

GCSE

**Mathematics
(Modular)**

Summer 2009

Mark Schemes

Issued: October 2009

**NORTHERN IRELAND GENERAL CERTIFICATE OF SECONDARY EDUCATION (GCSE)
AND NORTHERN IRELAND GENERAL CERTIFICATE OF EDUCATION (GCE)**

MARK SCHEMES (2009)

Foreword

Introduction

Mark Schemes are published to assist teachers and students in their preparation for examinations. Through the mark schemes teachers and students will be able to see what examiners are looking for in response to questions and exactly where the marks have been awarded. The publishing of the mark schemes may help to show that examiners are not concerned about finding out what a student does not know but rather with rewarding students for what they do know.

The Purpose of Mark Schemes

Examination papers are set and revised by teams of examiners and revisers appointed by the Council. The teams of examiners and revisers include experienced teachers who are familiar with the level and standards expected of 16- and 18-year-old students in schools and colleges. The job of the examiners is to set the questions and the mark schemes; and the job of the revisers is to review the questions and mark schemes commenting on a large range of issues about which they must be satisfied before the question papers and mark schemes are finalised.

The questions and the mark schemes are developed in association with each other so that the issues of differentiation and positive achievement can be addressed right from the start. Mark schemes therefore are regarded as a part of an integral process which begins with the setting of questions and ends with the marking of the examination.

The main purpose of the mark scheme is to provide a uniform basis for the marking process so that all the markers are following exactly the same instructions and making the same judgements in so far as this is possible. Before marking begins a standardising meeting is held where all the markers are briefed using the mark scheme and samples of the students' work in the form of scripts. Consideration is also given at this stage to any comments on the operational papers received from teachers and their organisations. During this meeting, and up to and including the end of the marking, there is provision for amendments to be made to the mark scheme. What is published represents this final form of the mark scheme.

It is important to recognise that in some cases there may well be other correct responses which are equally acceptable to those published: the mark scheme can only cover those responses which emerged in the examination. There may also be instances where certain judgements may have to be left to the experience of the examiner, for example, where there is no absolute correct response – all teachers will be familiar with making such judgements.

The Council hopes that the mark schemes will be viewed and used in a constructive way as a further support to the teaching and learning processes.

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General Certificate of Secondary Education
Summer 2009

Mathematics

Module N1 Paper 1
(Non-calculator)
Foundation Tier

[GMN11]

MONDAY 18 MAY

1.30 pm – 2.15 pm

MARK SCHEME

GCSE MATHEMATICS 2009

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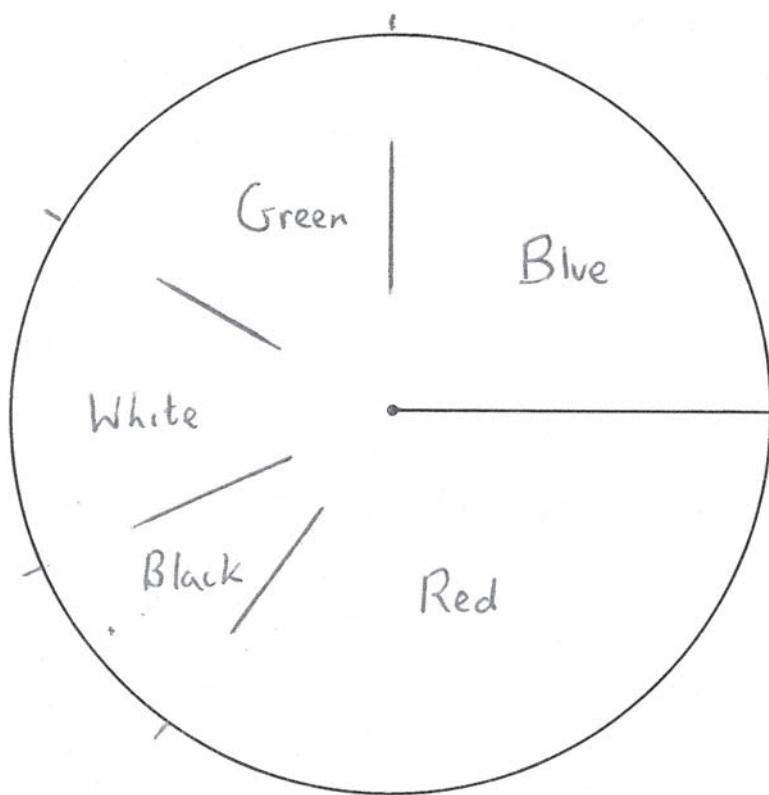
- a numerical error in one entry in a table of values might lead to several answers being incorrect, but these might not be essentially separate errors;
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When the candidate misreads a question in such a way as to make the question easier only a proportion of the marks will be available (based on the professional judgement of the examiner).

			AVAILABLE MARKS
1	(a) Square based pyramid, cuboid	A1, A1	
	(b) circumference, radius, chord	A1, A1, A1	5
2	(a) 6	A1	
	(b) 36	A1	
	(c) 3 cones drawn	M1, A1	4
3	(a) 16	A1	
	(b) 18	A1	
	(c) 12 and 18	A1	3
4	(a) 1, 4, 9, 16	A1	
	(b) Square numbers	A1	2
5	(a) $500 - 272 = 228$	M1, A1	
	(b) 26 000 000	A1	3
6	$28\% = 0.28$	MA1	
	$\frac{3}{10} = 0.3$	MA1	
	0.28, $\frac{3}{10}$, 0.4 are in correct order	MA1	3
7	(a) $200/10$ 20	M1, A1 A1	
	(b) (i) 1.5 hours	A2	
	(ii) 2 hours (allow 15 mins tolerance)	A1	
	(iii) 100 degrees (allow 2 degrees tolerance)	A1	7

			AVAILABLE MARKS
8	(a) 16	A1	
	(b) (i) $15 \times 10 \times 12 = 1800 \text{ cm}^3$	M1, A1, A1 (units)	
	(ii) $\frac{120}{(8 \times 5)} = 3$	M1, A1	6
9	See overlay $90^\circ, 60^\circ, 54^\circ, 30^\circ, 126^\circ$ (award one mark for evidence of 60 or 6) All sectors correct and labelled	A2 A2	4
10	(a) -4	A1	
	(b) graph	M1, A1	3
11	(a) $25 \times 8 = 200$	A1, A1	
	(b) $\frac{7}{8} \times 100 = \frac{700}{8}$ $= 87\frac{1}{2}$	MA1 MA1	4
		Total	44

GCSE MATHEMATICS SUMMER 2009
MODULE N1-1
OVERLAY QUESTION 9





General Certificate of Secondary Education
2009

Mathematics
Module N1 Paper 2
(With calculator)
Foundation Tier
[GMN12]

MONDAY 18 MAY
2.45 pm – 3.30 pm

**MARK
SCHEME**

GCSE MATHEMATICS 2009

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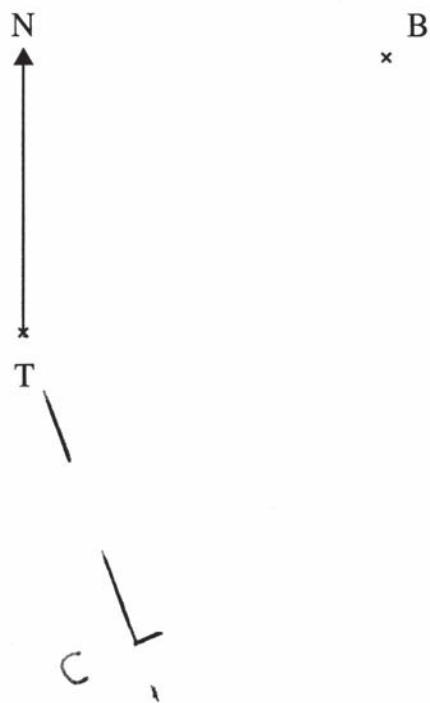
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			AVAILABLE MARKS
1	(a) Diagram 4 correct	A1	
	(b) 10 and 15	A1 (both correct)	2
2	(a) $\frac{6}{9} = \frac{2}{3}$	A1, A1	
	(b) $\frac{4}{15}, \frac{8}{30}$	A1, A1	4
3	(a) scales bars (allow A1 for 3 correct)	A1 A2	
	(b) car	A1	
	(c) 27	A1	5
4	(a) kilogram	A1	
	(b) millilitre or litre	A1	
	(c) kilometre	A1	3
5	(a) $4 \times 63p = £2.52$ change = $£5 - £2.52 = £2.48$	MA1 MA1	
	(b) $30 \div 4.2 = 7.14\dots$ $= 7$	MA1 MA1	4

			AVAILABLE MARKS
6	(a) 12 cm^2	A1	
	(b) $180 - 48 - 29 = 103$	A1	2
7	(a) (i) 5.6 (ii) 53.29	A1 A1	
	(b) $\frac{5}{100} \times 16000$ $= £800$	MA1 MA1	
	(c) (i) 25.29	A1	
	(ii) 8.5	A1	6
8	(a) $2 + 1 - 4$ $= -1$	MA1 A1	
	(b) $y = 18$	MA1	3
9	(a) 8	A1	
	(b) -4	A1	2
10	Girls Boys' mean = $130/10 = 13$ Girls' mean = $128/8 = 16$	A1 M1, A1 MA1	4
11	(a) 7	A1	
	(b) $\frac{10}{0.25}$ $= 40$	MA1 A1	3

		AVAILABLE MARKS
12	(a) (i) 053° or N 53° E ($\pm 2^\circ$)	A1
	(ii) distance 4.5 cm (± 2 mm) bearing 160° ($\pm 2^\circ$)	A1 A1
(b) (i)	80	MA1
	(ii) $180 - 80 = 100$ $100 \div 2 = 50$	MA1 MA1 6
		Total 44

