terms correct)	M1
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	$3 \times 2^2 - 2 - \frac{1}{2^2}$	(subs $x = 2$)	M1 dep
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	9.75	(o.e.)	A1
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3
Total 3 marks

17.	(a)	4, 10	B1	1
	(b)	2	B1	1
	(c)	9, 15	B1	1

3
Total 3 marks

18. $OA = OB = \sqrt{\frac{10^2}{2}}$ (7.1...) (o.e.) B1
- either $\frac{90}{360} \times \pi \times c's(7.1..)^2$ or $\frac{1}{2} \times c's(7.1)^2$ M1
- difference between c's two areas M1 dep
- 14.3 cm² A1
- 4
Total 4 marks
-
19. $375 = \frac{k}{2^2}$ M1
- $k = 2^2 \times 375$ (1500) (o.e.) M1 dep
- c's(k) $\div 5^2$ (o.e.) M1 dep
- 60 A1
- 4
Total 4 marks
-
20. (a) one correctly identified pair of angles equal with reason B1
- a second correctly identified pair of angles equal with reason and conclusion B1 2
- e.g.
- $\angle AED = \angle BEC$ vertically opposite $\angle$ s,
 $\angle DAC = \angle DBC$ $\angle$ s in same segment
- (b) $\frac{AE}{BE} = \frac{AD}{BC}$ M1
- $AE \times BC = BE \times AD$ A1 2
- 4
Total 4 marks

21. Either:

removing denominators correctly

$$(a - x) ay = a(x + ay) + a - x \quad \text{M1}$$

expanding terms (one sign error allowed)

$$a^2 y - axy = ax + a^2 y + a - x \quad \text{M1}$$

collecting terms (one sign error allowed)

$$x - ax - axy = a \quad (\text{o.e.}) \quad \text{M1}$$

$$x = \frac{a}{1 - a - ay}$$

(o.e.) A1

4

or:

$$\frac{x + ay}{a - x} = y - \frac{1}{a}$$

expanding terms (one sign error allowed)

$$x + ay = ay - xy - 1 + \frac{x}{a} \quad \text{M1}$$

collecting terms (one sign error allowed)

$$x + xy - \frac{x}{a} = -1 \quad \text{M1}$$

removing denominator correctly

$$ax + axy - x = -a \quad (\text{o.e.}) \quad \text{M1}$$

$$x = \frac{a}{1 - a - ay}$$

(o.e.) A1

Total 4 marks

22. (a) either:

$$18 + n(B) - 7 = 27 \quad (\text{o.e.})$$

or:

$$n(B \cap (A \cup C)') = 5 \quad (\text{seen}) \quad \text{M1}$$

$$n(B) = 16 \quad \text{A1} \quad 2$$

(b) either:

$$n(A \cap B') = 11 \text{ and } n(C \cap B') = 21 - c's(5)$$

or:

$$32 + 27 - c's(a) \quad (\text{o.e.}) \quad \text{M1}$$

$$43 \quad \text{A1} \quad 2$$

4
Total 4 marks

23. $\sqrt{20^2 - 12^2} \quad (= 16) \quad \text{M1}$

$$\pi \times 12^2 \times c's(16) \text{ or } \frac{1}{3} \times \pi \times 12^2 \times c's(16) \quad \text{M1}$$

$$\pi \times 12^2 \times "16" - \frac{1}{3} \times \pi \times 12^2 \times "16" \quad \text{M1 dep}$$

$$4830, 4820 \text{ (using } \pi = 3.14) \quad \text{A1}$$

4
Total 4 marks

24. $-10x^2 + 13x = -3 \quad \text{M1}$

$$10x^2 - 13x - 3 (= 0) \quad \text{A1}$$

attempt at solving a trinomial quadratic
($2x - 3$) ($5x + 1$) (= 0) M1

$$\frac{3}{2}, -\frac{1}{5} \quad (\text{o.e.}) \quad \text{A1, A1}$$

5
Total 5 marks

25.	(a)	12%	B1	1	
	(b)	either:			
		22	B1		
		(total weight =) $25 + 2x$	B1		
		$\frac{\text{any numerical value}}{25 + 2x} = \frac{2}{3}$	M1		
		4 kg	A1	4	5
		or:			
		33	B1		
		(total weight =) $25 + 2x$	B1		
		$25 + 2x = 33$	M1		
		4 kg	A1		
					Total 5 marks
26.	(a)	$ AB = \sqrt{3^2 + 3^2}$	M1		
		$k = 18$	A1	2	
	(b)	Correct use of Pythag. on at least one side	M1		
		Correct Pythag. method to find all 3 sides	M1 dep		
		conclusion correctly obtained	A1	3	
					5
		Alternatively:			
		Gradient of $OA = 1$	M1		
		Gradient of $AB = -1$	M1 dep		
		Gradient of $OA \times$ gradient of $AB = -1$			
		So OA is perpendicular to AB	A1		
					Total 5 marks

27.	correctly substituting			
	$\frac{3+x}{3-x} = \frac{x+4}{x-4}$	M1		
	removing the denominator			
	$(3+x)(x-4) = (x+4)(3-x)$	M1 dep		
	Expanding, allowing one slip max.			
	$x^2 - x - 12 = -x^2 - x + 12$	(o.e.) M1 dep		
	$2x^2 - 24 (= 0)$	A1		
	3.46, -3.46 (or equivalent surd form)	A1, A1		
			6	
			Total 6 marks	
28.	(a) no gaps and class boundaries correct	B1		
	1 correctly drawn height	B1		
	2 correctly drawn heights	B1		
	all correct	B1	4	
	$(0.9, 1.4, 2.3, 1.7 \pm \frac{1}{2} \text{ small square})$			
	(b) $10 \times c's(0.9) + 10 \times c's(1.4)$	(o.e.) M1		
	23 goals	A1	2	
			6	
			Total 6 marks	

29. (a) $\sin \angle EAD = \frac{3}{10}$ (o.e.) M1

Alternatively:

Using Pythagoras and then

$\tan \angle EAD = 3/\sqrt{c's(91)}$

$\angle EAD = 17.5^\circ$ A1 2

(b) $AD = \sqrt{10^2 - 3^2}$ (= 9.5394) M1

$\tan(20 + c's(\angle EAD)) = \frac{BD}{c's(AD)}$ M1 dep

$BD = 7.30, 7.31, 7.32$ A1 3

(c) $\Delta ABC = \frac{1}{2} \times (2 \times c's(AD)) \times c's(BD)$ (o.e.) M1

$\Delta ABC = 69.5 \rightarrow 69.8 \text{ cm}^2$ A1 2

7
Total 7 marks