

POSSIBLE ANSWERS

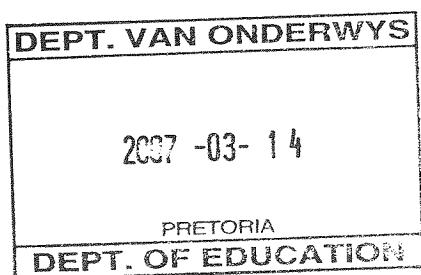
FEB / MARCH 2007

MATHEMATICS/P2/HG

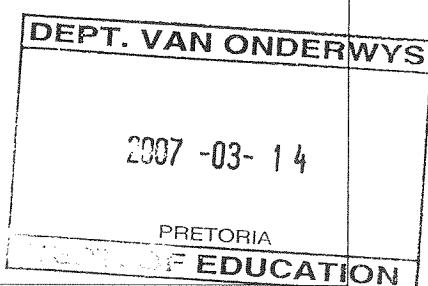
Marking Guideline/
SENIOR CERTIFICATE EXAMINATION – Feb/Mar 2007

QUESTION 1 [25]		
1.1	$m_{PQ} = \frac{9 - 12}{9 + 9} = -\frac{1}{6}$ ✓ M ✓ A	(2) gradient form & subst
1.2	$m_{PQ} = -\frac{1}{6}$ $\tan \beta = -\frac{1}{6}$ $\beta = 170,54^\circ$ ✓ A $m_{RQ} = \frac{3}{2}$ $\tan \alpha = \frac{3}{2}$ $\alpha = 56,31^\circ$ ✓ A $\hat{Q}_2 = 170,54^\circ - 56,31^\circ$ $= 114,23^\circ$ ✓ A $\hat{Q}_1 = 180^\circ - 114,23^\circ$ $= 65,77^\circ$ ✓ A	Correct angle Inclination correct angle correct angle correct angle correct angle
1.3	$M \left(\frac{-3 + 9}{2}; \frac{-9 + 9}{2} \right)$ ✓ M $M(3; 0)$ ✓ A	<div style="border: 1px solid black; padding: 5px; text-align: center;"> DEPT. VAN ONDERWYS 2007-03-14 PRETORIA DEPT. OF EDUCATION </div> (2) correct formula simplification
1.4	$m_{PM} = \frac{12 - 0}{-9 - 3} = -1$ ✓ M $y - y_1 = m(x - x_1)$ OR $y - 0 = -1(x - 3)$ ✓ M $y = -x + 3$ ✓ A	Correct formula Gradient of PM Substitution into any line formula Equation of line

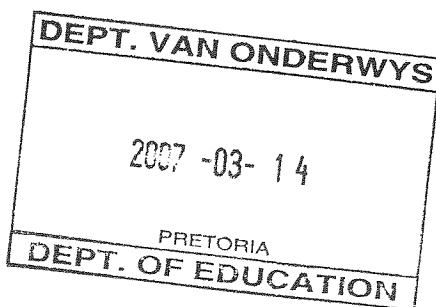
1.5	<p>$N(a; b)$</p> $b = -a + 3 \quad \checkmark M \text{ Eq.1}$ $\checkmark A \qquad QN = 5\sqrt{5} \quad \checkmark M$ $(a-9)^2 + (b-9)^2 = (5\sqrt{5})^2 \quad \dots \text{Eq. 2}$ <p>substitute Eq. 1 into Eq. 2</p> $(a-9)^2 + (-a-6)^2 = 125 \quad \checkmark CA$ $a^2 - 18a + 81 + a^2 + 12a + 36 - 125 = 0 \quad \checkmark CA \quad \checkmark CA$ $2a^2 - 6a - 8 = 0 \quad \checkmark CA$ $2(a-4)(a+1) = 0 \quad \checkmark M$ $a = -1 \quad \checkmark CA$ $b = -(-1) + 3 = 4 \quad \checkmark CA$ $N(-1; 4) \quad (10)$	<p>subst. in equation of line</p> <p>Use of distance formula & equating</p> <p>Correct substitution</p> <p>simplification</p> <p>simplification</p> <p>factorizing</p> <p>value of a</p> <p>value of b</p>
1.6	$x = -1 \quad \checkmark CA \quad \checkmark M$ <p>OR</p> $x = a \quad \checkmark CA \quad \checkmark M$	(2) Form



QUESTION 2 [25]		
2.1		
2.1.1	<p>If Q(3;-1)</p> $\begin{aligned} d(QB) &= \sqrt{(3-3)^2 + (-1-4)^2} && \checkmark M \\ &= 5 && \checkmark A \end{aligned}$ $\begin{aligned} d(QA) &= \sqrt{(3-7)^2 + (-1-2)^2} && \checkmark M \\ &= 5 && \checkmark A \end{aligned}$ <p style="text-align: center;">$\checkmark CA$</p> <p>$\therefore (3;-1)$ is the centre since radii are equal or $QB = QA$</p> <p style="text-align: center;">OR</p> <p>Centre $(a; b)$</p> $\therefore (3-a)^2 + (4-b)^2 = r^2 \checkmark A$ <p>and $(7-a)^2 + (2-b)^2 = r^2 \checkmark A$</p> $\begin{aligned} 9 - 6a + a^2 + 16 - 8b + b^2 &= r^2 && \dots\dots \text{Eq. 1} \\ 49 - 14a + a^2 + 4 - 4b + b^2 &= r^2 && \dots\dots \text{Eq. 2} \end{aligned}$ <p>Eq. 1 – Eq. 2:</p> $\begin{aligned} -40 + 8a + 12 - 4b &= 0 && \checkmark M \\ -7 + 2a &= b && \checkmark A \end{aligned}$ <p>when $a = 3$</p> $\begin{aligned} LHS - 7 + 2(3) &= -1 \\ &= b && \checkmark A \end{aligned}$ <p>$\therefore (3;-1)$ centre.</p>	<p>Substitution simplification</p> <p>substitution simplification</p> <p>conclusion</p>
2.1.2	<p>Centre $(3; -1)$</p> $\begin{aligned} r^2 &= (3-3)^2 + (-1-4)^2 && \checkmark A \\ &= 25 \end{aligned}$ <p>Equation of circle is : $(x-3)^2 + (y+1)^2 = 25$</p>	<p style="text-align: right;">(5)</p> <p>Correct value r</p> <p>Subst. into circle eq.</p> <p>Correct form</p>

