

POSSIBLE ANSWERS

FEB / MARCH 2007

MATHEMATICS/P2/SG

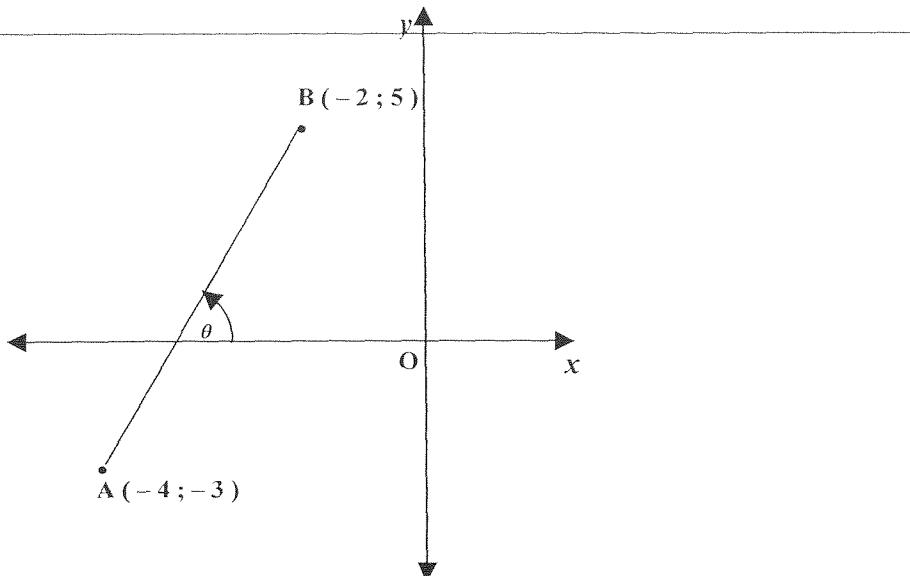
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Marking Guideline.

SENIOR CERTIFICATE EXAMINATION –Feb/Mar 2007

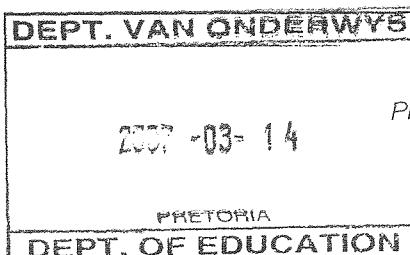
QUESTION 1

[23]



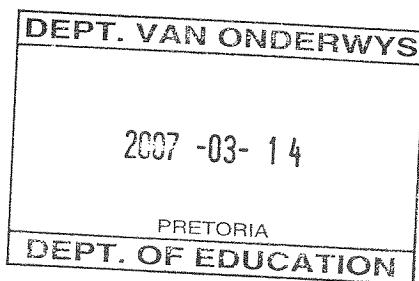
1.1	$AB = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \quad \checkmark_M$ $= \sqrt{(-2 + 4)^2 + (5 + 3)^2} \quad \checkmark_A$ $= \sqrt{68} \quad \text{OR} \quad 2\sqrt{17} \quad \checkmark_{CA}$	(3)	1 M distance formula 1 A substitution 1 CA solution
1.2	$m_{AB} = \frac{y_2 - y_1}{x_2 - x_1} \quad \checkmark_M$ $= \frac{5 + 3}{-2 + 4} \quad \checkmark_A$ $= 4 \quad \checkmark_{CA}$	(3)	1 M gradient formula 1 A substitution 1 CA solution
1.3	$\tan \theta = 4 \quad \checkmark_M$ $\theta = 76,0^\circ \quad \checkmark_{CA}$	(2)	1 M inclination formula 1 CA solution
1.4	$M \left(\frac{x_1 + x_2}{2}; \frac{y_1 + y_2}{2} \right) \quad \checkmark_M$ $= M \left(\frac{-4 + (-2)}{2}; \frac{-3 + 5}{2} \right) \checkmark_A$ $= M (-3; 1) \quad \checkmark_{CA}$	(3)	1 M midpoint formula 1 A substitution 1 CA solution

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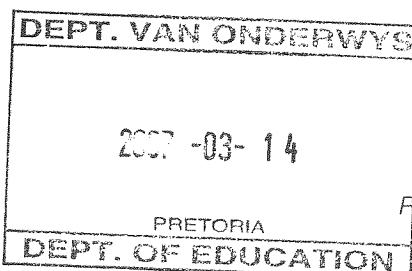


