ROLL NO. _____

Code: AE07 Subject: NUMERICAL ANALYSIS & COMPUTER PRO~~~~~ING

AMIETE – ET (OLD SCHEME)

Time: 3 Hours | **JUNE 2012** | **Max. Marks: 100**

PLEASE WRITE YOUR ROLL NO. AT THE SPACE PROVIDED ON EACH PAGE IMMEDIATELY AFTER RECEIVING THE QUESTION PAPER.

NOTE: There are 9 Questions in all.
- **Question 1 is compulsory and carries 20 marks. Answer to Q.1 must be written in the space provided for it in the answer book supplied and nowhere else.**
- **The answer sheet for the Q.1 will be collected by the invigilator after 45 minutes of the commencement of the examination.**
- **Out of the remaining EIGHT Questions answer any FIVE Questions. Each question carries 16 marks.**
- **Any required data not explicitly given, may be suitably assumed and stated.**

Q.1 **Choose the correct or the best alternative in the following:** **(2×10)**

a. In C language, do while loop is executed

    (A) at least once   **(B)** once
    (C) more than once   **(D)** None of these

b. When rounding is used than chopping then the bound on the relative error of a floating point number is reduced by

    (A) quarter   **(B)** half
    (C) unit   **(D)** None of these

c. Which one of the following programming languages is a tree-form language?

    (A) COBOL   **(B)** C
    (C) FORTRAN   **(D)** None of these

d. Newton-Raphson method is applied to obtain the positive square root of N. The formula is given by

    (A) $x_{k+1} = \dfrac{1}{2}\left(x_k - \dfrac{N}{x_k} \right)$ **(B)** $x_{k+1} = \dfrac{1}{2}\left(x_k + \dfrac{N}{x_k} \right)$

    (C) $x_{k+1} = \left(x_k - \dfrac{N}{x_k} \right)$ **(D)** $x_{k+1} = \left(x_k + \dfrac{N}{x_k} \right)$

e. An operating system is a program that controls

    (A) Only arithmetic operations in a computer system
    (B) Only string operations in a computer system
    (C) The entire operation of a computer system
    (D) None of these

f. LU decomposition is guaranteed when the coefficient matrix A is positive definite. This condition is

   (A) necessary only   **(B)** sufficient only
   (C) both necessary & sufficient   **(D)** none of these

g. Consider the following statements:
   (i)   In interpolation, Lagrange and divided difference polynomials are two different forms of the same polynomial.
   (ii)   When the degree of interpolating polynomial is fixed, a judicious choice of the initial points may improve the result.
   Which of the following statements are correct?

   (A) (i) only   **(B)** (ii) only
   (C) Both (i) & (ii)   **(D)** None of these

h. Consider the following statements:
   (i) In numerical differentiation methods, the round-off error is always proportional to some power of step length h.
   (ii) In numerical differentiation methods, the truncation error is always proportional to some power of step length h.
   Which of the following statements are correct?

   (A) (i) only   **(B)** (ii) only
   (C) Both (i) & (ii)   **(D)** None of these

i. If the formula $\int\limits_{0}^{h} f(x)\,dx = h\left[af(0) + bf\left(\dfrac{h}{3}\right) + cf(h) \right]$ is exact for polynomials of

   as high order as possible, the values of a, b and c are given as respectively:

   (A) $0, \dfrac{3}{4}, \dfrac{1}{4}$ **(B)** $1, \dfrac{3}{4}, \dfrac{1}{4}$

   (C) $0, \dfrac{1}{4}, \dfrac{1}{4}$ **(D)** $\dfrac{1}{4}, \dfrac{1}{4}, \dfrac{1}{4}$

j. The value of y(0.2) using Euler's method, given that $y' = x(y + x) - 2$, $y(0) = 2$ (h = 0.2) is

   (A) 1.4   **(B)** 1.6
   (C) 1.272   **(D)** None of these

Answer any FIVE Questions out of EIGHT Questions.
Each question carries 16 marks.