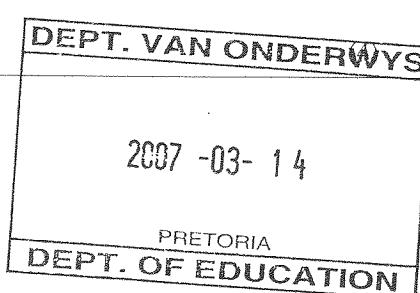


2.1.3	$m_{\text{rad}} = \frac{2 + 1}{7 - 3} = \frac{3}{4} \quad \checkmark M \quad \checkmark A$ $m_{\tan} = -\frac{4}{3} \quad \checkmark CA$ $y - 2 = -\frac{4}{3}(x - 7) \quad \checkmark M \quad \checkmark A \quad \text{OR}$ $3y = -4x + 28 + 6 \quad \text{OR}$ $3y = -4x + 34 \quad (5)$	Correct subst. and simplification Perpendicular slopes Subst. slope and point Simplification Form of straight line
2.1.4	Equation of AD : $3y = -4x + 34 \quad \checkmark CA$ \therefore Equation of BD is : $y = 4 \checkmark M$ $\therefore 3y = -4x + 34 \quad \checkmark A \checkmark M$ $\therefore 3(4) = -4x + 34 \quad \checkmark A \checkmark M$ $\therefore x = \frac{11}{2} \checkmark A$ $D\left(\frac{11}{2}; 4\right) \checkmark A$ OR $D(n; m),$ $D(n; 3) \checkmark A$ $BD^2 = DA^2 \quad \checkmark M$ $(m - 4)^2 + (n - 3)^2 = (m - 2)^2 + (n - 7)^2 \checkmark A$ $m^2 - 8m + 16 + n^2 - 6n + 9 = m^2 - 4m + 4 + n^2 - 14n + 49 \checkmark CA$ $-4m + 8n = 28$ $m - 2n = -7 \checkmark CA$ but $m = 4$ $-2n = -7 - 4$ $n = \frac{11}{2} \checkmark A$ $D\left(\frac{11}{2}; 4\right) \quad (6)$	



<p>2.2</p> $PB^2 = PO^2 + 3 \quad \checkmark M$ $\checkmark A$ $(x - x)^2 + (y - 1)^2 = x^2 + y^2 + 3 \quad \checkmark A$ $y^2 - 2y + 1 = x^2 + y^2 + 3 \quad \checkmark CA$ $-2y = x^2 + 2 \quad \checkmark CA$ <p>OR $y = -\frac{x^2}{2} - 1$</p> <p>(6)</p>	<p>Coordinates of B</p> <p>Setting up correct equation</p> <p>Substitution X 2</p> <p>Simplification</p> <p>Any form of equation</p>
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QUESTION 3		[15]	
3.1.1	$\sin 25^\circ = \sqrt{1 - \cos^2 25^\circ} \quad \checkmark M$ $= \sqrt{1 - (\sqrt{1-t^2})^2}$ $= t \quad \checkmark A$ <p>OR</p> $\sin 25^\circ = t \quad \checkmark A$		<p>Correct identity</p> <p>Substitution</p>
3.1.2	$\cot 115^\circ = -\cot 65^\circ$ $= \text{OR } -\tan 25^\circ \quad \checkmark A$ $= -\frac{t}{\sqrt{1-t^2}} \quad \checkmark CA$	(2)	<p>Use of Pythagoras</p> <p>substitution</p>
3.1.2	$\sin 50^\circ = \sin 2(25^\circ) \quad \checkmark M$ $= 2 \sin 25^\circ \cos 25^\circ \quad \checkmark A$ $= 2t \sqrt{1-t^2} \quad \checkmark CA$		<p>Reduction</p> <p>cofunction</p> <p>substitution</p>

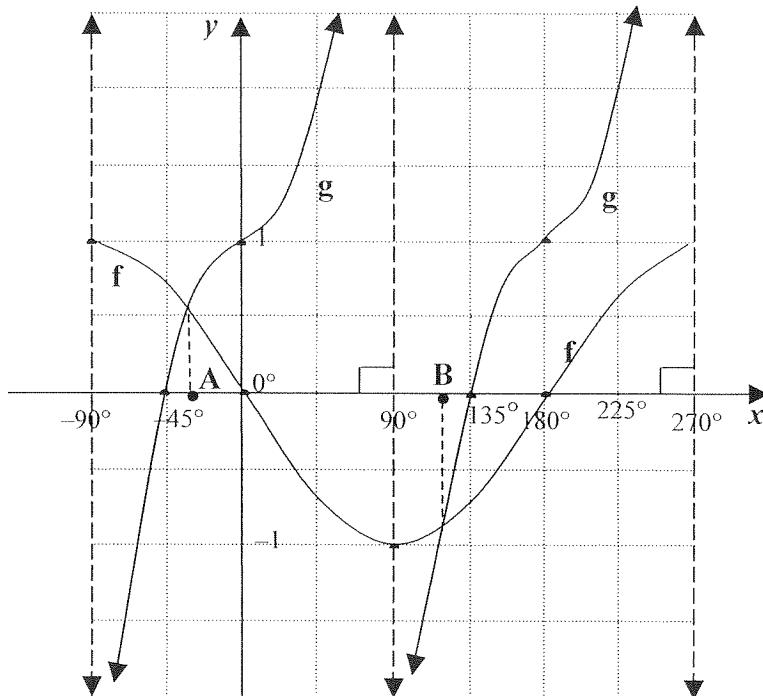


3.2	$\frac{\sin(1530^\circ - x) \sec(x - 360^\circ) \tan(x - 180^\circ)}{\sin(-x) \cos \operatorname{ec}(x - 90^\circ)}$ $= \frac{\sqrt{A} \sqrt{A} \sqrt{A}}{\cos x \cdot \sec(x) \cdot (\tan x)}$ $= \frac{-\sin x \cdot -\sec x}{\sqrt{A} \sqrt{A}}$ $= \frac{\cos x \cdot \sin x}{\sin x \cdot \cos x}$ $= 1 \quad \checkmark CA$	One for each correct reduction One for each correct reduction Simplification
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QUESTION 4 [18]