GCSE MATHEMATICS SUMMER 2009
MODULE N1-2
OVERLAY QUESTION 12





General Certificate of Secondary Education
Summer 2009

Mathematics

Module N2 Paper 1
(Non-calculator)
Foundation Tier

[GMN21]

MONDAY 18 MAY

1.30 pm – 2.15 pm

MARK SCHEME

GCSE MATHEMATICS 2009

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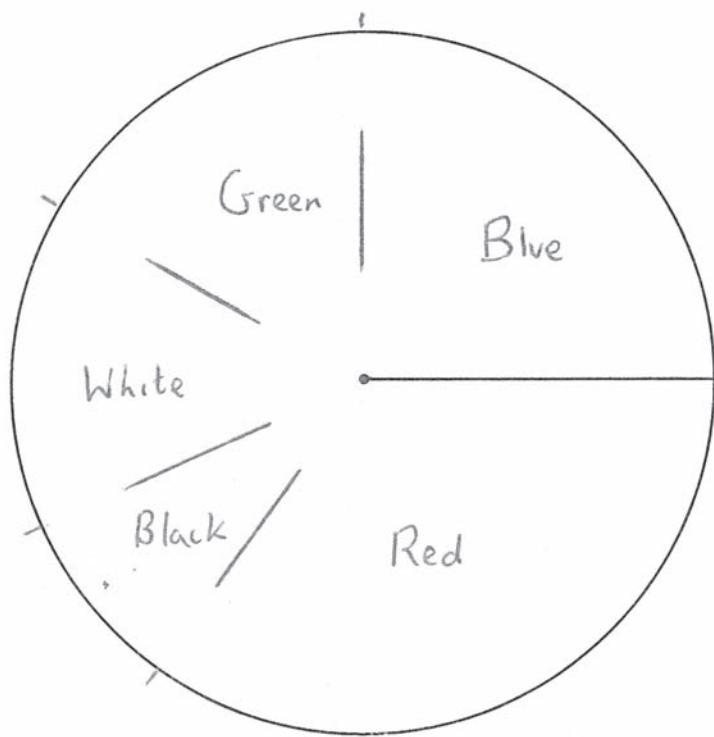
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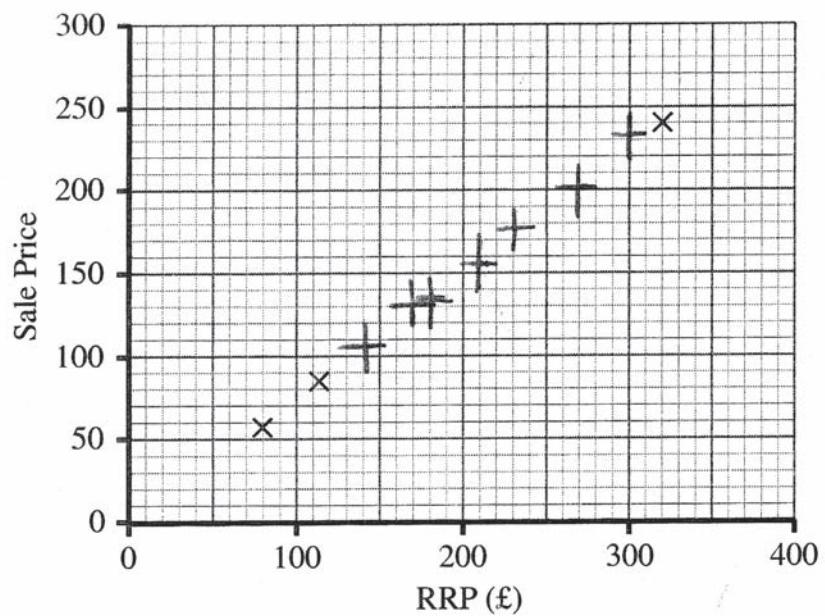
			AVAILABLE MARKS
1	2, -3	A1, A1	2
2	$120/(8 \times 5) = 3$	M1, A1	2
3	See overlay $90^\circ, 60^\circ, 54^\circ, 30^\circ, 126^\circ$ (award one mark for evidence of $\frac{360}{60}$ or 6) All sectors correct and labelled	A2 A2	4
4	(a) -4	A1	
	(b) graph	M1, A1	3
5	(a) 25×8 $= 200$	MA1 A1	
	(b) 0.08	MA1	
	(c) 2.77	MA1	
	(d) $\frac{7}{12} - \frac{2}{12}$ $= \frac{5}{12}$	MA1 A1	6
6	(a) Scatter graph allow A1 for 4 correct	A2	
	(b) oblique line with roughly half the points on either side	A1	
	(c) follow line	A1	
	(d) positive	A1	5
7	(a) $p(p + 7)$	MA1	
	(b) $n^2 - 3 = 78$ $n^2 = 81$ $n = 9$	M1 A1	3

				AVAILABLE MARKS																
8	(a) $\text{AOB} = 360/5 = 72$		M1, A1																	
	(b) $\text{ABC} = 180 - 72 = 108$		M1, A1	4																
9	$\begin{aligned} \frac{3}{4} \times 9 \\ = \frac{27}{4} = 6\frac{3}{4} \\ = 7 \text{ bottles} \end{aligned}$		MA1 MA1 A1	3																
10	Polygon, see overlay Correct frequencies at mid-points Points joined by straight lines		MA1 MA1	2																
11	$\begin{array}{r c} 2 & 80 \\ \hline 2 & 40 \\ \hline 2 & 20 \\ \hline 2 & 10 \\ \hline 5 & 5 \\ \hline & 1 \end{array}$ $= 2^4 \times 5$		M1 A1 MA1	3																
12	(a) Now: Jack = x Dan = $x - 5$ $3 \text{ years time } x + 3 + x - 5 + 3 = 15$ (or equivalent)		A1 MA1																	
	(b) $x = 7$		A1	3																
13	<table border="1"> <thead> <tr> <th>Mid-Points</th> <th>fx</th> </tr> </thead> <tbody> <tr> <td>57</td> <td>57</td> </tr> <tr> <td>62</td> <td>62</td> </tr> <tr> <td>67</td> <td>134</td> </tr> <tr> <td>72</td> <td>360</td> </tr> <tr> <td>77</td> <td>693</td> </tr> <tr> <td>82</td> <td>410</td> </tr> <tr> <td>87</td> <td>174</td> </tr> </tbody> </table>	Mid-Points	fx	57	57	62	62	67	134	72	360	77	693	82	410	87	174		MA1 M1 MA1 MA1	4
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57	57																			
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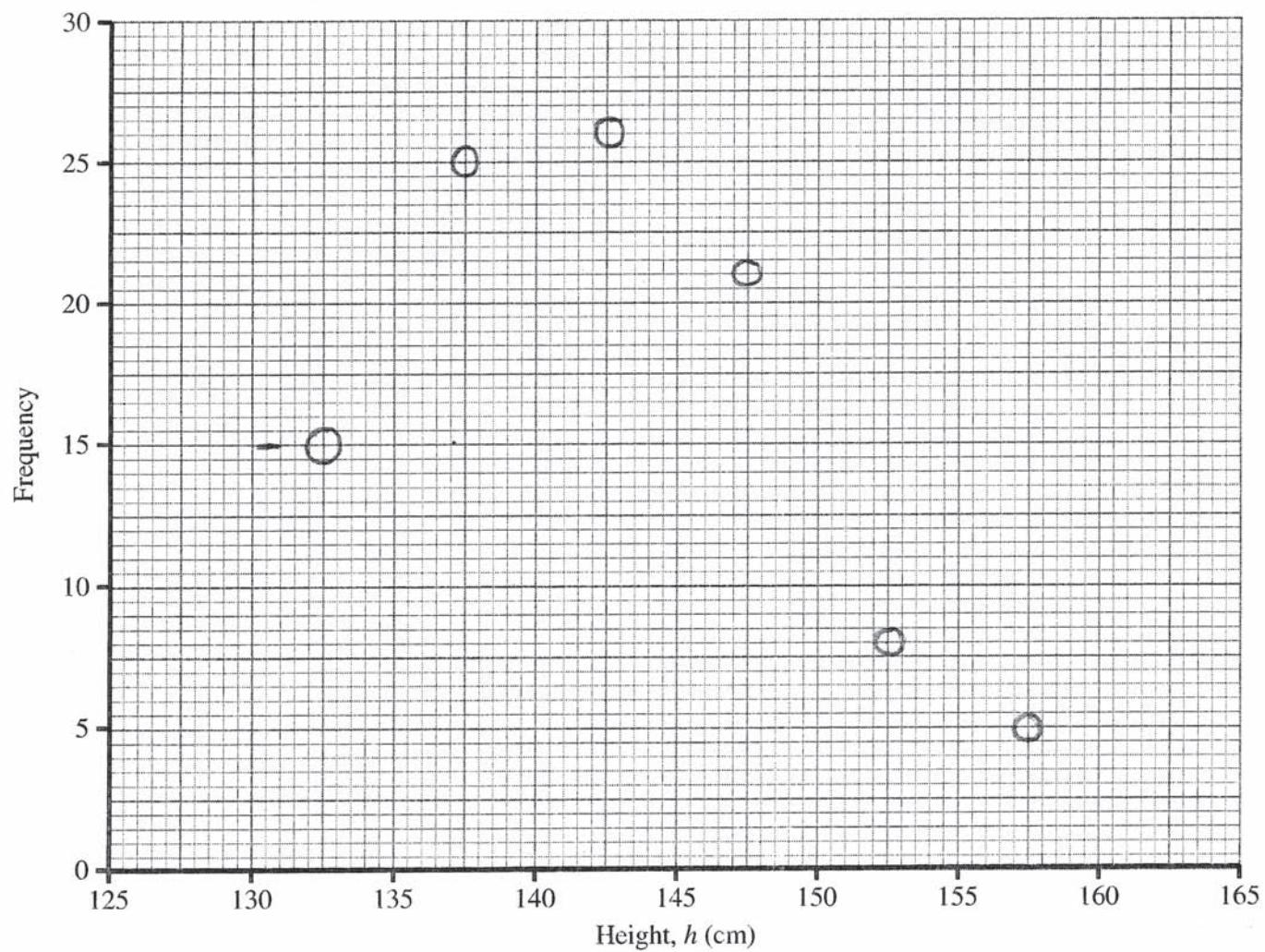
GCSE MATHEMATICS SUMMER 2009
MODULE N2-1
OVERLAY QUESTION 3