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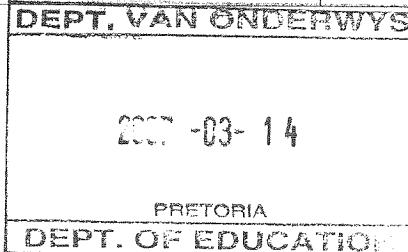
1.5	$m_{\text{line}} = \frac{-1}{m_{AB}} = -\frac{1}{4} \quad \checkmark M$ Eq. of line is $y - y_1 = m(x - x_1) \quad \checkmark M$ $y - 1 = -\frac{1}{4}(x + 3) \quad \checkmark CA$ $y = -\frac{1}{4}x - \frac{3}{4} + 1$ $= -\frac{1}{4}x + \frac{1}{4} \quad \checkmark CA$	1M \perp gradient 1M equation of line formula 1 CA substitution (4)
1.6	For D, $y = 0$, $0 = -\frac{1}{4}x + \frac{1}{4}$ $x = 1 \quad \checkmark CA$ $D(1; 0)$	1A y-value D 1CA x-value of D (2)
1.7	$m_{BD} = \frac{5 - 0}{-2 - 1} = -\frac{5}{3} \quad \checkmark CA$ $m_{BC} = \frac{10 - 5}{p + 2} \quad \checkmark CA$ $= \frac{5}{p + 2} \quad \checkmark CA$ $\therefore m_{BC} = m_{BD} \quad \checkmark M$ $\therefore \frac{5}{p + 2} = -\frac{5}{3} \quad \checkmark CA$ $p + 2 = -3$ $p = -5 \quad \checkmark CA$	1 CA solution 1 CA substitution 1 CA solution 1 M = gradients 1 CA substitution (6) 1 CA solution



Question 2		[21]
2.1.1	$x^2 + y^2 = r^2 \quad \checkmark M$ $(-2)^2 + (3)^2 = r^2 \quad \checkmark A$ $13 = r^2 \quad \checkmark CA$ $x^2 + y^2 = 13 \quad (3)$	1M equation of circle formula 1 A substitution 1 CA solution
2.1.2	$x^2 + y^2 = r^2$ $(-3)^2 + (-4)^2 = r^2 \quad \checkmark A$ $25 = r^2 \quad \checkmark CA$ $25 > 13 \quad \checkmark CA$ $\therefore C \text{ lies outside the circle.} \quad (3)$	1 A Pythagoras 1 CA solution 1 CA conclusion
2.1.3	$TR = 2(OP) \quad \checkmark M$ $= 2\sqrt{13} \quad \checkmark CA$ <p style="text-align: center;">OR</p> $OP = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ $= \sqrt{(-2)^2 + (3)^2} \quad \checkmark M$ $= \sqrt{13}$ $\therefore TR = 2\sqrt{13} \quad \checkmark CA \quad (2)$	1 method 1 CA solution 1 Method 1 CA solution



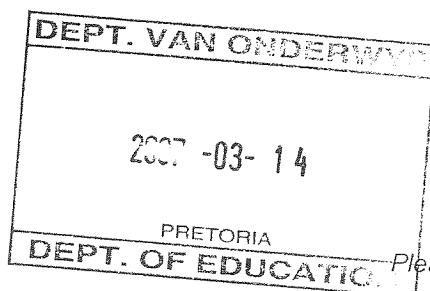
2.1.4	$m_{TR} = \frac{-3 - 0}{2 - 0} \quad \checkmark A$ $= -\frac{3}{2} \quad \checkmark CA$ $y\text{-int.} = 0 \quad \checkmark A$ $y = mx + c$ $\therefore y = -\frac{3}{2}x \quad \checkmark CA$ OR $m_{TR} = \frac{-3 - 0}{2 - 0} \quad \checkmark A$ $= -\frac{3}{2} \quad \checkmark CA$ Eq. of TR is $y - 0 = -\frac{3}{2}(x - 0) \quad \checkmark CA$ $y = -\frac{3}{2}x \quad \checkmark CA \quad (4)$	1 Asubstitution into gradient formula 1 CA m of PR 1 A y-int. = 0 1 CA solution 1 A substitution into gradient formula 1 CA m of PR 1 CA for sub. into st.line formula 1 CA solution
2.1.5	$m_{tan} = \frac{2}{3} \quad \checkmark CA \quad (1)$	1 CA gradient of tang.
2.1.6	Eq. of the tangent is $y - y_1 = m(x - x_1) \quad \checkmark M$ $y - 3 = \frac{2}{3}(x + 2) \quad \checkmark CA$ $3y = 2x + 13 \quad \checkmark CA \quad (3)$	1 M equation of line 1 CA substitution 1 CA solution
2.2	$m_{PA} = \frac{y - 6}{x + 2} \quad \checkmark A$ $m_{PB} = \frac{y - 3}{x + 4} \quad \checkmark A$ $\frac{y - 6}{x + 2} = 2 \left(\frac{y - 3}{x + 4} \right) \quad \checkmark M$ $(y - 6)(x + 4) = 2(y - 3)(x + 2) \quad \checkmark CA$ $xy + 4y - 6x - 24 = 2xy + 4y - 6x - 12$ $xy = -12 \quad \checkmark CA \quad (5)$	



