Student Bounty Com HONG KONG EXAMINATIONS AND ASSESSMENT AUTHORITY HONG KONG DIPLOMA OF SECONDARY EDUCATION EXAMINATION

## **MATHEMATICS** Compulsory Part PAPER 2 (Sample Paper)

Time allowed: 1 hour 15 minutes

- 1. Read carefully the instructions on the Answer Sheet. Stick a barcode label and insert the information required in the spaces provided.
- 2. When told to open this book, you should check that all the questions are there. Look for the words 'END OF **PAPER**' after the last question.
- 3. All questions carry equal marks.
- 4. ANSWER ALL QUESTIONS. You are advised to use an HB pencil to mark all the answers on the Answer Sheet, so that wrong marks can be completely erased with a clean rubber.
- 5. You should mark only ONE answer for each question. If you mark more than one answer, you will receive NO MARKS for that question.
- 6. No marks will be deducted for wrong answers.

Not to be taken away before the end of the examination session

There are 30 questions in Section A and 15 questions in Section B. The diagrams in this paper are not necessarily drawn to scale. Choose the best answer for each question.

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#### **Section A**

1. 
$$(3a)^2 \cdot a^3 =$$

- A.  $3a^5$ .
- B.  $6a^6$ .
- C.  $9a^5$ .
- D.  $9a^6$ .

2. If 
$$5-3m = 2n$$
, then  $m =$ 

- A. *n*.
- B.  $\frac{2n-5}{3}$ .
- $C. \qquad \frac{-2n+5}{3} \ .$

D. 
$$\frac{-2n+15}{3}$$
.

3. 
$$a^2 - b^2 + 2b - 1 =$$

A. 
$$(a-b-1)(a+b-1)$$
.

B. 
$$(a-b-1)(a+b+1)$$
.

C. 
$$(a-b+1)(a+b-1)$$
.

D. 
$$(a-b+1)(a-b-1)$$
.

D. 5.

Let  $f(x) = x^3 + 2x^2 - 7x + 3$ . When f(x) is divided by x + 2, the remainder is 5.

> A. 3.

B. 5.

C. 17 .

D. 33.

Let a be a constant. Solve the equation (x-a)(x-a-1) = (x-a). 6.

> x = a + 1A.

B. x = a + 2

C. x = a or x = a + 1

D. x = a or x = a + 2

Find the range of values of k such that the quadratic equation  $x^2 - 6x = 2 - k$  has no real roots. 7.

> A. k < -7

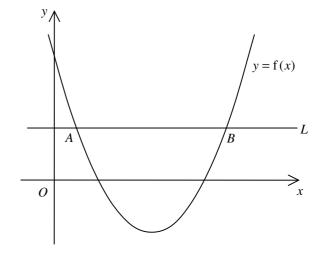
B. k > -7

C. *k* < 11

D. k > 11

## t A(1,k) and B(7, 1)

- 8. In the figure, the quadratic graph of y = f(x) intersects the straight line L at A(1, k) and B(7). Which of the following are true?
  - I. The solution of the inequality f(x) > k is x < 1 or x > 7.
  - II. The roots of the equation f(x) = k are 1 and 7.
  - III. The equation of the axis of symmetry of the quadratic graph of y = f(x) is x = 3.
    - A. I and II only
    - B. I and III only
    - C. II and III only
    - D. I, II and III

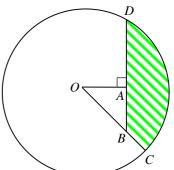


- 9. The solution of 5-2x < 3 and 4x+8 > 0 is
  - A. x > -2.
  - B. x > -1.
  - C. x > 1.
  - D. -2 < x < 1.
- 10. Mary sold two bags for \$ 240 each. She gained 20% on one and lost 20% on the other. After the two transactions, Mary
  - A. lost \$20.
  - B. gained \$10.
  - C. gained \$60.
  - D. had no gain and no loss.