GCSE MATHEMATICS SUMMER 2009
MODULE N2-1
OVERLAY QUESTION 6



GCSE MATHEMATICS SUMMER 2009
MODULE N2-1
OVERLAY QUESTION 10





General Certificate of Secondary Education
Summer 2009

Mathematics

Module N2 Paper 2
(With calculator)
Foundation Tier

[GMN22]

MONDAY 18 MAY
2.45 pm – 3.30 pm

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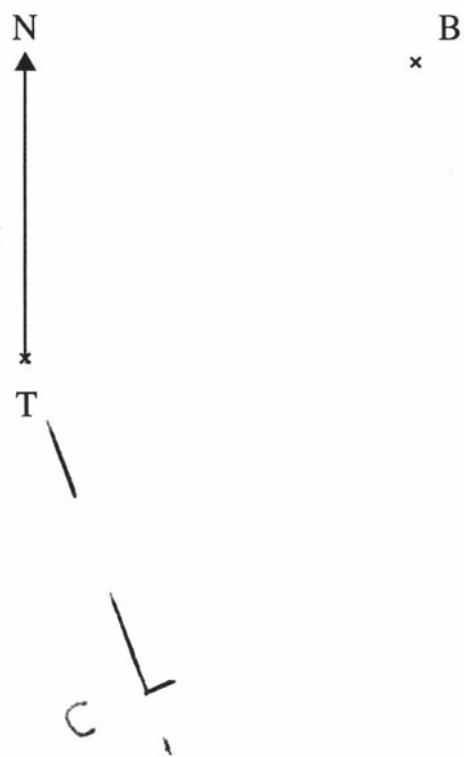
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			AVAILABLE MARKS
1 Girls	A1		
Boys' mean = $\frac{130}{10} = 13$	M1, A1		
Girls' mean = $\frac{128}{8} = 16$	MA1	4	
2 (a) $\frac{1}{4}$ of £600 = £150 or $\frac{1}{4} + \frac{1}{6}$	MA1		
$\frac{1}{6}$ of £600 = £100 or $\frac{3}{12} + \frac{2}{12} = \frac{5}{12}$	MA1		
Total = £250			
Remainder = £600 - £250 = £350 or Remainder = $1 - \frac{5}{12}$	MA1		
Fraction = $\frac{350}{600}$ or $\frac{7}{12}$	MA1		
(b) $\left(\frac{2}{10} = \frac{24}{120} \right)$	MA1		
$\frac{3}{20} = \frac{18}{120}$	(same fractions or decimal form)		
$\frac{7}{30} = \frac{28}{120}$			
$\frac{11}{40} = \frac{33}{120}$			
\therefore Ans $\frac{7}{30}$	MA1 selection/reason	6	
3 (a) (i) 053° or N 53° E ($\pm 2^\circ$)	A1		
(ii) distance 4.5 cm (± 2 mm)	A1		
bearing 160° ($\pm 2^\circ$)	A1		
(b) (i) 80°	MA1		
(ii) $180 - 80 = 100$	MA1		
$100 \div 2 = 50$	MA1	6	
4 Suitable answer, e.g. sample is made up totally of young people/teenagers etc. sample does not represent all age groups etc.	A1	1	
5 (a) $y = 18$	MA1		
(b) $8a + 12 - 7$ $= 8a + 5$	MA1 A1	3	

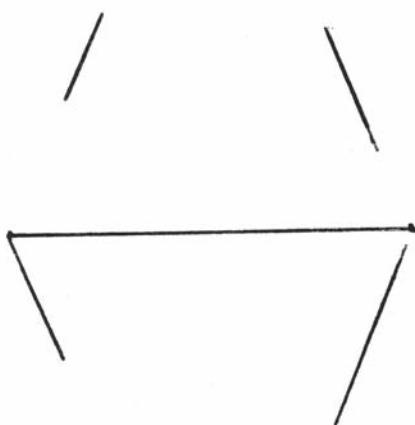
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15	3	7	8																							
16	2	3	6	7	7	7	8	9																		
17	0	1	4	7	8	8																				
18	1	2	5																							
	Key: 15 7 means 157 cm	MA1																								
7	diagonal 5 cm (± 2 mm)	A1																								
	Arcs 6.5 cm (± 2 mm) above and below diagonal	A1, A1																								
	Rhombus completed	A1																								
8	$\frac{35}{100} \times 640$ $= £224$ $640 - 224 = £416$	M1 A1 MA1																								
9	$25^2 = 7^2 + x^2$	MA1																								
	$625 = 49 + x^2$																									
	$576 = x^2$	MA1																								
	BC = 24 cm	MA1																								
10	4 minute 35 sec = 275 seconds	MA1																								
	$\frac{275}{25} = 11$ buckets	MA1																								
	$11 \times 15 = 165$ litres	MA1, A1 units																								
11	$1\text{st yr interest} = \frac{4}{100} \times 2500 = £100$ value yr 1 = £2600 $2\text{nd yr interest} = \frac{4}{100} \times 2600 = £104$ value yr 2 = £2704 $3\text{rd yr interest} = \frac{4}{100} \times 2704 = £108.16$ value yr 3 = £2812.16	MA1 MA1 MA1 MA1 MA1																								
		3																								

			AVAILABLE MARKS
12	$x = 4$	56	
	$x = 3$	21	MA1
	$x = 3.6$	39.456	
	$x = 3.7$	43.253	MA1
	$x = 3.65$	41.327...	MA1
	$x = 3.6$		A1 4
			Total 44

GCSE MATHEMATICS SUMMER 2009
MODULE N2-2
OVERLAY QUESTION 3



GCSE MATHEMATICS SUMMER 2009
MODULE N2-2
OVERLAY QUESTION 7





General Certificate of Secondary Education
Summer 2009

Mathematics

Module N5 Paper 1
(Non-calculator)
Foundation Tier

[GMN51]

MONDAY 1 JUNE

9.15 am – 10.15 am

MARK SCHEME

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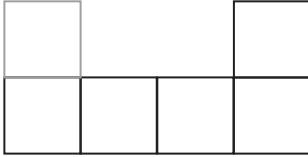
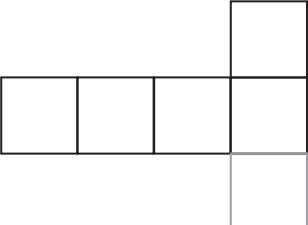
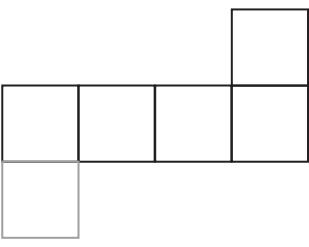
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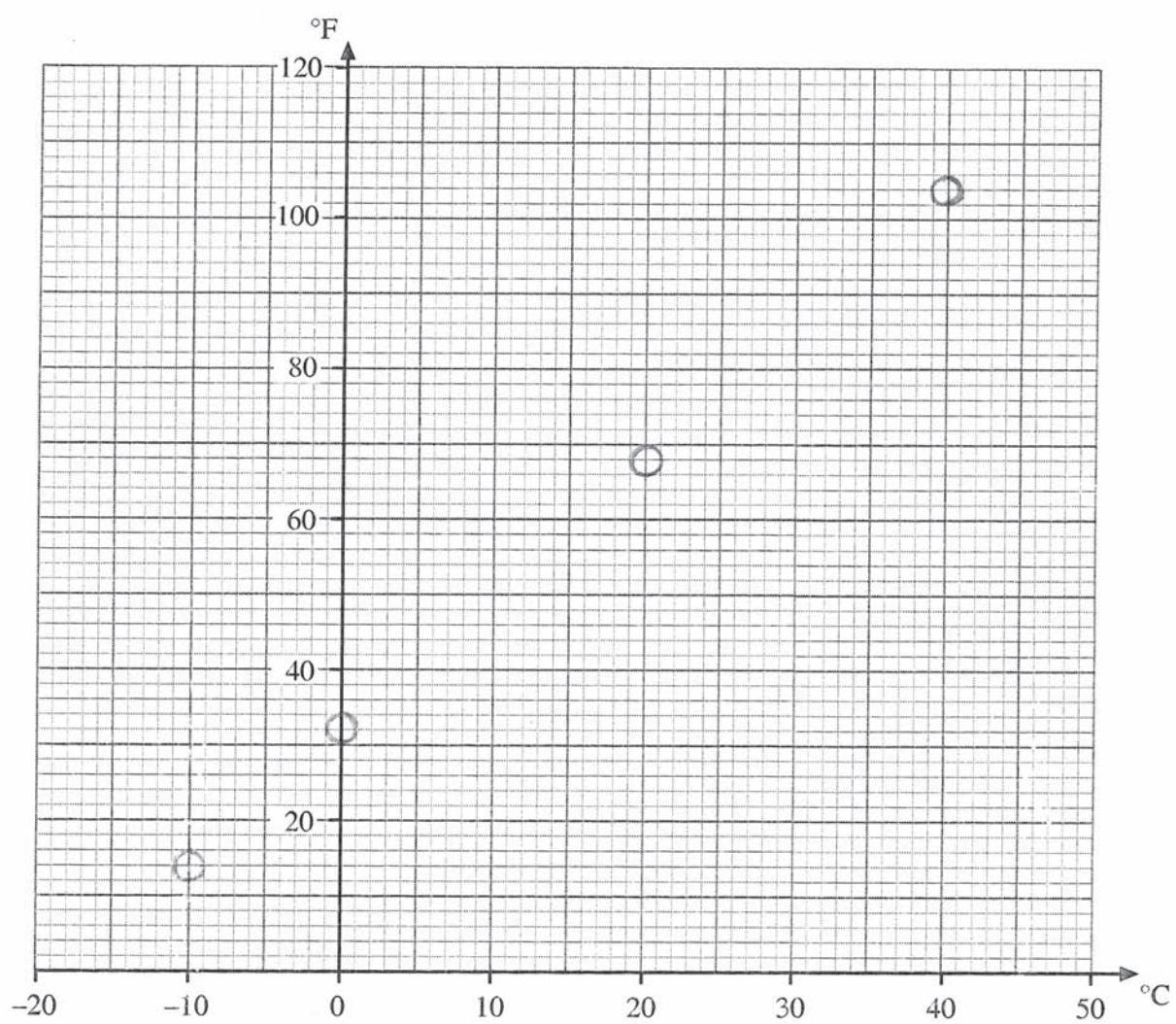
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		AVAILABLE MARKS
1	(a) sphere	A1
	(b) cylinder	A1
	(c) cone	A1
		3
2	(a) each line	A1, A1
	(b) correct shape and orientation, distance from mirror line	A1, A1
		4
3	(a) even + suitable reason	A1
	(b) (very) unlikely + suitable reason	A1
	(c) certain + suitable reason	A1
		3
4	$20 \times 4\frac{1}{2} + 40$	M1
	$= 130$	A1
		2
5	(a) (i) 5390	A1
	(ii) 5400	A1
	(b) (i) $100 \times 5 = 500$	M1, A1
	(ii) $\frac{18}{4} \rightarrow 4$	M1, A1
		6
6	(a) $15.00 - 5 = 10.00$ am	A1
	(b) $5.00 + 11 = 16.00 = 4.00$ pm	A1
		2