4.1

$$g(x) = 1 + \tan x \quad \text{and} \quad f(x) = -\sin x$$



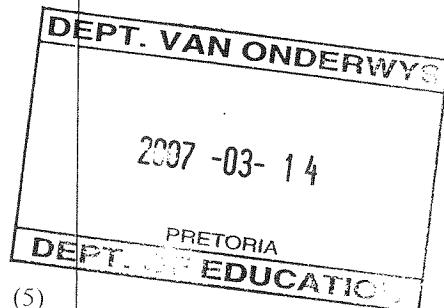
	f	g
shape	✓	✓
x-int	✓	✓
y-int	✓	✓
asym.		✓
TP Inflection	✓ ✓	

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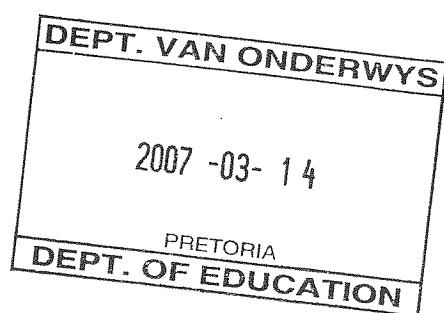
(9)

4.2.1	Indicated on graph ✓ A ✓ A ✓ M	(3)	1M use of A, B, .. One for each
4.2.2	0°; 180° ✓ A ✓ A	(2)	One for each value
4.2.3	$-90^\circ < x \leq -45^\circ ; \quad 0^\circ \leq x < 90^\circ ; \quad \text{Notation}$ $\text{OR } x \in (-90^\circ ; -45^\circ] \cup [0^\circ ; 90^\circ)$	(4)	One for each set of end points One for notation

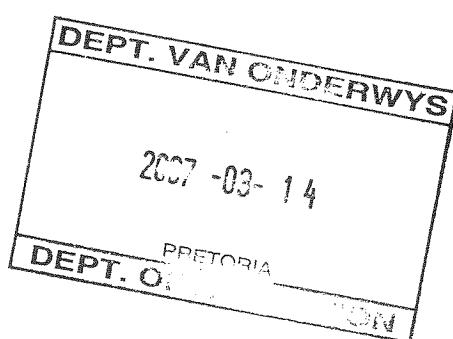
QUESTION 5		[25]
5.1	$\sin \theta = \cos \theta$ $\tan \theta = 1 \quad \checkmark A \quad \text{OR} \quad \sin \theta = \sin(90^\circ - \theta) \quad \checkmark A$ Ref Angle = $45^\circ \checkmark CA$ $2\theta = 90^\circ + k \cdot 360^\circ \checkmark CA$ $\checkmark CA \quad \checkmark A$ $\theta = 45^\circ + k \cdot 180^\circ, n \in \mathbb{Z}$ $\theta = 45^\circ + n \cdot 180^\circ \quad \checkmark CA$ $\theta = 45^\circ + n \cdot 180^\circ, n \in \mathbb{Z} \quad \checkmark A$	Identity Ref. \angle General form and $n \in \mathbb{Z}$ (4)
5.2	$\cos \theta = m + 1$ $-1 \leq m + 1 \leq 1 \quad \checkmark M$ $-2 \leq m \leq 0 \quad \checkmark A$	Correct interval Simplification (2)
5.3.1	LHS: $\sin 3\theta = \sin(2\theta + \theta) \checkmark M$ $= \sin 2\theta \cos \theta + \cos 2\theta \sin \theta \checkmark M$ $\checkmark A \quad \checkmark A$ $= 2\sin \theta \cos \theta \cdot \cos \theta + (1 - 2\sin^2 \theta) \sin \theta$ $= 2\sin \theta (1 - \sin^2 \theta) \checkmark A$ $= 2\sin \theta - 2\sin^3 \theta \quad \checkmark A$ $= 2\sin \theta - 2\sin^3 \theta + \sin \theta - 2\sin^3 \theta$ $= 3\sin \theta - 4\sin^3 \theta = \text{RHS}$ OR LHS: $\sin 3\theta = \sin(2\theta + \theta) \checkmark M$ $= \sin 2\theta \cos \theta + \cos 2\theta \sin \theta \checkmark M$ $\checkmark A$ $= 2\sin \theta \cos^2 \theta + \cos 2\theta \sin \theta$ $= \sin \theta(2\cos^2 \theta + \cos 2\theta)$ $= \sin \theta(2\cos^2 \theta + 2\cos^2 \theta - 1) \quad \checkmark A$ $= \sin \theta(4\cos^2 \theta - 1) \quad \checkmark A$ $= \sin \theta(4(1 - \sin^2 \theta) - 1)$ $= \sin \theta(4 - 4\sin^2 \theta - 1)$ $= 3\sin \theta - 4\sin^3 \theta = \text{RHS}$	Expanding 3θ Expansion of $\sin(2\theta + \theta)$ Expansion of $\sin 2\theta$ & $\cos 2\theta$ Expansion of $\cos^2 \theta$ (5)
5.3.2	$3\sin \theta - 4\sin^3 \theta = -\operatorname{cosec} \theta$ $3\sin \theta - 4\sin^3 \theta + \operatorname{cosec} \theta = 0 \quad \checkmark M$ $3\sin^2 \theta - 4\sin^4 \theta + 1 = 0 \quad \checkmark M$ $4\sin^4 \theta - 3\sin^2 \theta - 1 = 0$ $(4\sin^2 \theta + 1)(\sin^2 \theta - 1) = 0 \quad \checkmark A$ $\sin^2 \theta = \frac{1}{4} \quad \text{or} \quad \sin^2 \theta = -1$ $\checkmark A$	Substitution Substitution Factorizing Values of $\sin \theta$

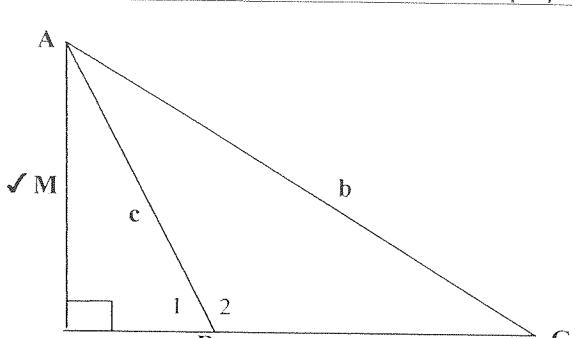
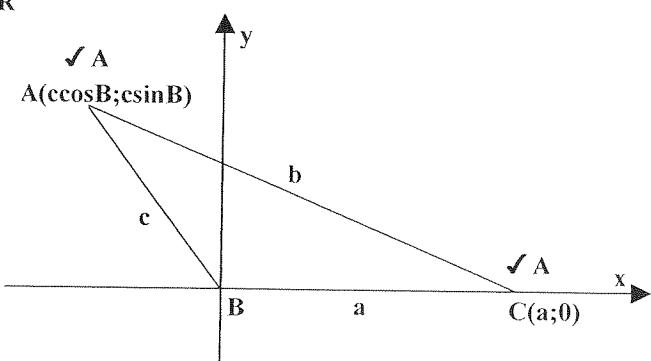