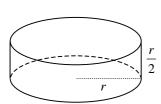
- 11. Let  $a_n$  be the *n*th term of a sequence. If  $a_1 = 4$ ,  $a_2 = 5$  and  $a_{n+2} = a_n + a_{n+1}$  for any positive then  $a_{10} =$ 
  - A. 13.
  - B. 157.
  - C. 254.
  - D. 411.
- 12. If the length and the width of a rectangle are increased by 20% and x% respectively so that its area is increased by 50%, then x=
  - A. 20.
  - B. 25.
  - C. 30.
  - D. 35.
- 13. If x, y and z are non-zero numbers such that 2x = 3y and x = 2z, then (x+z):(x+y) =
  - A. 3:5.
  - B. 6:7.
  - C. 9:7.
  - D. 9:10.
- 14. It is given that z varies directly as x and inversely as y. When x=3 and y=4, z=18. When x=2 and z=8, y=
  - A. 1.
  - B. 3.
  - C. 6.
  - D. 9.

## Student Bounty.com The lengths of the three sides of a triangle are measured as 15 cm, 24 cm and 25 cm respecti 15. three measurements are correct to the nearest cm, find the percentage error in calculating the perin the triangle correct to the nearest 0.1%.

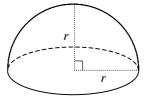
- 0.8% A.
- В. 2.3%
- C. 4.7%
- D. 6.3%
- In the figure, O is the centre of the circle. C and D are points lying on the circle. OBC and BAD are 16. straight lines. If OC = 20 cm and OA = AB = 10 cm, find the area of the shaded region BCD correct to the nearest  $cm^2$ .
  - $214 \text{ cm}^2$ A.
  - $230 \, \mathrm{cm}^2$ В.
  - $246 \, \text{cm}^2$ C.
  - $270 \, \mathrm{cm}^2$ D.

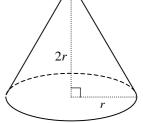


17. The figure shows a right circular cylinder, a hemisphere and a right circular cone with equal base radii. Their curved surface areas are  $a \text{ cm}^2$ ,  $b \text{ cm}^2$  and  $c \text{ cm}^2$  respectively.







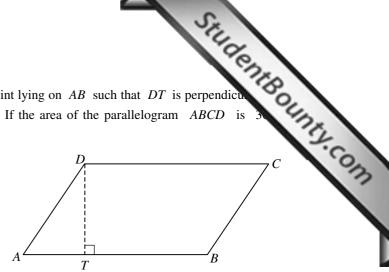


- A. a < b < c
- B. a < c < b
- C. c < a < b
- D. c < b < a

18. In the figure, ABCD is a parallelogram. T is a point lying on AB such that DT is perpendicular is given that CD = 9 cm and AT : TB = 1 : 2. If the area of the parallelogram ABCD is then the perimeter of the parallelogram ABCD is







19. 
$$\frac{\sin \theta}{\cos 60^{\circ}} + \frac{\cos(270^{\circ} - \theta)}{\tan 45^{\circ}} =$$

A. 
$$\sin \theta$$
.

B. 
$$3\sin\theta$$
.

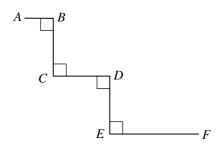
C. 
$$2\sin\theta - \cos\theta$$
.

D. 
$$2\sin\theta + \cos\theta$$
.

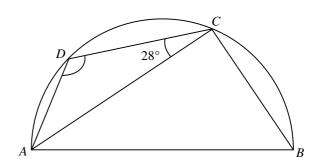
20. In the figure, AB = 1 cm, BC = CD = DE = 2 cm and EF = 3 cm. Find the distance between A and F correct to the nearest 0.1 cm.



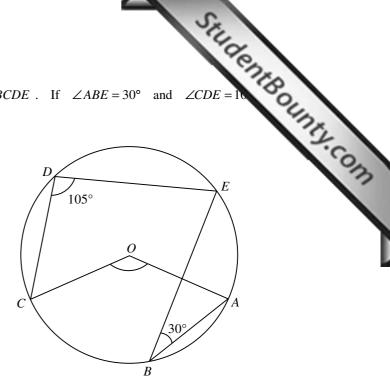
D. 8.1 cm



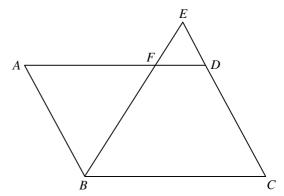
21. In the figure, ABCD is a semi-circle. If BC = CD, then  $\angle ADC =$ 