			AVAILABLE MARKS
7	(a) each correct pair (b) 4 (c)	A1, A1 A1 A1	
		or	
			
(d)		A1	5
8	(a) (i) 11 (ii) 14 (b) 6 and 7 (c) divide 80 by 2 or similar	A1 A1 A1 A1	
9	(a) 4 points plotted correctly (2 points plotted correctly A1) straight line drawn (b) (i) 86°F (ii) -7°C	A2 A1 A1 A1 A1	4 5

		AVAILABLE MARKS
10 (a) correct enlargement	A2	
(b) 9	A2	4
11 4, 16; 4, 36; 9, 25; etc	A2 (only)	2
12 (a) black	A1	
(b) red	A1	
(c) $0.15 \times 600 = 90$	M1, A1	4
13 $2n \times 2n$ $= 4n^2$ which can be divided by 4	MA1 MA1	2
14 (a) (i) enlargement scale factor 2 centre (1, 2) (ii) rotation 90° clockwise about (0, -2)	MA3 MA3	
(b) image moved 1 unit right and 5 down	MA1 MA1	8
15 $v - u = gt$ $g = \frac{v - u}{t}$	MA1 MA1	2
	Total	56

GCSE MATHEMATICS SUMMER 2009
MODULE N5-1
OVERLAY QUESTION 9





General Certificate of Secondary Education
2009

Mathematics

Module N5 Paper 2
(With calculator)
Foundation Tier

[GMN52]

MONDAY 1 JUNE

10.45 am – 11.45 am

MARK SCHEME

GCSE MATHEMATICS 2009

Introduction

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			AVAILABLE MARKS
1	(a) 41	A1	
	(b) arrow	A1	2
2	(a) 8	A1	
	(b) 5	A1	
	(c) 4	A1	3
3	$200 \times 45\text{p} = \text{£}90$ $80 \times 60\text{p} = \text{£}48$ total £138	MA1 M1, A1 MA1	4
4	$250 + 4 \times 45$ 430	M1 A1	2
5	(a) $24 \times 5.6 = 134.4$ $\frac{1}{2}$ (accuracy)	M1, A1 A1	
	(b) Suitable reason (real-life)	A1	4
6	(a) 1/13	A1	
	(b) 12/13	A1	
	(c) $7/13 + 1/13 = 8/13$	M1, A1	4
7	(a) $2 \times 10 + 2 \times 4$ = 28	MA1 A1	
	(b) $10 \times 4 = 40$	MA1	3
8	$40 \times \text{£}15.20 = \text{£}608$ $\text{£}430 + \text{£}608 = \text{£}1038$ $\text{£}40 \times 24 = \text{£}960$ $\text{£}1038 - \text{£}960 = \text{£}78$	MA1 M1, A1 M1, A1 MA1	6

							AVAILABLE MARKS																														
9	(a)	4 lines correct (3 lines correct (2 lines correct			A3 A2) A1																																
	(b)	$40 \times 5/8 = 25$			MA1, A1																																
	(c)	$1 \text{ litre} = 1.75 \text{ pints}$ $7 \text{ pints} = 7/1.75 = 4$			A1 MA1		7																														
10	(a)	B			A1																																
	(b)	C			A1																																
	(c)	G			A1		3																														
11	(a)	he has stopped			A1																																
	(b)	24 km			A1																																
	(c)	$12 \div 1\frac{1}{2}$ $= 8 \text{ km/hr}$			M1 A1		4																														
12	(a)	<table border="1"> <tr><td></td><td></td><td></td><td></td><td></td><td></td></tr> <tr><td>3</td><td>5</td><td>7</td><td>9</td><td>11</td><td>13</td></tr> <tr><td>5</td><td>7</td><td>9</td><td>11</td><td>13</td><td>15</td></tr> <tr><td>7</td><td>9</td><td>11</td><td>13</td><td>15</td><td>17</td></tr> <tr><td>9</td><td>11</td><td>13</td><td>15</td><td>17</td><td>19</td></tr> </table>												3	5	7	9	11	13	5	7	9	11	13	15	7	9	11	13	15	17	9	11	13	15	17	19
3	5	7	9	11	13																																
5	7	9	11	13	15																																
7	9	11	13	15	17																																
9	11	13	15	17	19																																
		Allow A1 for at least 12 correct entries																																			
	(b)	$6/24 \text{ or } 1/4 \text{ or } 0.25 \text{ or } 25\%$																																			
		M1, A1																																			

			AVAILABLE MARKS
13	$(4/25) \times 200$ 32	MA1 A1	2
14	$1\frac{1}{2} \times 20 = 30$ $1\frac{1}{2} \times 36 = 54$ $1\frac{1}{2} \times 52 = 78$	MA1 MA1 MA1	3
15	(a) t^6 (b) r^4	A1 A1	2
16	$\text{£}180 \div 15 = \text{£}12$ (Mikey) $\text{£}12 \times 8 = \text{£}96$ (Lisa) $\text{£}12 \times 6 = \text{£}72$ (Richard)	MA1 MA1 MA1	3
Total			56



General Certificate of Secondary Education
Summer 2009

Mathematics

Module N3 Paper 1
(Non-calculator)
Higher Tier

[GMN31]

MONDAY 18 MAY

1.30 pm – 2.30 pm

MARK SCHEME

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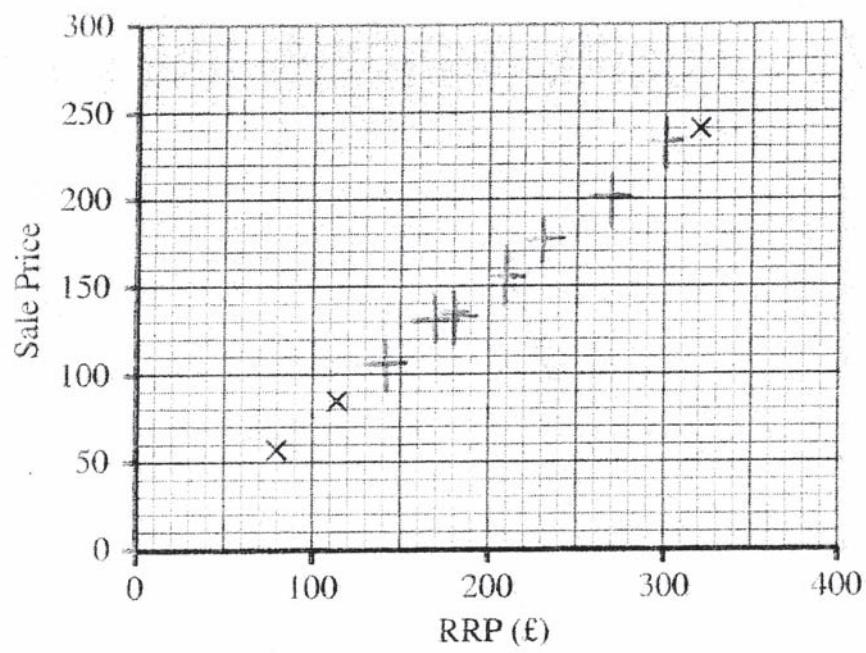
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			AVAILABLE MARKS
1	70	M1, A1	2
2	$\frac{3}{4} \times 9$ $\frac{27}{4} = 6\frac{3}{4}$ = 7 bottles	M1 MA1 A1	3
3	$500 - 42y$	A1, A1	2
4	(a) scatter graph (Allow A1 for 4 correct)	A2	
	(b) oblique line with roughly half the points on either side	A1	
	(c) follow pupil's line	A1	
	(d) positive	A1	5
5	(a) $\text{AOB} = \frac{360}{5} = 72$	M1A1	
	(b) $\text{ABC} = 180 - 72 = 108$	M1A1	4
6	$n^2 - 3 = 78$ $n^2 = 81$ $n = 9$	M1 A1	2
7	polygon, see overlay correct frequencies at mid-points points joined by straight lines	MA1 MA1	2
8	$ \begin{array}{r} 2 \mid 80 \\ 2 \mid 40 \\ 2 \mid 20 \\ 2 \mid 10 \\ 5 \mid 5 \\ \hline 1 \end{array} $ $= 2^4 \times 5$	M1 A1 MA1	3