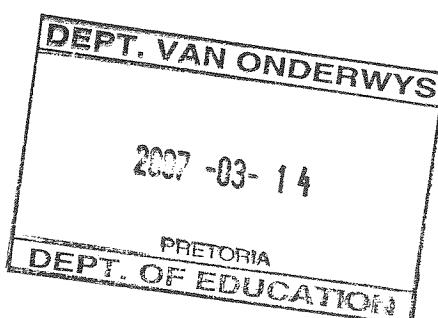
	$\sin \theta = \pm \frac{1}{2}$ or $\sin \theta = \pm 1$ $\checkmark A$ $\theta = 30^\circ$ or $\theta = 90^\circ$ ref $\angle s$ $\theta = -30^\circ; -90^\circ; -150^\circ$ $\checkmark CA$ (8)	Ref \angle Values of θ
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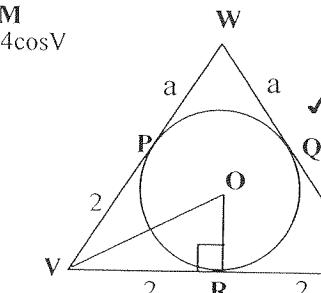


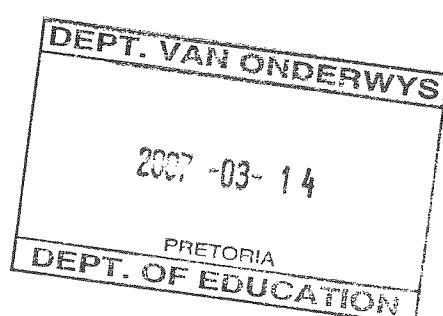
5.4	$2 \cot 2\theta \cdot \tan \theta = 2 - \sec^2 \theta$ $\text{LHS : } 2 \cot 2\theta \cdot \tan \theta = \frac{2 \cos 2\theta}{\sin 2\theta} \cdot \frac{\sin \theta}{\cos \theta} \quad \checkmark A$ $= \frac{2(2\cos^2 \theta - 1) \cdot \sin \theta}{2 \sin \theta \cdot \cos \theta \cdot \cos \theta} \quad \checkmark A$ $= \frac{(2\cos^2 \theta - 1)}{\cos^2 \theta} \quad \checkmark CA$ $= 2 - \frac{1}{\cos^2 \theta} \quad \checkmark A$ $= 2 - \sec^2 \theta$ $= \text{RHS}$ <p>OR</p> $\text{LHS : } 2 \cot 2\theta \cdot \tan \theta = \frac{2}{\tan 2\theta} \cdot \tan \theta \quad \checkmark A$ $= \frac{2}{\frac{2 \tan \theta}{1 - \tan^2 \theta}} \cdot \tan \theta \quad \checkmark A$ $= \frac{2(1 - \tan^2 \theta) \cdot \tan \theta}{2 \tan \theta} \quad \checkmark A$ $= 1 - \tan^2 \theta \quad \checkmark A$ $\text{RHS : } 2 - \sec^2 \theta = 2 - (1 + \tan^2 \theta) \quad \checkmark A$ $= 1 - \tan^2 \theta \quad \checkmark A$ $\therefore \text{LHS} = \text{RHS} \quad (6)$	2 Identities 2 Identities Simplification Identity Identity Simplification Simplification Identity Simplification Penalty 1 no conclusion.
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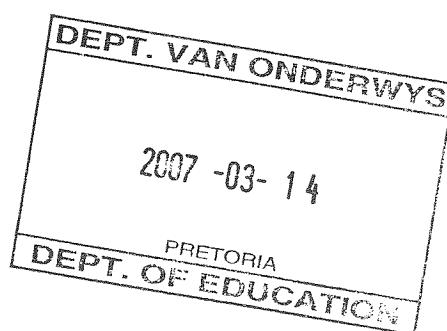
QUESTION 6		[25]
6.1		Construction
	$\begin{aligned} b^2 &= AD^2 + DC^2 \quad \checkmark M \\ &= c^2 - DB^2 + (DB + a)^2 \quad \checkmark A \\ &= c^2 - DB^2 + DB^2 + 2aDB + a^2 \\ &= a^2 + c^2 + 2aDB \quad \checkmark CA \end{aligned}$	Pythagoras expansion Simplification
	<p>But $\cos B_2 = -\cos B_1 \quad \checkmark M$</p> $= -\frac{DB}{c} \quad \checkmark A$ $DB = (-c)\cos B$ $\therefore b^2 = a^2 + c^2 - 2(a)(c)\cos B$	\cos in 2 nd quad \cos ratio
	<p>OR</p> 	Coordinates of A and C
	$\begin{aligned} b^2 &= AC^2 \\ &= (a - c \cdot \cos B)^2 + (0 - c \cdot \sin B)^2 \quad \checkmark M \\ &= a^2 - 2a \cdot c \cdot \cos B + c^2 \cdot \cos^2 B + c^2 \sin^2 B \quad \checkmark A \\ &= a^2 + c^2 (\cos^2 B + \sin^2 B) - 2a \cdot c \cdot \cos B \quad \checkmark A \\ &= a^2 + c^2 - 2a \cdot c \cdot \cos B \quad \checkmark A \end{aligned} \quad (6)$	Distance formula Expansion Grouping $\cos^2 B + \sin^2 B = 1$