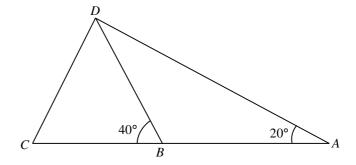




23. In the figure, ABCD is a parallelogram. F is a point lying on AD. BF produced and CD produced meet at E. If CD:DE=2:1, then AF:BC=

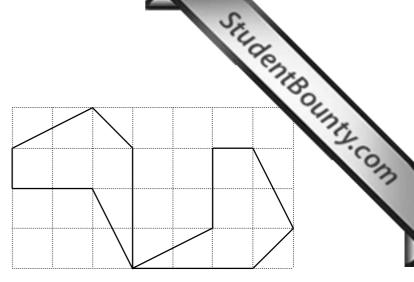


24. In the figure, ABC is a straight line. If BD = CD and AB = 10 cm, find BC correct to the nearest cm.



### 25. In the figure, the two 6-sided polygons show

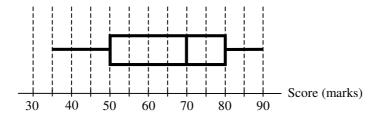
- A. a rotation transformation.
- B. a reflection transformation.
- C. a translation transformation.
- D. a dilation transformation.



## 26. If the point (-4,3) is rotated anti-clockwise about the origin through $180^{\circ}$ , then the coordinates of its image are

- A. (-3, -4).
- B. (3,4).
- C. (-4, -3).
- D. (4,-3).

## 27. The box-and-whisker diagram below shows the distribution of the scores (in marks) of the students of a class in a test.



If the passing score of the test is 50 marks, then the passing percentage of the class is

- A. 25%.
- B. 50%.
- C. 70%.
- D. 75%.

Stem (tens)	Leaf (units) 3 3 4 5 6 7 9 1 2 2 3 5 6 6 8 1 2 6 7 9 2 6 7							
15	3	3	4	5	6	7	9	
16	1	2	2	3	5	6	6	8
17	1	2	6	7	9			
18	2	6	7					

Find the median of the distribution.

- 164 cm A.
- B. 165 cm
- C. 165.5 cm
- D. 166 cm
- $\{a-7, a-1, a, a+2, a+4, a+8\}$  and  $\{a-9, a-2, a-1, a+3, a+4, a+6\}$  are two 29. groups of numbers. Which of the following is/are true?
  - I. The two groups of numbers have the same mean.
  - II. The two groups of numbers have the same median.
  - III. The two groups of numbers have the same range.
    - A. I only
    - B. II only
    - C. I and III only
    - D. II and III only
- 30. The students' union of a school of 950 students wants to investigate the opinions of students in the school on the services provided by the tuck shop. A questionnaire is designed by the students' union and only the chairperson and vice-chairperson of the students' union are selected as a sample to fill in the questionnaire. Which of the following are the disadvantages of this sampling method?
  - The sample size is very small.
  - II. Not all students in the school are selected.
  - III. Not all students in the school have an equal chance of being selected.
    - A. I and II only
    - B. I and III only
    - C. II and III only
    - D. I, II and III

#### **Section B**

31. 
$$\frac{1}{2-x} + \frac{x-1}{(x-2)^2} =$$

$$A. \qquad \frac{-3}{(2-x)^2} \ .$$

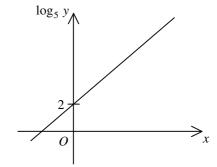
$$B. \qquad \frac{1}{(2-x)^2} \ .$$

C. 
$$\frac{-2x+3}{(2-x)^2}$$
.

D. 
$$\frac{2x-3}{(2-x)^2}$$
.

32. The graph in the figure shows the linear relation between x and  $\log_5 y$ . If  $y = ab^x$ , then a =





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33.  $1010010001001_2 =$ 

A. 
$$2^{12} + 2^{10} + 137$$
.

B. 
$$2^{12} + 2^{10} + 273$$
.

C. 
$$2^{13} + 2^{11} + 137$$
.

D. 
$$2^{13} + 2^{11} + 273$$
.

34. If *k* is a real number, then  $4k - \frac{6+ki}{i} =$ 

A. 
$$3k + 6i$$
.

B. 
$$3k-6i$$
.

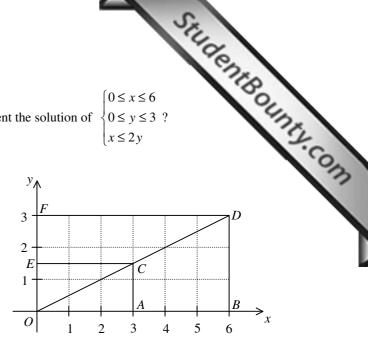
C. 
$$5k + 6i$$
.