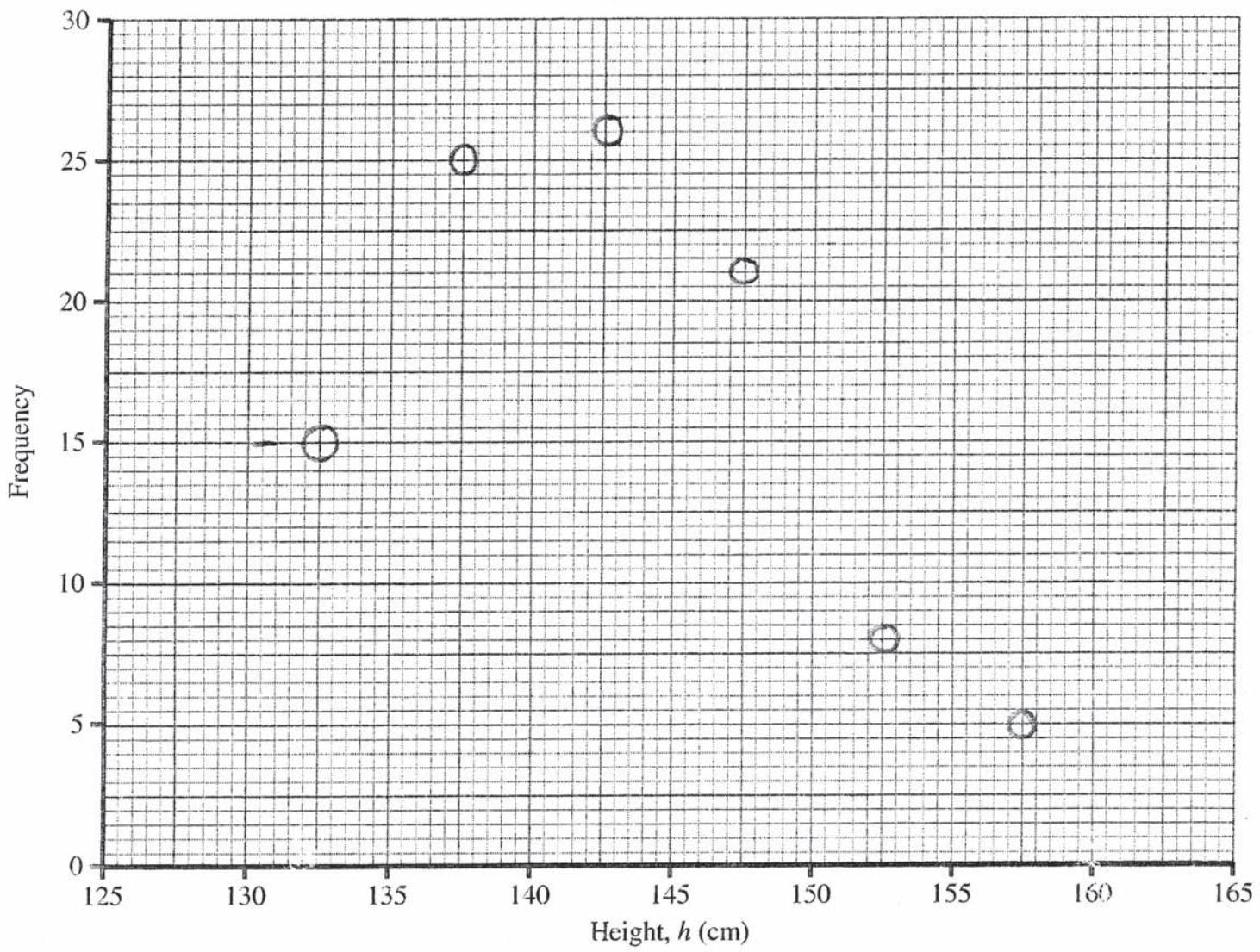
			AVAILABLE MARKS																
9	(a) now: Jack = x Dan = $x - 5$ 3 years time $x + 3 + x - 5 + 3 = 15$ (or equivalent)	A1 MA1																	
	(b) $x = 7$	A1	3																
10	<table border="1" style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="text-align: left;">Mid-Points</th> <th style="text-align: right;">fx</th> </tr> </thead> <tbody> <tr><td style="text-align: left;">57</td><td style="text-align: right;">57</td></tr> <tr><td style="text-align: left;">62</td><td style="text-align: right;">62</td></tr> <tr><td style="text-align: left;">67</td><td style="text-align: right;">134</td></tr> <tr><td style="text-align: left;">72</td><td style="text-align: right;">360</td></tr> <tr><td style="text-align: left;">77</td><td style="text-align: right;">693</td></tr> <tr><td style="text-align: left;">82</td><td style="text-align: right;">410</td></tr> <tr><td style="text-align: left;">87</td><td style="text-align: right;">174</td></tr> </tbody> </table>	Mid-Points	fx	57	57	62	62	67	134	72	360	77	693	82	410	87	174		
Mid-Points	fx																		
57	57																		
62	62																		
67	134																		
72	360																		
77	693																		
82	410																		
87	174																		
	mid-points fx products 1890 75.6	MA1 M1 MA1 MA1	4																
11	(a) $6x^2 + 3x - 4x - 2$ $= 6x^2 - x - 2$	MA1 A1																	
	(b) $4x = 24$ $x = 6$ $y = 2$	MA1 A1	4																
12	(a) 90	MA1																	
	(b) 130	MA1																	
	(c) 100	MA1	3																
13	$2\frac{1}{5} \div 1\frac{2}{3}$ $\frac{11}{5} \div \frac{5}{3}$ $\frac{11}{5} \times \frac{3}{5}$ $\frac{33}{25} \left(= 1\frac{8}{25}\right)$	MA1 MA1 A1	3																

		AVAILABLE MARKS
14	$5(2x + 1) - 3(x + 1) = 45$ $10x + 5 - 3x - 3 = 45$ $7x + 2 = 45$ $7x = 45 - 2$ $7x = 43$ $x = \frac{43}{7}$ or $6\frac{1}{7}$	MA1 MA1 MA1 A1
		4
	Total	44

GCSE MATHEMATICS SUMMER 2009
MODULE N3-1
OVERLAY QUESTION 4



GCSE MATHEMATICS SUMMER 2009
MODULE N3-1
OVERLAY QUESTION 7





General Certificate of Secondary Education
Summer 2009

Mathematics

Module N3 Paper 2
(With calculator)
Higher Tier

[GMN32]