6.2.1	<p>In $\triangle WVR$</p> <p>$WR \perp VR \quad \checkmark A$</p> <p>$VR = VP = 2 \checkmark A$</p> <p>$WV = WP + PV \checkmark M$</p> <p>$= a + 2 \checkmark A$</p> <p>$\cos V = \frac{VR}{VW} \checkmark M$</p> <p>$= \frac{2}{2+a} \checkmark A$</p> <p>OR</p> <p>$WT^2 = WV^2 + VT^2 - 2WV \cdot VT \cos V \checkmark M$</p> <p>$(2+a)^2 = (2+a)^2 + 4^2 - 2(2+a) \cdot 4 \cos V \checkmark A$</p> <p>$-8(2+a)\cos V = -16 \checkmark A$</p> <p>$\cos V = \frac{2}{2+a} \checkmark A$</p>  <p style="text-align: right;">(7)</p>	<p>Recognizing $WR \perp VR$</p> <p>Value of WP</p> <p>Value of VR</p> <p>Value of WV</p> <p>Substitution</p> <p>Definition of cos</p> <p>substitution</p> <p>Using cos formula</p> <p>Correct substitution</p> <p>Correct lengths on diagram</p> <p>Simplification</p> <p>Simplification</p> <p>Solution</p>
6.2.2	<p>$\cos V = \frac{2}{3} = 0,66 \checkmark M$</p> <p>$\hat{V} = 48,189^\circ \checkmark A$</p> <p>$\frac{\hat{V}}{2} = 24,0945^\circ$</p> <p>In $\triangle AVOR$</p> <p>$\frac{OR}{VR} = \tan \frac{V}{2} \quad \checkmark CA$</p> <p>$OR = 2 \tan 24,09^\circ \checkmark CA$</p> <p>$= 0,9 \text{ units} \checkmark CA$</p> <p style="text-align: right;">(5)</p>	<p>cosine expression</p> <p>value of \hat{V}</p> <p>simplification</p> <p>Identity</p> <p>substitution</p> <p>Simplification</p>



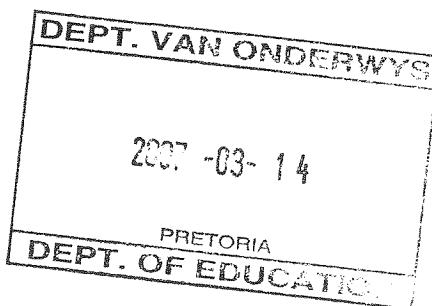
6.3.1	$\frac{h}{PN} = \tan w \quad \checkmark M$ $PN = \frac{h}{\tan w} \quad \checkmark A$ $\frac{PN}{\sin y} = \frac{PD}{\sin \hat{PND}} \quad \checkmark M$ $\frac{PN}{\sin y} = \frac{PD}{\sin (180^\circ - (x + y))} \quad \checkmark A$ $PD = \frac{PN \sin (x + y)}{\sin y} \quad \checkmark A$ $\therefore PD = \frac{h \cdot \sin (x + y)}{\sin y \cdot \tan w} \quad (5)$	<p>Correct tan ratio</p> <p>Application of sine formula</p> <p>Substitution & value for \hat{PND}</p> <p>Reduction and substitution</p>
6.3.2	$h = \frac{70 \cdot \sin 50^\circ \cdot \tan 64^\circ}{\sin 110^\circ} \quad \checkmark A$ $= 117 \text{ m} \quad \checkmark CA$	<p>Making h subject Correct substitution simplification</p> <p>(2)</p>



QUESTION 7

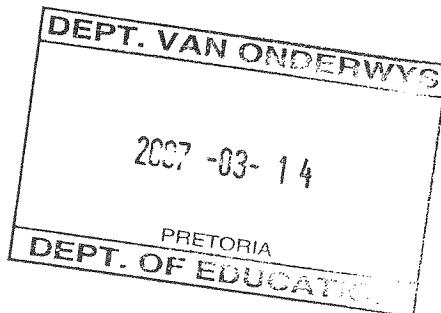
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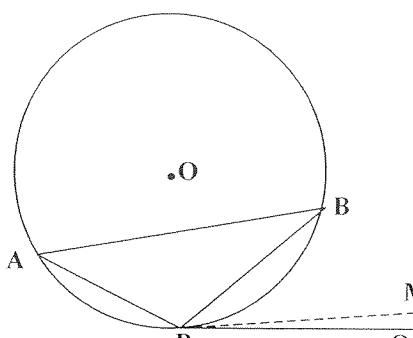
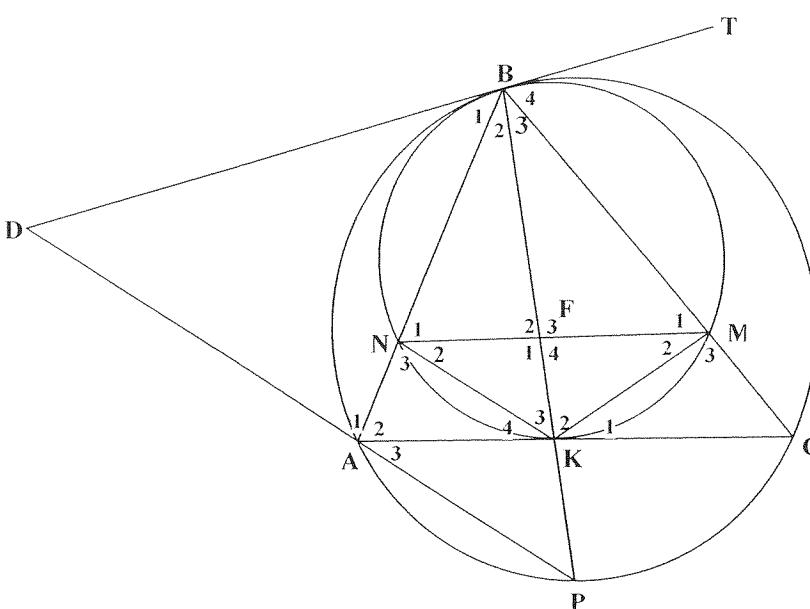
7.1	$\hat{A}_1 = 90^\circ \checkmark S \dots\dots (\angle \text{ in semi circle}) \checkmark R$ $\hat{T}_4 = \hat{A}_1 \dots\dots (\text{corr. } \angle \text{s}) \checkmark S/R$ $= 90^\circ \checkmark R$ $\therefore T \text{ is midpoint of } AC \dots (\text{line from centre } \perp \text{ to chord bisects chord}) \quad (4)$ OR	$BO = OC \quad (\text{radii}) \checkmark S/R$ $\text{In } \triangle ACB, AB // OT \text{ (given)} \checkmark S/R$ $\checkmark S$ $\therefore AT = TC \text{ (line from centre } \perp \text{ to } 2^{\text{nd}} \text{ side, bisects } 3^{\text{rd}} \text{ side)} \checkmark R$
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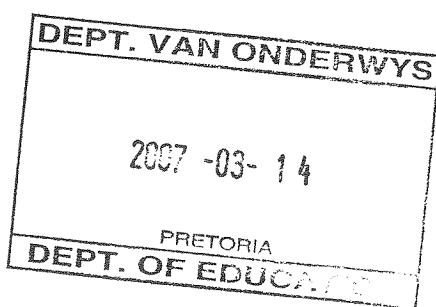