D. 
$$5k - 6i$$
.

35. Which of the triangular regions in the figure may represent the solution of



- A.  $\Delta OAC$
- B.  $\Delta OBD$
- C.  $\Delta OCE$
- D.  $\Delta ODF$



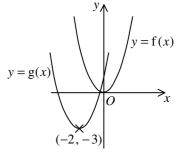
- 36. If the 3rd term and the 6th term of an arithmetic sequence are 18 and -6 respectively, then the 2nd term of the sequence is
  - -8 . A.
  - B. 10.
  - C. 26.
  - D. 34.
- If the figure shows the graph of y = f(x) and the graph of y = g(x) on the same rectangular coordinate 37. system, then

A. 
$$g(x) = f(x-2)-3$$
.

B. 
$$g(x) = f(x-2) + 3$$
.

C. 
$$g(x) = f(x+2)-3$$
.

D. 
$$g(x) = f(x+2) + 3$$
.



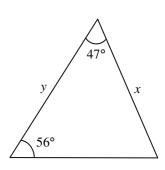
38. In the figure, y =

A. 
$$\frac{x \sin 77^{\circ}}{\sin 56^{\circ}}$$

B. 
$$\frac{x\sin 47^{\circ}}{\sin 56^{\circ}}$$
.

$$C. \qquad \frac{x \sin 56^{\circ}}{\sin 77^{\circ}}$$

D. 
$$\frac{x \sin 77^{\circ}}{\sin 47^{\circ}}$$



D. 882.18

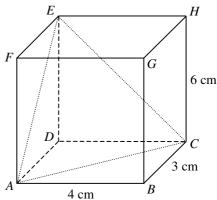
40. The figure shows a cuboid ABCDEFGH. If the angle between the triangle ACE and the plane ABCD is  $\theta$ , then  $\tan \theta =$ 



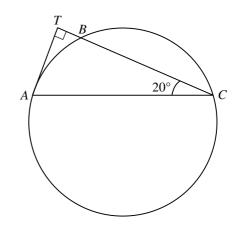
B. 
$$\frac{3}{2}$$
.

C. 
$$\frac{5}{2}$$
.

D. 
$$\frac{12}{5}$$
.



41. In the figure, A, B and C are points lying on the circle. TA is the tangent to the circle at A. The straight line CBT is perpendicular to TA. If  $BC = 6 \, \text{cm}$ , find the radius of the circle correct to the nearest  $0.1\,\mathrm{cm}$  .



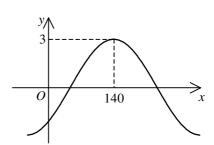
42. Let a be a constant and  $-90^{\circ} < b < 90^{\circ}$ . If the figure shows the graph of  $y = a\cos(x^{\circ} + b)$ , then

A. 
$$a = -3$$
 and  $b = -40^{\circ}$ .

B. 
$$a = -3$$
 and  $b = 40^{\circ}$ .

C. 
$$a = 3$$
 and  $b = -40^{\circ}$ .

D. 
$$a = 3$$
 and  $b = 40^{\circ}$ .





B. 
$$\frac{29}{81}$$

C. 
$$\frac{52}{81}$$
.

D. 
$$\frac{68}{81}$$
.

44. If 2 girls and 5 boys randomly form a queue, find the probability that the two girls are next to each other in the queue.

A. 
$$\frac{1}{7}$$

B. 
$$\frac{2}{7}$$

C. 
$$\frac{6}{7}$$

D. 
$$\frac{1}{2}$$

45. A set of numbers has a mode of 32, an inter-quartile range of 27 and a variance of 25. If 3 is added to each number of the set and each resulting number is then doubled to form a new set of numbers, find the mode, the inter-quartile range and the variance of the new set of numbers.

	Mode	Inter-quartile range	Variance
A.	64	60	50
B.	70	60	100
C.	70	54	50
D.	70	54	100

END OF PAPER