

**DiplETE – ET/CS (NEW SCHEME)**

Time: 3 Hours

**JUNE 2012**

Max. Marks: 100

**PLEASE WRITE YOUR ROLL NO. AT THE SPACE PROVIDED ON EACH PAGE IMMEDIATELY AFTER RECEIVING THE QUESTION PAPER.**

**NOTE: There are 9 Questions in all.**

- Question 1 is compulsory and carries 20 marks. Answer to Q.1 must be written in the space provided for it in the answer book supplied and nowhere else.
- The answer sheet for the Q.1 will be collected by the invigilator after 45 minutes of the commencement of the examination.
- Out of the remaining EIGHT Questions answer any FIVE Questions. Each question carries 16 marks.
- Any required data not explicitly given, may be suitably assumed and stated.

**Q.1 Choose the correct or the best alternative in the following:**

(2×10)

a.  $\lim_{x \rightarrow 1} \frac{x-1}{\log x}$  is :

(A) 1

(B)  $\frac{1}{2}$ 

(C) 2

(D) -1

b. The centroid of the triangle with vertices (2, 7), (3, 4) and (-6, 4) is

(A)  $\left(5, \frac{1}{3}\right)$ (B)  $\left(\frac{1}{3}, -5\right)$ (C)  $\left(-\frac{1}{3}, 5\right)$ (D)  $\left(-5, \frac{1}{3}\right)$ 

c.  $\int \sin^3 x dx$  is

(A)  $\frac{3}{4} \sin x + \frac{1}{12} \sin 3x + C$ (B)  $-\frac{3}{4} \cos x + \frac{1}{12} \cos 3x + C$ (C)  $\frac{3}{4} \sin x + \frac{1}{12} \cos 3x + C$ (D)  $-\frac{3}{4} \cos x - \frac{1}{12} \cos 3x + C$ 

d. If  $\Delta = \begin{vmatrix} \omega & \omega^2 & 1 \\ 1 & \omega & \omega^2 \\ \omega^2 & 1 & \omega \end{vmatrix}$ , then the value of  $\Delta$  is

(A) -1

(B) 1

(C) 2

(D) 0

e. If  $3 \begin{bmatrix} x & y \\ z & w \end{bmatrix} = \begin{bmatrix} x & 6 \\ -1 & 2w \end{bmatrix} + \begin{bmatrix} 4 & x+y \\ z+w & 3 \end{bmatrix}$ , then x, y, z, w is equal to

- (A) 1, 2, 3, 4 (B) 2, 4, 1, 3  
(C) -1, 3, 2, 4 (D) 1, -2, 1, 4

f. The order and degree of differential equation  $\frac{d^2y}{dx^2} = 1 + \sqrt{\frac{dy}{dx}}$  is

- (A) O = 2, D = 1 (B) O = 1, D = 1  
(C) O = 2, D = 3 (D) O = 2, D = 2

g. The middle term in the expansion of  $\left(x + \frac{1}{x}\right)^{12}$  is

- (A) 1001 (B) 923  
(C) 1004 (D) 924

h. The value of  $2 \cos\left(\frac{\pi}{4} + \theta\right) \cos\left(\frac{\pi}{4} - \theta\right)$  is

- (A)  $\sin 2\theta$  (B)  $\cos 2\theta$   
(C)  $\sin \theta \cos \theta$  (D)  $\cos 3\theta$

i. The distance between the pair of points  $A(am_1^2, 2am_1), B(am_2^2, 2am_2)$  is

- (A)  $a(m_2 - m_1)\sqrt{(m_2 + m_1)^2 + 4}$  (B)  $a(m_2 + m_1)\sqrt{(m_2 - m_1)^2 + 4}$   
(C)  $a(m_1 + m_2)\sqrt{(m_1 + m_2)^2 + 4}$  (D)  $a(m_2 - m_1)\sqrt{(m_2 + m_1)^2 - 4}$

j. If  $y = \log(\sec x + \tan x)$ , then  $\frac{dy}{dx}$  is

- (A)  $\sec x \operatorname{cosec} x$  (B)  $\tan x$   
(C)  $\sec x$  (D)  $\sec x \tan x$

Answer any FIVE Questions out of EIGHT Questions.

Each question carries 16 marks.

**Q.2** a. If  $x\sqrt{1+y} + y\sqrt{1+x} = 0$ , prove that  $\frac{dy}{dx} = -\frac{1}{(1+x)^2}$ . (8)

b. Find all the points of maxima minima and the corresponding maximum and minimum values of the function  $f(x) = -x^3 + 12x^2 - 5$ . (8)

**Q.3** a. Evaluate  $\int \frac{\sec^2 x}{5 \tan^2 x - 12 \tan x + 14} dx$  (8)

b. Evaluate  $\int_0^{\pi/4} \log(1 + \tan x) dx$  (8)

**Q.4** a. Solve the following equation  $\begin{vmatrix} x-2 & 2x-3 & 3x-4 \\ x-4 & 2x-9 & 3x-16 \\ x-8 & 2x-27 & 3x-64 \end{vmatrix} = 0$  (8)

b. Solve with the help of matrices the simultaneous equations:  
 $x + y + z = 3$   
 $x + 2y + 3z = 4$   
 $x + 4y + 9z = 6$  (8)

**Q.5** a. Solve  $\frac{dy}{dx} = \cos^3 x \sin^4 x + x\sqrt{2x+1}$  (8)

b. Solve  $\frac{dy}{dx} + y \sec x = \tan x$  (8)

**Q.6** a. Find the term independent of  $x$  in the expansion of  $\left(2x^2 - \frac{1}{x}\right)^{12}$  (8)

b. If the first term of an AP is 2 and the sum of first five terms is equal to one fourth of the sum of the next five terms, find the sum of first 30 terms. (8)

**Q.7** a. Prove that  $\cos 20^\circ \cos 30^\circ \cos 40^\circ \cos 80^\circ = \frac{\sqrt{3}}{16}$  (8)

b. If  $A + B + C = \pi$ , show that  $\sin A + \sin B + \sin C = 4 \cos \frac{A}{2} \cos \frac{B}{2} \cos \frac{C}{2}$  (8)

**Q.8** a. Find the equation of a line passing through the point (2, 3) and making an angle of  $45^\circ$  with the line  $3x + y - 5 = 0$ . (8)

b. If  $p$  is the length of the perpendicular from the origin to the line  $\frac{x}{a} + \frac{y}{b} = 1$ , then prove that  $\frac{1}{p^2} = \frac{1}{a^2} + \frac{1}{b^2}$  (8)

**Q.9** a. Find the equation of the circle passing through the point (2, 4) & has its centre at the intersection of lines  $x - y = 4$  and  $2x + 3y = -7$ . (8)

b. Show that  $4x^2 + 16y^2 - 24x - 32y - 12 = 0$  is the equation of an ellipse. Find its vertices, foci, eccentricity, directrices, major axis, minor and latusrectum. (8)