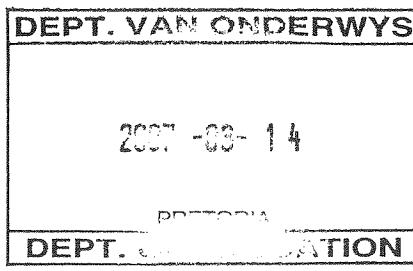
<p>7.2</p> $\begin{aligned} OT &= 3DT \\ OC &= OT + DT \quad \checkmark S \\ &= 4DT \\ TC &= \sqrt{OC^2 - OT^2} \checkmark S \\ &= \sqrt{(4DT)^2 - (3DT)^2} \\ &= \sqrt{7}DT \quad \checkmark S \\ MC^2 &= TC^2 + TM^2 \checkmark S \\ &= (\sqrt{7}DT)^2 + (7DT)^2 \checkmark S \\ &= 56DT^2 \checkmark S \\ MC &= \sqrt{56}DT \quad \text{OR } 2\sqrt{14}DT \quad \text{OR } 7,48DT \end{aligned}$ <p style="text-align: center;">OR</p> $\begin{aligned} AT &= TC ; \quad OT = 3DT \checkmark S \\ OD &= 4DT \checkmark S \\ \therefore MT &= 7DT \\ MC^2 &= MT^2 + TC^2 \checkmark S \\ &= (7DT)^2 + (16DT^2 - 9DT^2) \checkmark S \\ &= 49DT^2 + 7DT^2 \checkmark S \\ &= 56DT^2 \\ MC &= \sqrt{56}DT \end{aligned} \tag{6}$	<p style="text-align: center;">OR</p> $\begin{aligned} \Delta ABC //&/ \Delta MCT \checkmark S \\ \therefore \frac{AD}{MC} &= \frac{DT}{CT} = \frac{AT}{MT} \checkmark S \\ \text{but } CT &= AT \\ \therefore AT^2 &= DT \cdot MT \\ &= DT(7DT) \\ AT &= \sqrt{7}DT \quad \checkmark S \\ AD^2 &= AT^2 + DT^2 \\ &= 7DT^2 + DT^2 \\ &= 8DT^2 \\ AD &= \sqrt{8}DT \quad \checkmark S \\ \therefore \frac{AD}{MC} &= \frac{DT}{CT} \\ \frac{\sqrt{8}DT}{MC} &= \frac{DT}{\sqrt{7}DT} \quad \checkmark S \\ MC &= \sqrt{8} \cdot \sqrt{7}DT \\ &= \sqrt{56}DT \quad \text{OR } 2\sqrt{14}DT \checkmark S \\ \text{OR } 7,48DT \end{aligned}$
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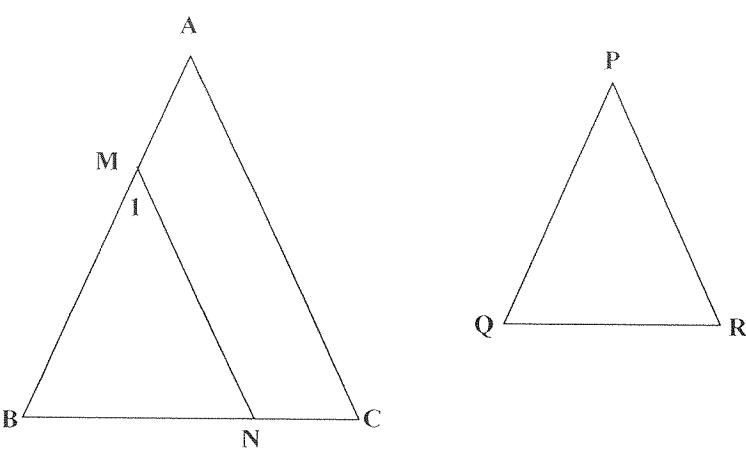
<p>7.3</p> $\begin{aligned} \hat{O}_2 &= 2\hat{M} \quad \checkmark S \quad (\angle \text{ at centre} = 2 \angle \text{ at circum.}) \\ \hat{M} &= \frac{1}{2}\hat{O}_2 \\ \hat{A}\hat{C}\hat{M} &= 90^\circ - \hat{M} \quad (\angle \text{s of } \Delta) \quad \checkmark S/R \\ &= 90^\circ - \frac{1}{2}\hat{O}_2 \\ \hat{D} &= \hat{A}\hat{C}\hat{M} \quad \checkmark S \quad (\angle \text{s in same segment}) \quad \checkmark R \\ &= 90^\circ - \frac{1}{2}\hat{O}_2 \end{aligned} \tag{5}$	<p style="text-align: center;">OR</p> $\begin{aligned} \hat{O}_2 &= \hat{O}_4 = x \quad (\text{vert. opp. } \angle \text{'s}) \checkmark S/R \\ \hat{C}_1 &= \frac{x}{2} \quad (\angle \text{ at centre} = 2 \angle \text{ at circum.}) \quad \checkmark S/R \\ \hat{C}_2 &= 90^\circ - x \quad (\angle \text{s of } \Delta) \checkmark S/R \\ \hat{D} &= \hat{C}_1 + \hat{C}_2 \quad (\angle \text{s in same segment}) \quad \checkmark S/R \\ &= \frac{x}{2} + 90^\circ - x = 90^\circ - \frac{1}{2}x \checkmark S \end{aligned}$
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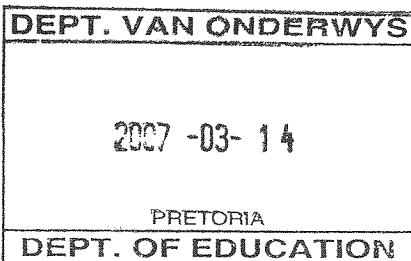