MONDAY 18 MAY

2.45 pm – 3.45 pm

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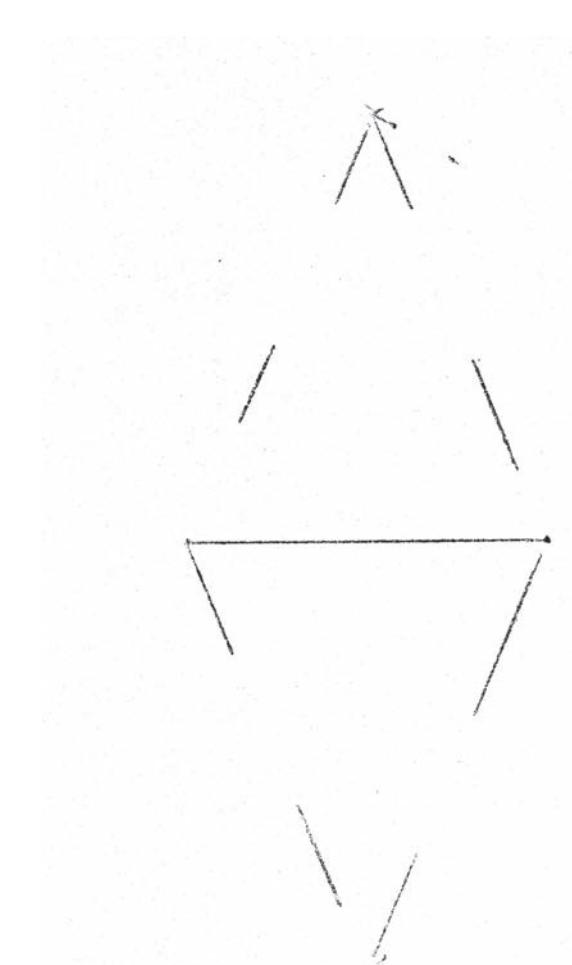
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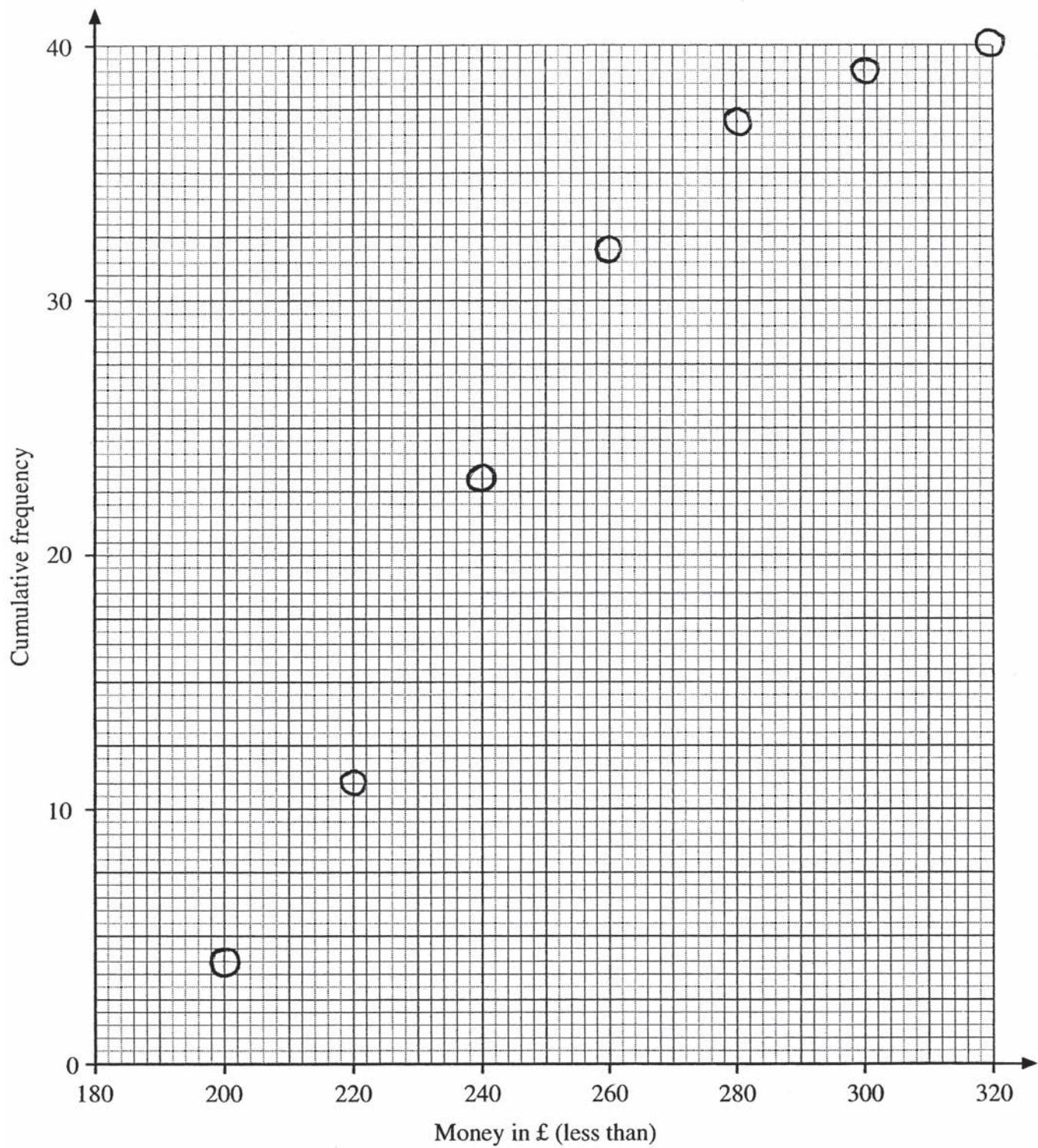
				AVAILABLE MARKS
1	$(\frac{1}{2}, -1)$	A1A1	2	
2	$\begin{array}{c ccccccccc} 15 & 3 & 7 & 8 \\ 16 & 2 & 3 & 6 & 7 & 7 & 7 & 8 & 9 \\ 17 & 0 & 1 & 4 & 7 & 8 & 8 \\ 18 & 1 & 2 & 5 \end{array}$	M1A1		
	Key: 15 7 means 157 cm	MA1	3	
3	$35\% \text{ of £}640 = \frac{35}{100} \times 640$ $= \text{£}224$ $\text{s.p.} = \text{£}640 - \text{£}224 = \text{£}416$	M1 A1 MA1	3	
4	Diagonal 5 cm (± 2 mm) Arcs 6.5 cm (± 2 mm) above and below diagonal Rhombus completed	A1 A1A1 A1	4	
5	Suitable answer, e.g. sample is made up totally of young people/teenagers etc. sample does not represent all age groups etc.	A1	1	
6	(a) $8a + 12 - 7$ $= 8a + 5$	MA1 A1		
	(b) (i) $2(3a - 5)$	MA1		
	(ii) $a(a + 1)$	MA1	4	
7	4 minutes 35 sec = 275 seconds	MA1		
	$\frac{275}{25} = 11$ buckets	MA1		
	$11 \times 15 = 165$ litres	MA1A1 units	4	
8	$x = 4$ 56 $x = 3$ 21 $x = 3.6$ 39.456 $x = 3.7$ 43.253 $x = 3.65$ 41.327... $x = 3.6$	MA1 MA1 MA1 MA1 A1	4	

			AVAILABLE MARKS										
9	$1\text{st yr Int} = \frac{4}{100} \times 2500 = £100$ $\text{Value yr } 1 = 2500 + 100 = £2600$ $2\text{nd yr Int} = \frac{4}{100} \times 2600 = £104$ $\text{Value yr } 2 = 2600 + 104 = £2704$ $3\text{rd yr Int} = \frac{4}{100} \times 2704 = £108.16$ $\text{Value yr } 3 = £2812.16$	MA1 MA1 MA1 MA1	3										
10	(a) $25^2 = 7^2 + x^2$ $625 = 49 + x^2$ $576 = x^2$ $BC = 24 \text{ cm}$ (b) $\cos BAC = \frac{7}{25}$ $BAC = 73.74$	MA1 MA1 MA1 M1A1 MA1	6										
11	$220 = 88\%$ $\frac{220}{88} = 1\% = 2.5$ $\frac{220}{88} \times 100 = 100\% = 250$	M1 A1 MA1	3										
12	(a) <table style="margin-left: auto; margin-right: auto;"><tr><td></td><td>23</td></tr><tr><td>< 260</td><td>32</td></tr><tr><td>< 280</td><td>37</td></tr><tr><td>< 300</td><td>39</td></tr><tr><td>< 320</td><td>40</td></tr></table> (b) points plotted correctly smooth curve (c) (i) 235 (follow pupil's curve) (ii) $256 - 217$ (follow pupil's curve) 39		23	< 260	32	< 280	37	< 300	39	< 320	40	A1 M1A1 A1 MA1 MA1 A1 Total	7 44
	23												
< 260	32												
< 280	37												
< 300	39												
< 320	40												

GCSE MATHEMATICS SUMMER 2009
MODULE N3-2
OVERLAYS QUESTION 4



GCSE MATHEMATICS SUMMER 2009
MODULE N3-2
OVERLAYS QUESTION 12





General Certificate of Secondary Education
2009

Mathematics

Module N4 Paper 1
(Non-calculator)
Higher Tier

[GMN41]

MONDAY 18 MAY

1.30 pm – 2.30 pm

MARK SCHEME

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		MA1	AVAILABLE MARKS
		A1	
1	(a) $6x^2 + 3x - 4x - 2$ $= 6x^2 - x - 2$	MA1 A1	
	(b) $4x = 24$ $x = 6$ $y = 2$	MA1 A1	4
2	$\frac{11}{5} \div \frac{5}{3}$ $\frac{11}{5} \times \frac{3}{5}$ $\frac{33}{25} \left(= 1\frac{8}{25}\right)$	MA1 MA1 A1	3
3	$5(2x + 1) - 3(x + 1) = 45$ $10x + 5 - 3x - 3 = 45$ $7x + 2 = 45$ $7x = 45 - 2$ $7x = 43$ $x = \frac{43}{7}$ or $6\frac{1}{7}$	MA1 MA1 MA1 A1	4
4	0.80 left after 1 yr 0.8^2 left after 2 yrs = 0.64 0.8^3 left after 3 yrs = 0.512 → 51.2%	M1 A1	2
5	(a) 90 (b) 130 (c) 100 (d) 70	MA1 MA1 MA1 MA2	5
6	(a) $(x - 2)(x + 2)$ (b) $\frac{(x - 2)(x + 2)}{(2x + 3)(x - 2)}$ $= \frac{x + 2}{2x + 3}$	A1 MA2 A1	4
7	Mode because it is the one he needs to order most of or other suitable reason	A1 A1	2

			AVAILABLE MARKS
8	$y = -\frac{1}{3}x + 2$	A1, A1	2
9	(a) $\frac{(3)^3}{27}$	M1 A1	
	(b) $\frac{1}{81^{\frac{1}{2}}}$	M1	
	$\frac{1}{9}$	A1	4
10	(a) Frequency per unit interval 18, 56, 68, 8, 8 and correctly drawn, correct vertical scale or key	MA1, A1 A1	
	(b) (i) $\frac{20}{80} \times 28$	MA1	
	7	A1	
	(ii) $\frac{1}{2}(80) = 40$		
	$40 + 16 + 4 = 60$	M1, A1	7
11	$3x + 2(x^2 + 3x - 2) = 22$	MA2	
	$3x + 2x^2 + 6x - 4 = 22$	MA1	
	$2x^2 + 9x - 26 = 0$	MA1	
	$(2x + 13)(x - 2) = 0$	MA1	
	$x = -6\frac{1}{2}$ or $x = 2$	MA1	
	$y = 20\frac{3}{4}$ or $y = 8$	A1	7
		Total	44



General Certificate of Secondary Education
2009

Mathematics

Module N4 Paper 2
(With calculator)
Higher Tier

[GMN42]