QUESTION 3

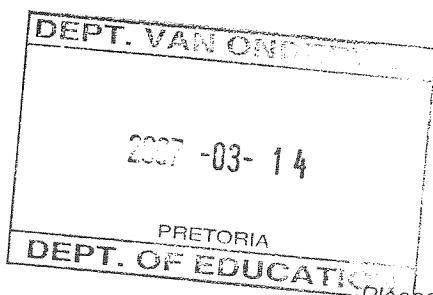
[17]

3.1.1	$\sin 2x + \sec y = \sin 2(155^\circ) + \sec 130^\circ \checkmark M$ $= -2,32 \checkmark A$ (2)	1 M substitution 2 A solution
3.1.2	$\tan^2(x-y) = \tan^2(155^\circ - 130^\circ) \checkmark M$ $= \tan^2 25^\circ$ $= 0,22 \checkmark A$ (2)	1 M substitution 1 A solution
3.2.1	$\sin \theta = -\frac{5}{13} \checkmark M$ $x^2 + y^2 = r^2$ $x^2 + (-5)^2 = 13^2 \checkmark M$ $\therefore x^2 = 144 \checkmark CA$ $x = -12 \checkmark CA$ $\cot \theta + \operatorname{cosec} \theta = \frac{-12}{-5} + \frac{13 \checkmark CA}{-5} \quad \text{OR} \quad \frac{\cos \theta}{\sin \theta} + \frac{1}{\sin \theta}$ $= \frac{12 - 13}{5} = \frac{\cos \theta + 1}{\sin \theta}$ $= -\frac{1}{5} \checkmark CA = \frac{1 + \frac{-12 \checkmark CA}{13}}{\frac{-5 \checkmark CA}{13}}$ $= -\frac{1}{5} \checkmark CA$ (7)	1 M $\sin \theta$ 1 A correct quadrant 1 M Pythagoras 1 CA value of x 1 CA $\cot \theta$ 1 CA $\sec \theta$ 1 CA solution