QUESTION 8		[25]
8.1	<p>Construction : Draw tangent PM to circle O through P</p> <p>Proof : $\hat{BPM} = \hat{A}$ $\checkmark S$ (tan-chord) $\checkmark R$</p> <p>But $\hat{BPQ} = \hat{A}$ (given) $\checkmark S$</p> <p>$\therefore \hat{BPQ} = \hat{BPM}$ $\checkmark S$ $\checkmark S$</p> <p>Which is impossible unless PM and PQ coincides \therefore PQ is a tangent</p>	 <p>(6)</p>
8.2		
8.2.1	$\hat{B}_1 = \hat{M}_1 \dots \checkmark S \dots \text{(tan-chord)}$ } $\checkmark R$ $\hat{B}_1 = \hat{C} \quad \checkmark S \dots \text{(tan-chord)}$ } $\therefore \hat{M}_1 = \hat{C}$ $\therefore MN \parallel CA \dots \text{(corr. } \angle s = \dots \checkmark R \quad (4)$	
8.2.2	$\hat{K}_1 = \hat{M}_2 \dots \text{(alt. } \angle s \dots \checkmark S/R$ $\hat{K}_1 = \hat{N}_2 \quad \checkmark S \dots \text{(tan-chord)} \quad \checkmark R$ $\therefore \triangle KMN \text{ is isosceles} \dots \text{(2 equal } \angle s \dots \quad (3)$	

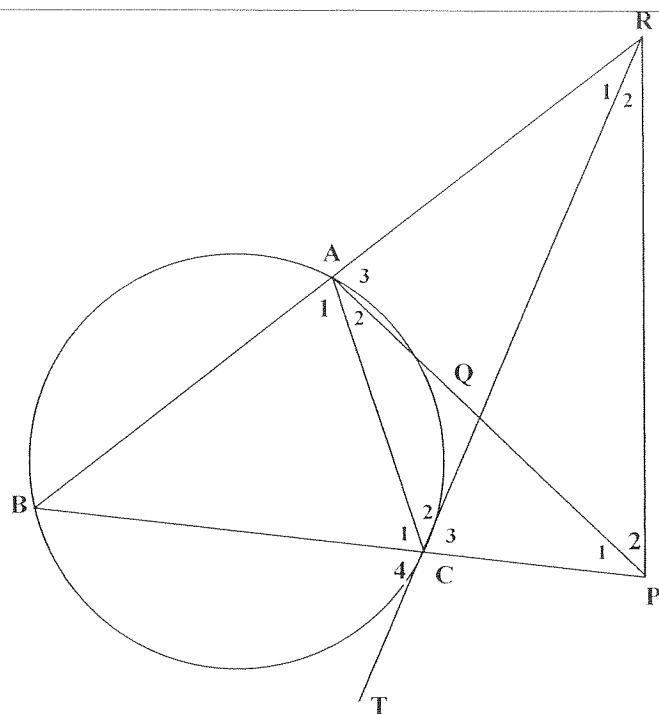


<p>8.2.3</p> $\hat{N}_2 = \hat{K}_4 \quad \dots \text{(alt. } \angle \text{s)} \quad \checkmark S$ $\hat{N}_2 = \hat{B}_3 \checkmark S \quad \checkmark R \quad \dots \text{(\angle s in same segment)}$ $\hat{B}_3 = \hat{A}_3 \quad \dots \text{(\angle s in same segment)}$ $\therefore \hat{K}_4 = \hat{A}_3$ $\therefore NK \parallel AP \quad \checkmark S \quad (\text{alt. } \angle' =)$ $\therefore \frac{BN}{NA} = \frac{BK}{KP} \quad \dots \text{(line } \parallel \text{ to one side of } \Delta) \checkmark S/R$ <p>but $\frac{BN}{NA} = \frac{BM}{MC} \quad \dots \text{(line } \parallel \text{ to one side of } \Delta)$</p> $\therefore \frac{BK}{KP} = \frac{BM}{MC} \quad (7)$	<p>OR</p> <p>Join P to C $\checkmark S$</p> $\hat{B}_4 = \hat{K}_2 \checkmark S \quad \checkmark R \quad \text{(tan-chord theorem)}$ $\hat{B}_4 = \hat{B} \hat{P} \hat{C} \checkmark S/R \quad \text{(tan-chord theorem)}$ $\therefore \hat{K}_2 = \hat{B} \hat{P} \hat{C} \quad \text{and they are corresp.}$ $KM \parallel PC \quad (\text{coresp. } \angle \text{s}) \checkmark S/R =$ $\frac{BK}{KP} = \frac{BM}{MC} \quad (\text{line } \parallel \text{ to one side of } \Delta) \checkmark S/R$
<p>8.2.4</p> $\hat{A}_3 = \hat{B}_3 \checkmark S \quad \checkmark R \quad \dots \text{(\angle s in same segment)}$ $\hat{B}_3 = \hat{B}_2 \checkmark S \quad \checkmark R \quad \dots \text{(equal chords subtend equal } \angle \text{s)}$ $\therefore \hat{A}_3 = \hat{B}_2 \checkmark S$ <p>$\therefore DA$ is a tangent to the circle through A, B and K</p> <p>OR</p> $\hat{A}_3 = \hat{B}_3 \checkmark S \quad \checkmark R \quad \dots \text{(\angle s in same segment)}$ $\hat{K}_1 = \hat{B}_3 \checkmark S \quad \checkmark R \quad \dots \text{(tan-chord)}$ $\hat{K}_1 = \hat{M}_2 \quad \checkmark S/R \quad \dots \text{(alt. } \angle \text{s, lines } \parallel)$ $\hat{M}_2 = \hat{B}_2 \quad \dots \text{(\angle s in same segment)}$ $\therefore \hat{A}_3 = \hat{B}_2$ <p>$\therefore DA$ is a tangent to the circle through A, B and K</p> <p>OR</p> $\hat{A}_1 = \hat{B}_2 + \hat{P} \quad \dots \text{(ext. } \angle \text{ of } \Delta) \quad \checkmark S/R$ $\hat{B}_2 = \hat{M}_2 \checkmark S \quad \checkmark R \quad \dots \text{(\angle s in same segment)}$ $\therefore \hat{M}_2 = \hat{N}_2 \quad \dots \text{(proved)}$ $\hat{N}_2 = \hat{K}_4 \quad \dots \text{(alt. } \angle' =, \text{ lines } \parallel)$ $\therefore \hat{B}_2 = \hat{K}_4$ $\hat{P} = \hat{K}_3 \quad \checkmark S/R \quad \dots \text{(corresp. } \angle' =, \text{ lines } \parallel)$ $\therefore \hat{A}_1 = \hat{K}_3 + \hat{K}_4$ <p>$\therefore DA$ is a tangent to the circle through A, B and K (5)</p>	 <p>DEPT. VAN ONDERWYS 2007 -03- 14 PRETORIA DEPT. OF EDUCATION</p>