Code: AE07   Subject: NUMERICAL ANALYSIS & COMPUTER PROGRAMMING

Q.2 a. Write a program in C to evaluate $\int_{0}^{1}\dfrac{x}{\left(1+x^2\right)}dx$ using Trapezoidal rule, using 10 subintervals. **(8)**

b. Find the iterative methods based on the Newton-Raphson method for finding the smallest positive root of $x^4-x-10=0$, correct to three decimal places. **(8)**

Q.3 a. Given equation $x-e^x=0$. Use secant method to find the smallest positive root of the given equation correct to three decimal places. **(8)**

b. What is the use of malloc() function? How can it be used in a C program? **(8)**

Q.4 a. Solve the system of equations by LU decomposition
$$4x_1+x_2+x_3=4$$
$$x_1+4x_2-2x_3=4$$
$$3x_1+2x_2-4x_3=6$$
(8)

b. Solve the following system of equations by Jacobi's method (perform 3 iterations)
$$4x+y+2z=4$$
$$3x+5y+z=7$$
$$x+y+3z=3$$
(8)

Q.5 a. Obtain   s   second   degree   polynomial   approximation   to $f(x)=(1+x)^{\frac{1}{2}}, x\in[0,\ 0.1]$, using the Taylor series expansion about x = 0. Use the expansion to approximate f(0.05) and find a bound of the Truncation Error. **(8)**

b. For the following data, calculate the divided differences and obtain the divided difference polynomial. Interpolate at x = 3.5. **(8)**

x :	0	1	2	4	5	6
$f(x)$:	1	14	15	5	6	19

Q.6 a. Determine the linear least square approximation to the function $y=2^x$ at the points $x_i=0,1,2,3,4$. **(8)**

b. Let $f(x)=\ell n(1+x), x_0=1$ and $x_1=1.1$. Find an approximate value of f(1.04) by Lagrange interpolation and obtain a bound on the truncation error. **(8)**
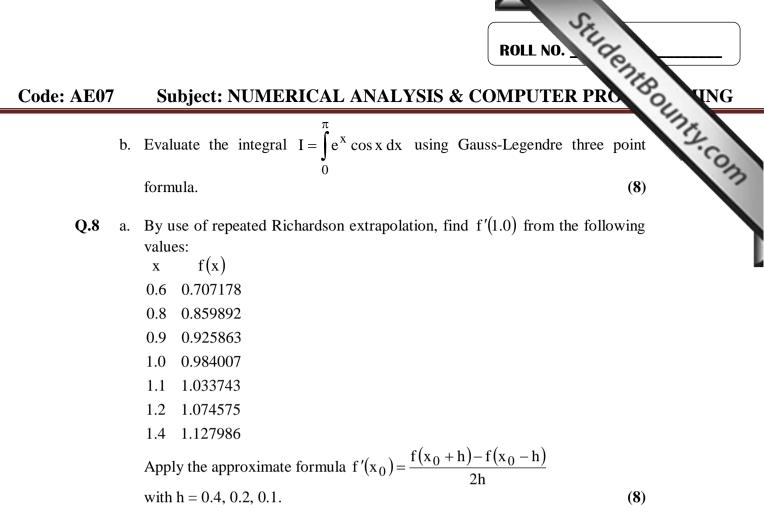
Q.7 a. Evaluate the integral $I=\int_{0}^{1}\dfrac{dx}{1+x}$ using composite Simpson's rule taking eight intervals. Also obtain the number of function evaluations required to get an accuracy of 10^{-6} when the integral is evaluated directly by using Simpson's rule. **(8)**

b. Evaluate the integral $I = \int\limits_{0}^{\pi} e^{x} \cos x \, dx$ using Gauss-Legendre three point formula. **(8)**

Q.8 a. By use of repeated Richardson extrapolation, find $f'(1.0)$ from the following values:

x	$f(x)$
0.6	0.707178
0.8	0.859892
0.9	0.925863
1.0	0.984007
1.1	1.033743
1.2	1.074575
1.4	1.127986

Apply the approximate formula $f'(x_0) = \dfrac{f(x_0 + h) - f(x_0 - h)}{2h}$

with $h = 0.4, 0.2, 0.1$. **(8)**

b. Given $\dfrac{dy}{dx} = \dfrac{1}{x + y}$, where y(0) = 1, find y(0.5) and y(0.1) using Runge-Kutta fourth order method. **(8)**

Q.9 a. Using Gauss-Jordan method with partial pivoting, solve the system of equations

$$\begin{bmatrix} 1 & 1 & -2 & | & 3 \\ 4 & -2 & 1 & | & 5 \\ 3 & -1 & 3 & | & 8 \end{bmatrix}.$$ **(8)**

b. Compute the number of steps required in Bisection method, given the initial guess values are a and b. **(8)**