MONDAY 18 MAY

2.45 pm – 3.45 pm

MARK SCHEME

GCSE MATHEMATICS 2009

Introduction

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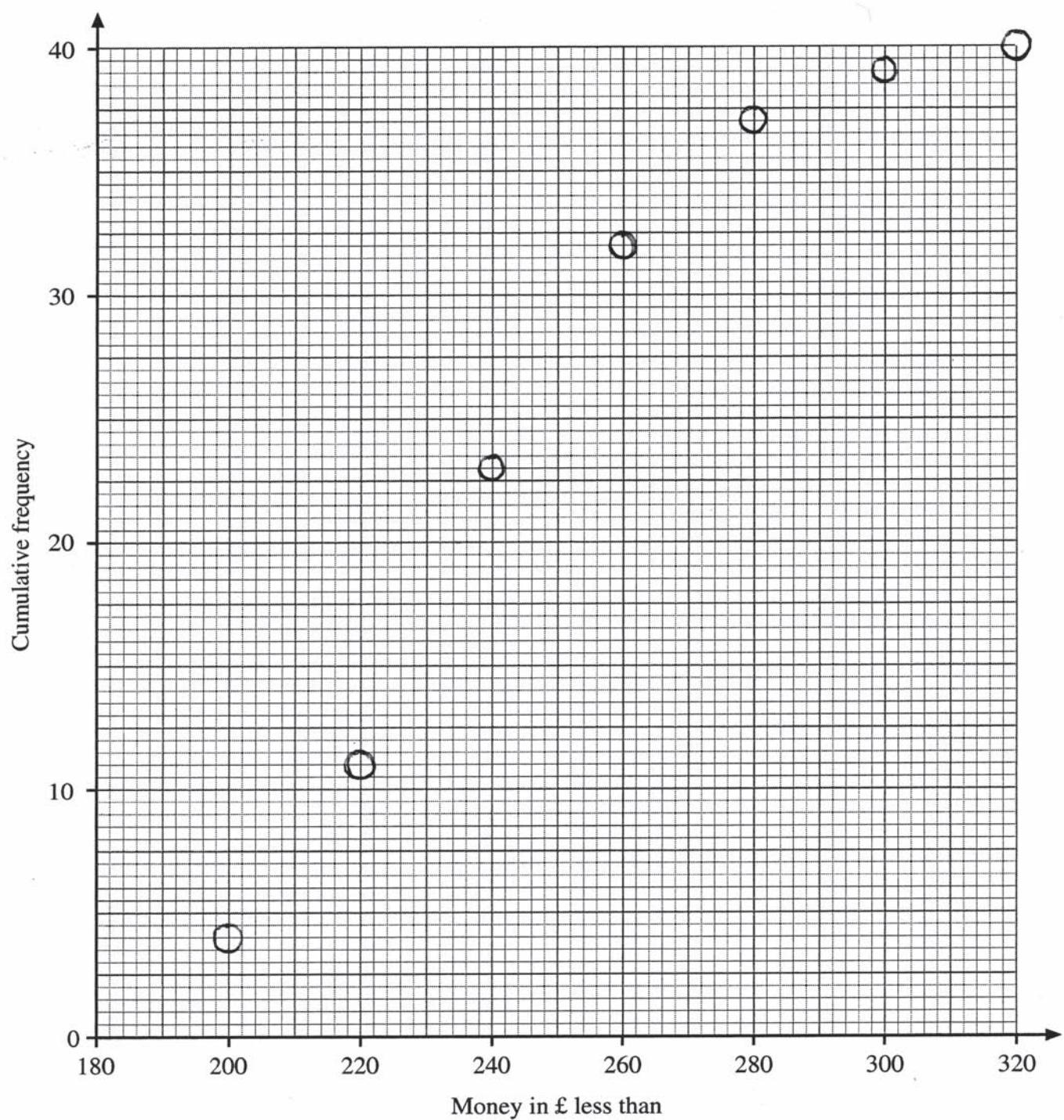
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				AVAILABLE MARKS
1	Volume of sphere = $\frac{4}{3}\pi r^3 = \frac{4}{3}\pi(35)^3$ = 179 594.38 cm ³ (180 000)		MA1 A1, A1 units	3
2	(a) 23 < 260 32 < 280 37 < 300 39 < 320 40		A1	
	(b) points plotted correctly smooth curve/lines		MA2 A1	
	(c) (i) 235 (follow pupil's curve)		MA1	
	(ii) 256 – 217 (follow pupil's curve) 39		MA1 A1	
	(iii) from graph		M1, A1	
	(d) Median at 235 (follow pupil's curve) Quartiles at 217 and 256 (follow pupil's curve) Range: Start 185, End 315		MA1 MA1 MA1	12
3	Discrete data is counted, continuous data is measured etc. Suitable example of each		A1 A1	2
4	(a) $BD^2 = 8^2 + 10^2 - 2 \times 8 \times 10 \cos 80^\circ = 136.216\dots$ $BD = 11.67$		M1, A1 MA1	
	(b) Area = $\frac{1}{2} \times 5 \times 11.67 \sin 22^\circ = 10.93$		M1, A1	5
5	(a) $x^2 + (x + 8)^2 = 144$ $x^2 + x^2 + 16x + 64 - 144 = 0$ $2x^2 + 16x - 80 = 0$ $x^2 + 8x - 40 = 0$		MA1 MA1 MA1	
	(b) $x = \frac{-8 \pm \sqrt{64 + 160}}{2}$		MA1	
	$x = \frac{-8 \pm 14.96663}{2}$		A1	
	$x = 3.48$		A1	6

		AVAILABLE MARKS
6	(a) $\frac{DE}{EB} = \frac{BC}{AC}$ $\frac{DE}{14} = \frac{24}{7}$ DE = 48 cm	MA1 MA1
	(b) Volume of original cone = $\frac{1}{3}\pi r^2 h = \frac{1}{3}\pi(21)^2(72)$ Volume of cone removed = $\frac{1}{3}\pi r^2 h = \frac{1}{3}\pi(14)^2(48)$ Volume of frustum = $\frac{1}{3}\pi(21)^2(72) - \frac{1}{3}\pi(14)^2(48)$ = 33251 - 9852 = 23399	MA1 MA1 M1 A1
		6
7	(a) suitable example, e.g. 3 (b) suitable example, e.g. 2 (c) suitable example, e.g. -1	A1 A1 A1
		3
8	$(x + b)^2 = x^2 + 2bx + b^2$ $2b = -10 \quad b = -5$ $b^2 = c \quad c = 25$	MA1 MA1 MA1
		3
9	angle DAJ AD = 40 cm $\tan^{-1} \frac{30}{40}$ = 36.9	M1 MA1 MA1 A1
		4
	Total	44

GCSE MATHEMATICS SUMMER 2009
MODULE N4-2
OVERLAY QUESTION 2





General Certificate of Secondary Education
Summer 2009

Mathematics
Module N6 Paper 1
(Non-calculator)
Higher Tier
[GMN61]

MONDAY 1 JUNE
9.15 am – 10.30 am

**MARK
SCHEME**

GCSE MATHEMATICS 2009

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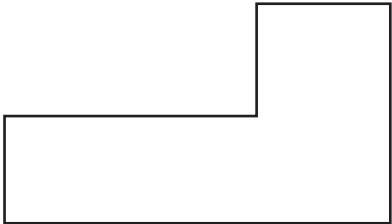
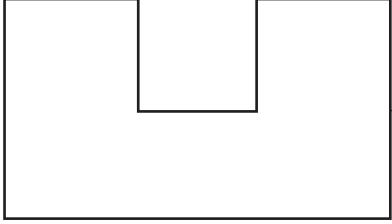
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			AVAILABLE MARKS
1	(a) $1 - 0.8 = 0.2$	M1, A1	
	(b) $0.15 \times 600 = 90$	M1, A1	4
2	$\frac{(2 - 12) \times (-4)}{8}$ $= \frac{40}{8}$	MA1 A1	
	$= 5$	A1	3
3	(a)		
		A2	
	(b)		
		A2	4
4	(a) (i) $\frac{5 \times 30}{(9-7)} = \frac{5 \times 30}{2} = 75$	MA1, MA1	
	(ii) $\sqrt{90\,000 / 100} = \sqrt{900} = 30$	M1, A2	
	(b) 15 800	A1	6

				AVAILABLE MARKS
5	(a) enlargement	scale factor 2	centre (1,2)	MA1, MA1, MA1
	(b) reflection	in the line $y = x$		MA1, MA1
	(c) rotation	90° clockwise	about (0, -2)	MA1, MA1, MA1
				8
6	(a) $v - u = gt$			MA1
	$g = \frac{v - u}{t}$			MA1
	(b) $-7 < 3n \leq 9$			MA1
	$-2\frac{1}{3} < n \leq 3$			MA1
	$n = -2, -1, 0, 1, 2, 3$			A2
				6
7	70°			A1
				1
8	(a) $2n \times 2n$			MA1
	$4n^2$ which can be divided by 4			MA1
	(b) any negative number ≤ -1			A1
	(c) $n^2 - n + n - 1 + 2n - 2n + 2 - n^2$	along with suitable indication of completion to = 1	A1	A1
				5
9	(a) 3.6714×10^8			A1
	(b) 5.972×10^{-5}			A1
	(c) $18 \times 10^{-7} = 1.8 \times 10^{-6}$		A1, A1	4
10	(a) 0.3, 0.4, 0.6, 0.4			A1
	(b) $0.7 \times 0.4 + 0.3 \times 0.6 = 0.28 + 0.18 = 0.46$		M1, A1	3
11	(a) $(2\sqrt{2} + 3\sqrt{2})^2$ $= (5\sqrt{2})^2 = 25 \times 2$ 50	$8 + 6\sqrt{16} + 18$ $8 + 24 + 18$ 50	MA1 A1	
	(b) $f = 3.4545\dots$ $100f = 345.4545\dots$ $99f = 342$ $f = \frac{342}{99} \left(= \frac{38}{11}\right)$		M1, A1 A1	5

		AVAILABLE MARKS
12	(a) $\left(\frac{3}{12}\right) \times \left(\frac{2}{11}\right)$	M1, A1
	$\frac{6}{132}$ or $\frac{1}{22}$	A1
(b)	$\left[\left(\frac{3}{12}\right) \times \left(\frac{2}{11}\right) \times \left(\frac{9}{10}\right) \right] + \left[\left(\frac{7}{12}\right) \times \left(\frac{6}{11}\right) \times \left(\frac{5}{10}\right) \right]$ $+ \left[\left(\frac{2}{11}\right) \times \left(\frac{1}{11}\right) \times \left(\frac{10}{10}\right) \right]$ $\left(\frac{54}{1320} \right) + \left(\frac{210}{1320} \right) + \left(\frac{20}{1320} \right)$ $= \frac{284}{1320} \text{ or } \frac{71}{330} \text{ or } 0.215151\dots$	M1, A1 A2
		7
	Total	56