QUESTION 9		[27]					
9.1	 <p>Construction : On AB and BC cut off BM and BN respectively such that $BM = PQ$ and $BN = QR$ $\checkmark S$</p> <p>Proof : In $\triangle BMN$ and $\triangle QPR$</p> <table style="margin-left: 100px;"> <tr> <td>$BM = PQ$(constr.)</td> <td rowspan="3" style="vertical-align: middle; font-size: 2em;">}</td> <td rowspan="3" style="vertical-align: middle;">$\checkmark S$</td> </tr> <tr> <td>$\hat{B} = \hat{Q}$(given)</td> </tr> <tr> <td>$BN = QR$(constr.)</td> </tr> </table> <p>$\triangle BMN \equiv \triangle QPR$(s, \angle, s) $\checkmark R$</p> <p>$\therefore \hat{M}_1 = \hat{P}$</p> <p>$= \hat{A}$ $\checkmark S/R$</p> <p>$\therefore MN \parallel AC$(corr. \angles =, lines \parallel)</p> <p>$\therefore \frac{AB}{MB} = \frac{BC}{BN}$(line \parallel to one side of \triangle) $\checkmark R$</p> <p>$\therefore \frac{AB}{PQ} = \frac{BC}{QR}$(MB = PQ and BN = QR) $\checkmark R$</p>	$BM = PQ$(constr.)	}	$\checkmark S$	$\hat{B} = \hat{Q}$(given)	$BN = QR$(constr.)	(7)
$BM = PQ$(constr.)	}	$\checkmark S$					
$\hat{B} = \hat{Q}$(given)							
$BN = QR$(constr.)							



9.2



9.2.1(a)

$$\hat{C}_3 = \hat{CPR} \quad \dots \text{(opp equal sides)} \quad \checkmark S/R$$

$$\hat{C}_3 + \hat{C}_2 = \hat{A}_1 + \hat{B} \quad \dots \text{(ext } \angle \text{ of } \Delta) \quad \checkmark S/R$$

$$\hat{C}_2 = \hat{B} \quad \checkmark S \quad \dots \text{(tan-chord)} \quad \checkmark R$$

$$\therefore \hat{C}_3 = \hat{A}_1$$

$$\therefore \hat{A}_1 = \hat{CPR} \quad \dots \text{(both } = \hat{C}_3) \quad \checkmark R$$

\therefore ACPR is a cyclic quadrilateral (conv. ext \angle of quad)

OR

$$\hat{C}_3 = \hat{C}_4 \quad \dots \text{(vert. opp. } \angle \text{s)} \quad \checkmark S/R$$

$$\hat{A}_1 = \hat{C}_4 \quad \dots \text{(tan-chord)} \quad \checkmark R$$

$$\therefore \hat{CPR} = \hat{C}_3$$

$$= \hat{A}_1 \quad \checkmark S$$

\therefore ACPR is a cyclic quadrilateral (conv. ext \angle of quad)

(5)

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9.2.1(b) In ΔCBA and ΔRPA

$$\hat{P}_2 = \hat{C}_2 \quad \checkmark S \quad \dots \text{(\mathit{\angle}s in same segment)} \quad \checkmark R$$

$$= \hat{B} \quad \checkmark S \quad \text{(proved in 9.2.1(a))}$$

$$\hat{B} = \hat{P}_2 \quad \dots \text{(proved)}$$

$$\hat{C}_1 = \hat{ARP} \quad \checkmark S \quad \text{(ext } \angle \text{ of cyclic quad)} \quad \checkmark R$$

	$\hat{A}_1 = \hat{A}_3 \dots \text{(3rd } \angle \text{ of } \Delta)$ $\therefore \Delta CBA \parallel\!\!\! \Delta RPA \dots (\angle \angle \angle) \quad \checkmark R \quad (6)$									
9.2.1(c)	$\frac{RP}{CB} = \frac{RA}{CA} \quad \text{(from 9.2.2(b))} \quad \checkmark S$ $RP = \frac{CB.RA}{AC} \quad \text{but } RP = RC \text{ given}$ $\therefore RC = \frac{CB.RA}{AC} \quad \checkmark S \quad (2)$									
9.2.1(d)	In ΔRAC and $\Delta RCB \checkmark S$ $\hat{C}_2 = \hat{B} \dots \text{(tan-chord)} \checkmark S$ \hat{R}_1 is common $R \hat{C} B = R \hat{A} C \dots \text{(3rd is } \angle)$ $\therefore \Delta RAC \parallel\!\!\! \Delta RCB \dots (\angle \angle \angle) \quad \checkmark R$ $\therefore \frac{AC}{CB} = \frac{RC}{RB} \quad \checkmark S \quad (\Delta's \parallel\!\!\!)$ $RB.AC = RC.CB \quad (4)$									
9.2.2	$\frac{CB}{RP} = \frac{CA}{RA} \dots \text{from 9.2.1(b)}$ $\frac{CB}{RC} = \frac{CA}{RA} \dots RC = RP \quad \checkmark S$ $AC = \frac{CB.RA}{RC} \dots \text{(i)}$ <p>from 9.2.2</p> $AC = \frac{RC.CB}{RB} \quad \checkmark S$ $\therefore \frac{CB.RA}{RC} = \frac{RC.CB}{RB} \quad \checkmark S$ $\therefore RC^2 = RA.RB$ <p>OR</p> $RP = RC$ $RC = \frac{CB.RA}{CA} \quad \checkmark S$ $RC = \frac{AC.RB}{CB} \quad \checkmark S$ $RC^2 = \frac{CB.RA}{CA} \cdot \frac{AC.RB}{CB} \quad \checkmark S$ $= RA.RB$	<table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td colspan="2">DEPT. VAN ONDERWYS</td> </tr> <tr> <td colspan="2">2007 -03- 14</td> </tr> <tr> <td colspan="2">PRETORIA</td> </tr> <tr> <td colspan="2">DEPT. OF EDUCATION</td> </tr> </table> (3)	DEPT. VAN ONDERWYS		2007 -03- 14		PRETORIA		DEPT. OF EDUCATION	
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