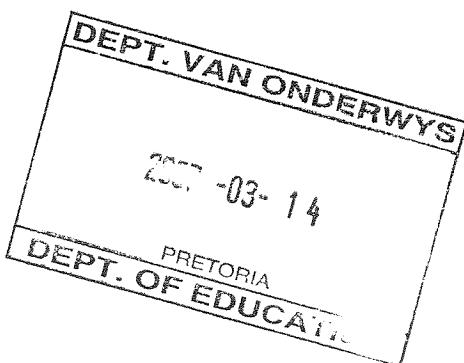


3.2.2	$ \begin{aligned} & \frac{\sin(180^\circ - x) \cdot \sec(90^\circ - x) \cdot \cos 240^\circ}{\tan(360^\circ - x)} \\ &= \frac{\sin x \cdot \operatorname{cosec} x \cdot -\cos 60^\circ}{-\tan x} \\ &= \frac{\sqrt{A} \quad \sqrt{A} \quad 1}{\sin x \cdot \operatorname{cosec} x \cdot -\frac{1}{2}} \quad \checkmark A \\ &= \frac{-\tan x}{\sqrt{A}} \\ &= \frac{\sin x \cdot \frac{1}{\sin x}}{2 \cdot \tan x} \quad \checkmark CA \\ &= \frac{1}{2 \tan x} \quad \text{or} \quad \frac{\cot x}{2} \quad \checkmark CA \end{aligned} $ (6)	4 A reduction/special angle 1 CA identity 1 CA solution
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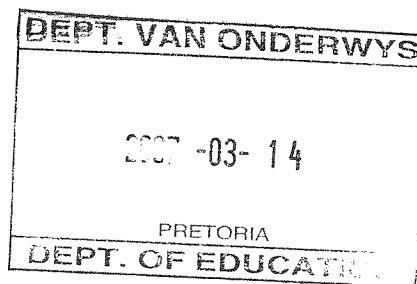
QUESTION 4		[12]
4.1	$m = 2$; $p = 1$; $k = \sin 30^\circ \checkmark M$ $k = 0,86 \checkmark A$	(4) 1 A value of a 1 A value of b 1M 1A for value of k
4.2	$360^\circ \checkmark A$	(1) 1 A
4.3	$C(90^\circ; 0) \checkmark A$	(1) 1 A solution
4.4	$\checkmark A \quad \checkmark A$ $(150^\circ; -0,86)$ or $(150^\circ; -\frac{\sqrt{3}}{2})$	(2) 1A for x value 1A for y value
4.5.1	$(90^\circ; 180^\circ) \checkmark A \checkmark A \checkmark M$	(3) 2A for end values 1M for correct interval
4.5.2	$180^\circ \checkmark A$	(1) 1A

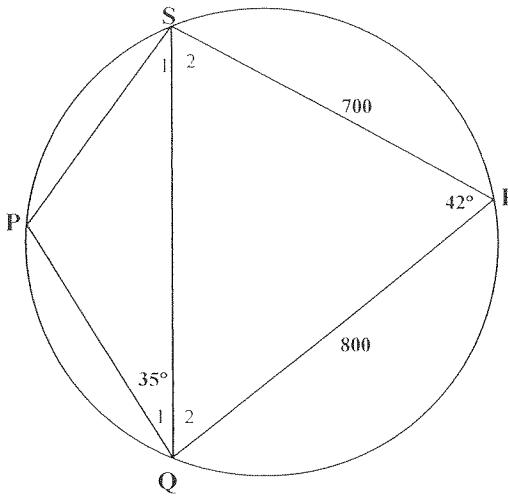


Question 5		[9]
5.1	<p>LHS: $\tan x \cdot \cot x = \frac{\sin x}{\cosec x}$</p> <p style="text-align: center;">✓A</p> $= \tan x \frac{1}{\tan x} - \frac{\sin x}{\frac{1}{\sin x}} \checkmark A$ $= 1 - \sin^2 x \checkmark CA$ $= \cos^2 x \checkmark CA$ $= RHS$ <p style="text-align: center;">OR</p> <p>LHS: $\tan x \cdot \cot x = \frac{\sin x}{\cosec x}$</p> $= \frac{\sin x}{\cos x} \left(\frac{\cos x}{\sin x} \right) - \frac{\sin x}{\frac{1}{\sin x}} \checkmark CA$ $= 1 - \sin^2 x \checkmark CA$ $= \cos^2 x \checkmark CA$ $= RHS \quad (4)$	<p>2 A identity</p> <p>2 CA simplification</p> <p>1 CA identity</p>
5.2	$2 \tan \theta = -3,2$ $\tan \theta = -1,6 \quad \checkmark A$ <p>R.A. $= 58^\circ \quad \checkmark CA$</p> $\theta = 180^\circ - 58^\circ \checkmark M \quad \text{or} \quad \theta = 360^\circ - 58^\circ$ $= 122^\circ \quad \text{or} \quad \theta = 302^\circ \checkmark CA \quad (5)$	<p>1A</p> <p>1CA reference angle</p> <p>1 M / 1 CA quadrants</p> <p>1CA solutions</p>



QUESTION 6		[17]
6.1	<p>Area of $\Delta ABC = \frac{1}{2}$ base X height $\checkmark M$</p> $= \frac{1}{2} \cdot c \cdot b \sin A \quad \checkmark A$ $= \frac{1}{2} (b)(c) \sin A$	<p>1M formula</p> <p>1A substitution</p> <p>(4)</p>
	<p>OR</p> <p>Constr: Draw $CD \perp AB$</p> $h = b \sin A \quad \checkmark A$ <p>Area of $\Delta ABC = \frac{1}{2}$ base X height $\checkmark M$ 1M formula</p> $= \frac{1}{2} (c) (h)$ $= \frac{1}{2} \cdot c \cdot b \sin A \quad \checkmark A$ $= \frac{1}{2} (b)(c) \sin A$	