General Certificate of Secondary Education
Summer 2009

Mathematics

Module N6 Paper 2
(With calculator)
Higher Tier

[GMN62]

MONDAY 1 JUNE
10.45 am – 12.00 noon

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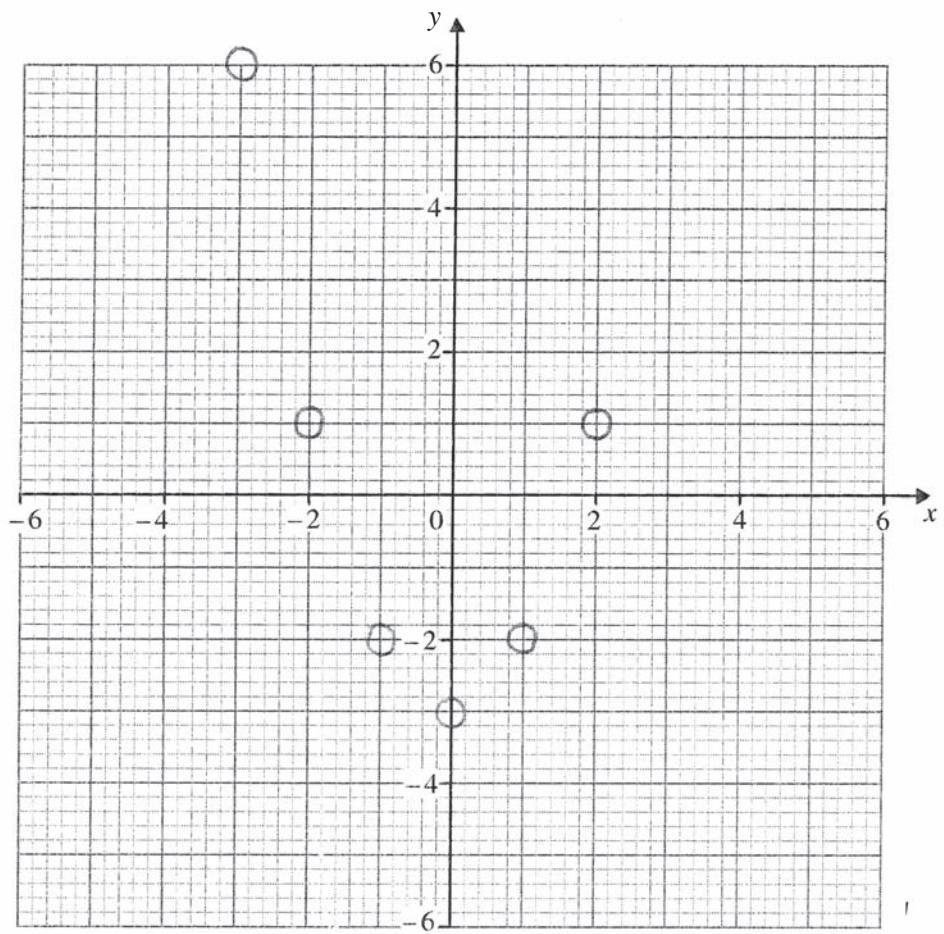
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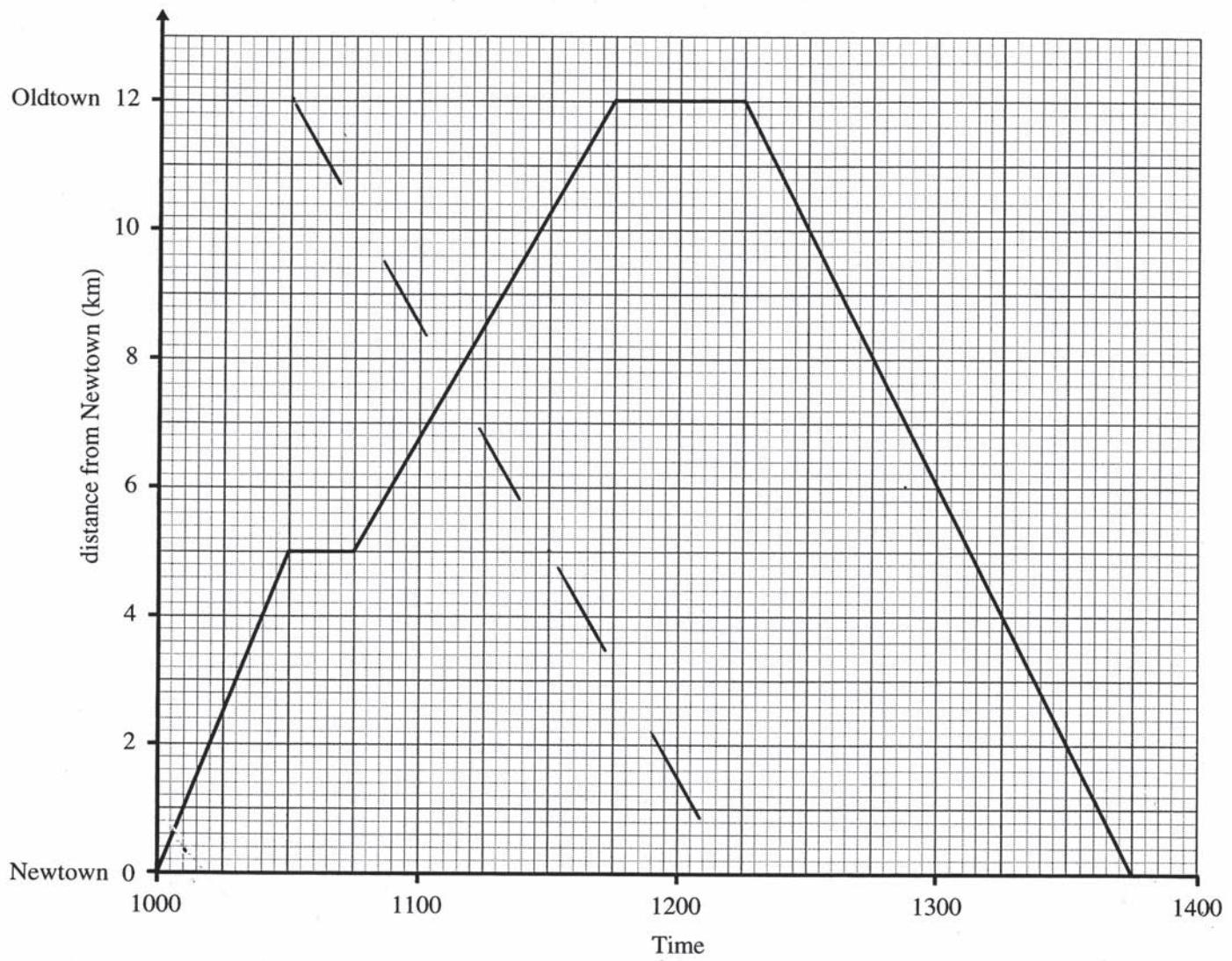
			AVAILABLE MARKS
1	$\left[\frac{4}{25} \right] \times 200$ 32	MA1 A1	2
2	$\frac{1}{2}(8.5 + 12.6) \times 6.1 = 64.355$ Answer 64	M1, A1 A1 (accuracy)	3
3	(a) $1\frac{1}{2} \times 20 = 30$ $1\frac{1}{2} \times 36 = 54$ $1\frac{1}{2} \times 52 = 78$	MA1 MA1 MA1	
	(b) $\frac{\text{€}42}{\text{€}3} = 14$ $14 \times 5 = \$70 = \text{£} \frac{70}{2}$ $\therefore \quad = \text{£}35$ $\therefore \quad \text{€}42 \text{ camera is cheaper}$		5
4	(a) 1 and -2	A1, A1	
	(b) plotting points accuracy of curve	A1 A1	4
5	$\frac{2700}{600} = 4.5$	M1, A1	2
6	(a) $12 \div 1\frac{1}{2}$ $= 8 \text{ km/hr}$	M1 A1	
	(b) (i) starting point (1030, 12) line passing through (1130, 5)	A1 MA2	
	(ii) 1108 or 1107	A1	6
7	$550 \times 0.3 = 165$ $450 \times 0.18 = 81$ $165 + 81 = 246$	M1, A1 MA1 MA1	4

				AVAILABLE MARKS
8	$\text{£}12 \times 8 = \text{£}96$ (Lisa) $\text{£}180 \div 15 = \text{£}12$ (Mikey) $\text{£}12 \times 6 = \text{£}72$ (Richard)	MA1 MA1 MA1		3
9	(a) t^6 (b) r^4 (c) $8xy^4$	A1 A1 A2 for 3 correct terms (A1 for any two)		4
10	$4\pi \times 9^2 = 1017.876$	M1, A1		2
11	(a) Perpendicular bisector of CD (b) Circular arc centre A, radius 6 cm Shaded area between arc and perp. bisector (upper part)	A2 A1 A1		4
12	length none volume area (3 correct A2, 2 correct A1)	A3		3
13	$pr = 50q + 50r$ $pr - 50r = 50q$ $r(p - 50) = 50q$ $r = \frac{50q}{p - 50}$	MA1 MA1 MA1 MA1		4
14	(a) Arc length = $\frac{216}{360} \times 2\pi \times 20 = 24\pi$	MA1, M1, A1		
	(b) $2\pi r = 24\pi$ $r = 12$	M1 A1		5
15	(3, -5)	A1, A1		2
16	(a) correct transformation (reflection in x axis) (b) correct transformation (enlargement scale factor $\frac{1}{3}$ on x axis) (c) correct transformation (3 down)	A1 A1 A1		3
		Total	56	

GCSE MATHEMATICS SUMMER 2009
MODULE N6-2
OVERLAY QUESTION 4



GCSE MATHEMATICS SUMMER 2009
MODULE N6-2
OVERLAY QUESTION 6



GCSE MATHEMATICS SUMMER 2009
MODULE N6-2
OVERLAY QUESTION 11

