

Subject: FINITE AUTOMATA & FORMULA LANGUAGES
Time: 3 Hours

Max. Marks: 100

JUNE 2011

NOTE: There are 9 Questions in all.

- **Question 1 is compulsory and carries 20 marks. Answer to Q.1 must be written in the space provided for it in the answer book supplied and nowhere else.**
- **The answer sheet for the Q.1 will be collected by the invigilator after 45 Minutes of the commencement of the examination.**
- **Out of the remaining EIGHT Questions answer any FIVE Questions. Each question carries 16 marks.**
- **Any required data not explicitly given, may be suitably assumed and stated.**

Q.1 Choose the correct or the best alternative in the following: (2×10)

a. The grammar with production rule is $\{S \rightarrow aSbb, S \rightarrow abb\}$ is

- (A) type-3 grammar (B) type-2 grammar
(C) type-1 grammar (D) type-0 grammar

b. Which of the following statement is wrong?

- (A) A Turing Machine cannot solve halting problem.
(B) Set of recursively enumerable languages is closed under union.
(C) A Finite State Machine with 3 stacks is more powerful than Finite State Machine with 2 stacks.
(D) Context sensitive grammar can be recognized by a linearly bounded memory machine.

c. Recursively enumerable languages are not closed under

- (A) Complementation (B) Union
(C) Intersection (D) None of the above

d. Regular expression (x/y) denotes the set

- (A) $\{xy, xy\}$ (B) $\{xx, xy, yx, yy\}$
(C) $\{x, y\}$ (D) $\{x, y, xy\}$

e. Which of the following string can be generated by the productions:
 $S \rightarrow aS/bA, A \rightarrow d/cA$

- (A) aabccd (B) adabcca
(C) abcca (D) abababd

f. Regular sets are closed under

- (A) Union (B) Concentration
(C) Kleene's closure (D) All of the above

g. A Finite State Machine with finite is length tape and unidirectional head movement is considered as

- (A) Turing machine (B) Pushdown automata
(C) Context free languages (D) Regular languages

h. Which of the following language is not regular?

- (A) $\{a^n b^n \mid n \geq 0\}$ (B) $\{a^n \mid n \geq 1\}$
(C) $\{a^n b^m \mid n \geq 0, m \geq 10\}$ (D) $\{abc\}$

i. Consider the following production rules

$$S \rightarrow a/aS$$

$$S \rightarrow b$$

Which of the following regular expression is generated by the above production rules

- (A) $(ab)^*$ (B) $a(ab)^*b$
(C) aa^*b^+ (D) aa^*b

j. Consider the following grammar

$$S \rightarrow SS$$

$$S \rightarrow OS1$$

$$S \rightarrow 1S0$$

$$S \rightarrow \epsilon$$

The grammar will generate

- (A) regular language (B) context-free language
(C) context sensitive language (D) recursively enumerable language.

**Answer any FIVE Questions out of EIGHT Questions.
Each question carries 16 marks.**

Q.2 a. Prove by mathematical induction $n^4 - 4n^2$ is divisible by 3 for $n \geq 0$. (8)

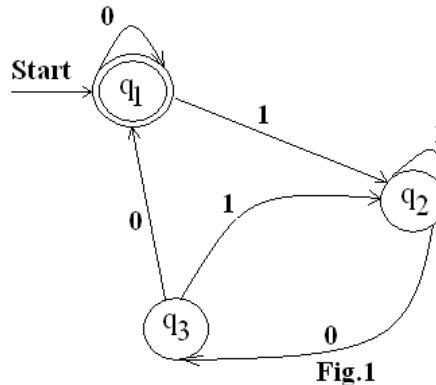
b. Discuss diagonalization Principle with example. (8)

Q.3 a. Draw the state diagram for NFA accepting language
 $L = (ab)^* (ba)^* \cup aa^*$. (8)

- b. Design the deterministic finite automata for the language
 $L = \{w: n_a(w) \leq 3, w \in (a,b)^*\}$ (8)

- Q.4** a. Write the regular expression for the language
 $L = \{a^n b^m \mid n \geq 4, m \leq 3\}$ (8)

- b. Find a regular expression corresponding to the state diagram given in Fig.1.



- Q.5** a. Prove that $L = \{a^n b a^n \mid n = 0, 1, 2, \dots\}$ is not regular. (8)

- b. $\Sigma = \{0, 1\}$, and $\Sigma' = \{1, 2, 3\}$. Define h by
 $h(0) = 3122$
 $h(1) = 132$
 If L is regular language denoted by
 $r = (0 + 1^*)(00)^*$
 then find the regular expression for language $h(L)$. (8)

- Q.6** a. Write a context free grammar, that generates palindrome of binary numbers. (8)

- b. Construct the pushdown automata for the following language.
 $L = \{a^n b^{n+1} \mid n = 1, 2, 3, \dots\}$. (8)

- Q.7** a. Change the following grammar to CNF
 $G = (\{S\}, \{a, b, c\}, \{S \rightarrow a/b/CSS\}, S)$ (8)

- b. Prove that language $L = \{WW \mid W \in \{a, b\}^*\}$ is not context-free. (8)

- Q.8** a. Design a Turing Machine that accepts the language of all strings that contain aba as a substring. (8)

- b. Discuss 'Church's thesis? Why Church's thesis is not considered as a theorem in mathematics. (8)

- Q.9** a. Prove that following instance of a Post Correspondence Problem (PCP) has no solution over $\Sigma = \{0, 1\}$, X and Y be lists of three strings as follows: (8)

	List X	List Y
i	X_i	Y_i
1	10	101
2	011	11
3	101	011

- b. Prove that if a language L and its complement L' are both recursively enumerable, then L (and hence L') is recursive. (8)