6.2		
6.2.1	$\text{Area of } \triangle QRS = \frac{1}{2} \cdot QR \cdot RS \cdot \sin R \quad \checkmark M$ $= \frac{1}{2} \times 800 \times 700 \times \sin 42^\circ \quad \checkmark CA$ $= 187\ 356,6 \text{ m}^2 \quad \checkmark CA$ (3)	1M area rule 1A substitution 1 CA solution
6.2.2	$\text{In } \triangle QSR$ $QS^2 = SR^2 + QR^2 - 2(SR)(QR) \cos R \quad \checkmark M$ $= (700)^2 + (800)^2 - 2(700)(800) \cos 42^\circ \quad \checkmark A$ $= 297\ 677,7955.. \quad \checkmark CA$ $QS = 545,6 \text{ m} \quad \checkmark CA$ (4)	
6.2.3	$\hat{P} = 180^\circ - 42^\circ \quad \checkmark R$ $= 138^\circ \quad \checkmark A (\text{opp. } \angle's \text{ cyclic. quad. supp})$ (2)	
6.2.4	$\frac{PS}{\sin Q_1} = \frac{QS}{\sin P} \quad \checkmark M$ $\frac{PS}{\sin 35^\circ} = \frac{545,6}{\sin 138^\circ} \quad \checkmark CA$ $\therefore PS = \frac{\sin 35^\circ (545,6)}{\sin 138^\circ} \quad \checkmark CA$ $= 467,7 \text{ m} \quad \checkmark CA$ (4)	1M sine rule 1 CA substitution 1M manipulation 1 CA solution

DEPT. VAN ONDERWYS

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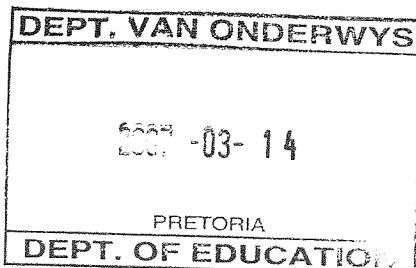
EDUCATION

Question 7

[18]

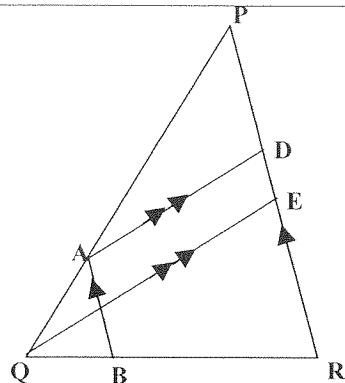
7.1	<p>Const: Join CO and extend to D ✓ construction</p> <p>Proof: ✓S/R</p> <p>In $\triangle ACO$, $\hat{O}_1 = \hat{A} + \hat{C}_1$ (ext. \angle of a \triangle) $AO = OC$ (= radii)</p> <p>but $\hat{A} = \hat{C}_1$ (\angle's opp = s's) $\therefore \hat{O}_1 = 2\hat{C}_1$ ✓S</p> <p>similarly $\hat{O}_2 = 2\hat{C}_2$ ✓S</p> <p>$\therefore \hat{O}_1 + \hat{O}_2 = 2\hat{C}_1 + 2\hat{C}_2$ ✓S $= 2(\hat{C}_1 + \hat{C}_2)$ $\therefore \hat{AOB} = 2\hat{ACB}$</p> <p>(6)</p>	
7.2		
7.2.1(a)	$\hat{O}_3 = 70^\circ$ ✓S $\therefore \hat{A}_2 = 35^\circ$ ✓S (angle at the centre = 2. angle at cir)	DEPT. VAN ONDERWYS 2007 -03- 14 PRETORIA Please turn over DEPT. OF EDUCATION

<p>7.2.1 (b)</p> <p>$\hat{P}_2 + \hat{P}_3 = 90^\circ \quad \checkmark S \quad (\angle s \text{ in a semi-circle})$</p> <p>$\therefore \hat{P}_1 = 90^\circ \quad (\text{adj. } \angle \text{s on a st.line})$</p> <p>OR</p>	<p>$\hat{O}_3 = 70^\circ \quad \checkmark S/R \quad (\text{adj. supp. } \angle \text{'s})$</p> <p>$\hat{P}_3 = \frac{110^\circ}{2} = 55^\circ \quad \checkmark S/R \quad (\text{sum of } \angle \text{s in a } \Delta)$</p> <p>$\hat{P}_1 = \hat{A}_2 \quad (\angle \text{'s opp. == s's})$</p> <p>$\therefore \hat{P}_1 = 90^\circ \quad \checkmark S/R \quad (\text{adj. supp } \angle \text{'s})$</p>
<p>7.2.2</p> <p>$\hat{O}_1 = 90^\circ \quad (\text{given})$</p> <p>$\hat{P}_1 = 90^\circ \quad (\text{proved}) \quad \checkmark S/R$</p> <p>$\therefore \text{AOPM is cyclic } (= \angle \text{s sub. by same line segment})$</p> <p>OR</p> <p>$\therefore \hat{M}_1 = 180^\circ - (90^\circ + 55^\circ) \quad (\angle \text{'s in a } \Delta)$ $= 35^\circ \quad \checkmark S/R$</p> <p>$\therefore \hat{A}_2 = \hat{M}_1 \quad (= 35^\circ) \quad \checkmark R$</p> <p>$\therefore \text{AOPM is cyclic } (= \angle \text{sub. by same line segm.})$</p>	
<p>7.2.3</p> <p>$\hat{M}_1 = 35^\circ \quad \checkmark S \quad (\angle \text{'s in same segm.})$</p>	
<p>7.2.4</p> <p>PBOL is cyclic quad. $\checkmark S$</p> <p>$\hat{P}_1 = \hat{O}_2 + \hat{O}_3 = 90^\circ \quad \checkmark R$</p> <p>OR</p> <p>ext. $\angle =$ int.opp. $\angle \quad \checkmark R$</p> <p>OR</p> <p>$\hat{O}_1 = \hat{P}_2 + \hat{P}_3 = 90^\circ \quad \checkmark R$</p>	



Question 8

[7]

8.1 In $\triangle PQR$, $AB \parallel PR$

$$\frac{QB}{QR} = \frac{2}{7} \quad (\text{line } \parallel \text{ to one side of a } \triangle) \quad (2)$$

8.2 In $\triangle PQE$, $AD \parallel QE$

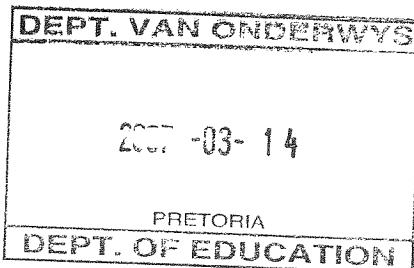
$$\frac{PD}{DE} = \frac{PA}{AQ} \quad (\text{line } \parallel \text{ to one side of a } \triangle)$$

$$= \frac{5}{2} = \frac{5y}{2y} \quad (\text{given}) \quad \checkmark S$$

$$ER = PE = 7y \quad (\text{given}) \quad \checkmark S$$

$$\frac{DE}{PR} = \frac{2y}{7y+7y} \quad \checkmark A$$

$$= \frac{1}{7} \quad \checkmark A \quad (5)$$



Question 9

[26]

9.1

Const: Mark a point D on KL such that $KD = PQ$ and \sqrt{M}
 E is a point on KM such that $KE = PR$. Join DE.

Proof: $\triangle KDE \cong \triangle PQR$ (SAS) $\checkmark S/R$

$$\therefore \hat{D}_1 = \hat{Q} \quad \checkmark S \quad (\cong)$$

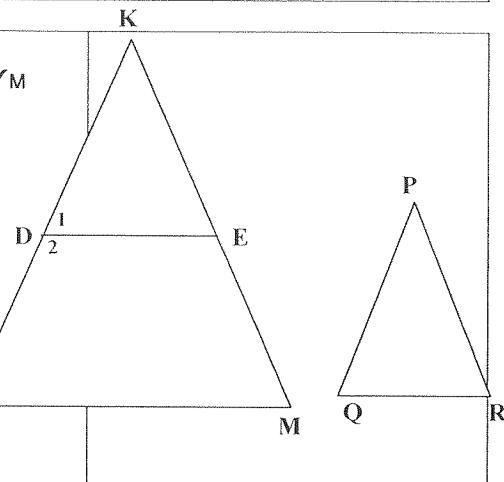
$$\text{but } \hat{Q} = \hat{L} \quad (\text{given})$$

$$\therefore \hat{D}_1 = \hat{L} \quad \checkmark S \quad \checkmark S/R$$

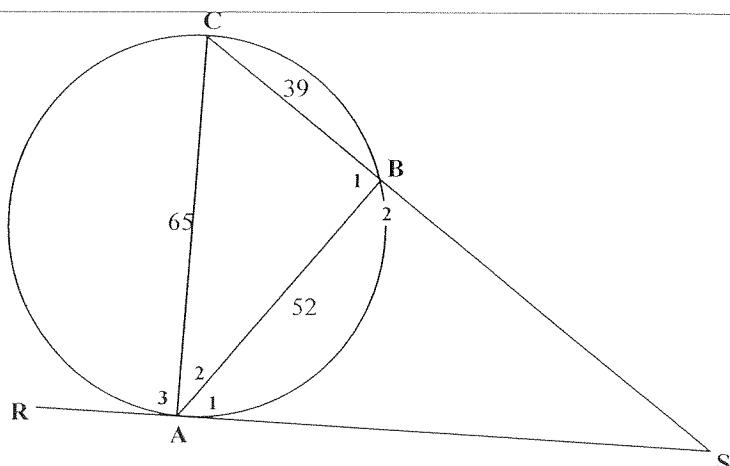
$$\therefore DE \parallel LM \quad (\text{corr. } \angle s =)$$

$$\frac{KL}{KD} = \frac{KM}{KE} \quad \checkmark S \quad (\text{line } \parallel \text{ to one side of a } \Delta)$$

$$\frac{KL}{PQ} = \frac{KM}{PR} \quad (\text{Const.})$$



(7)

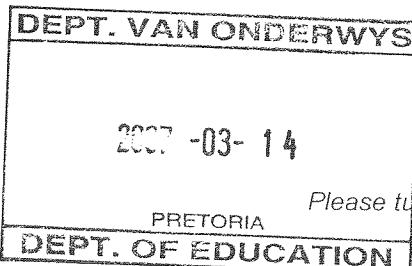
9.2.1
(a)

$$AC^2 = 65^2 = 4225 \quad \checkmark S$$

$$AB^2 + BC^2 = 52^2 + 39^2$$

$$= 4225 = AC^2 \quad \checkmark S$$

$$\therefore \hat{B}_1 = 90^\circ \quad (\text{converse of Pythagoras}) \quad (3)$$



9.2.1 (b)	<p>\checkmark_S \checkmark_R</p> <p>AC is the diameter of circle ABC (conv. \angle in semi-circle)</p> <p>$\therefore \hat{C} \hat{A} \hat{S} = 90^\circ \checkmark_S$ ($\tan \perp$ diameter)</p> <p>\checkmark_R</p> <p>$\therefore CS$ is a diameter of circle through ACB (conv. \angle in semi-circle) (5)</p>	
9.2.1 (c)	<p>In ΔBCA and ΔBAS</p> <p>$\hat{C} = \hat{A}_1 \checkmark_S$ \checkmark_R (tan-chord)</p> <p>$\hat{B}_1 = \hat{B}_2 = 90^\circ \checkmark_S$ (proved)</p> <p>$\hat{A} = \hat{S}$ \checkmark_R (sum of the \angles of a Δ)</p> <p>$\Delta BAS \parallel \Delta BCA$ ($\angle \angle \angle$) (4)</p>	
9.2.2	<p>$\frac{BS}{BA} = \frac{BA}{BC} \checkmark_S$ ($\angle \angle \angle$) \checkmark_R</p> <p>$\frac{BS}{52} = \frac{52}{39} \checkmark_A$</p> <p>$\therefore BS = \frac{52 \cdot 52}{39} = 69,3 \checkmark_{CA}$ (4)</p>	

9.2.3

In ΔABC , $\cos C = \frac{BC}{AC} \checkmark_S$

In ΔACS , $\cos C = \frac{AC}{SC} \checkmark_S$

$\cos C \cdot \cos C = \frac{BC}{AC} \cdot \frac{AC}{SC} = \frac{BC}{SC} \checkmark_S$

OR LHS: $\cos^2 C = \left(\frac{AC}{CS}\right)^2 \checkmark_S$ OR $\left(\frac{39}{65}\right)^2$

$= \left(\frac{65}{39 + 69,3}\right)^2 = 0,36 \checkmark_S$

RHS: $\frac{BC}{SC} = \frac{39}{39 + 69,3} = 0,36 = \text{LHS}$ (3)

