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| <i>DO NOT WRITE ON THIS PAPER</i>   | <b>TIME 2 hours</b>   | <i>Paper 2 of 5 from ZigZag Education</i> |
| <b>Sample GCSE Examination Paper<br/>Intermediate Tier Calculator Paper</b> | Standard Equipment: lined or squared paper, pen, pencil, ruler, CALCULATOR.<br>Additional Equipment: pair of compasses, plain paper.<br>Notes: graph paper or squared paper useful for Q2 Q9 & Q16. |   |

1. Solve the equations–
- a)  $6 - 2x = 2x - 6$
- b)  $2(1 + x) = x - 2$

Calculate the value of  $y$  when  $x = 3$  in the equations–

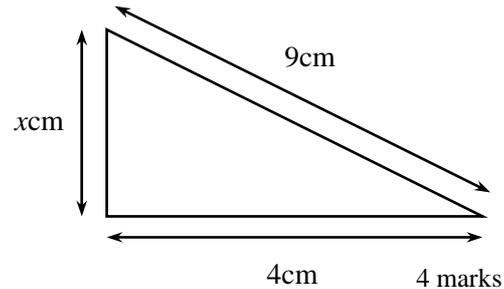
- c)  $y = x(x + 1)$
- d)  $y = 10^x$

8 marks

2. Draw the graph of  $y - x = 7$

5 marks

3. Work out a formula for the perimeter and area of the triangle.



4 marks

4. Work out–

- (a)  $169^2$
- (b)  $2^{24}$

2 marks

5. (a) Estimate the value of  $(39 \times 98) \div 19$  without a calculator, and showing your working.

- (b) Calculate the exact value of  $(39 \times 98) \div 19$  giving your answer as a mixed fraction.

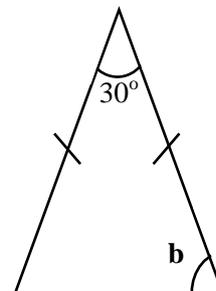
- (c) Work out the difference between your estimate and the exact value of  $(39 \times 98) \div 19$ .

4 marks

6. A phone costs £12 plus vat at 17.5%.  
Calculate the cost of the phone after VAT has been added.

3 marks

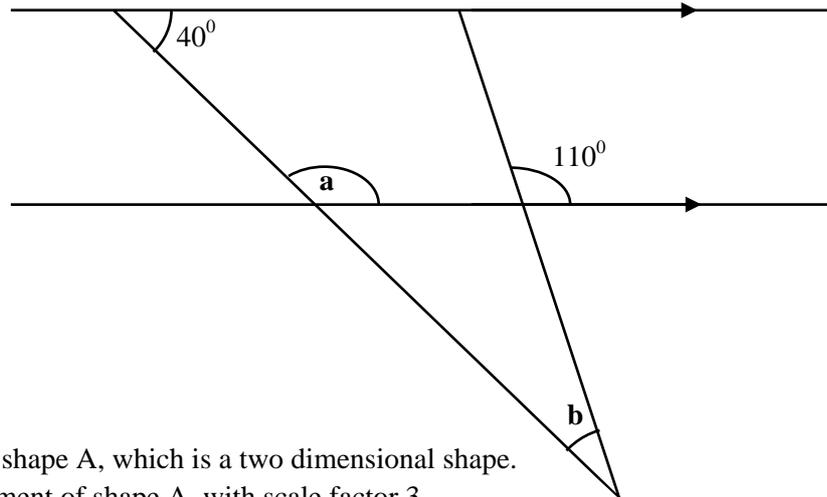
7. Here is an isosceles triangle. Work out angle  $b$ .



2 marks

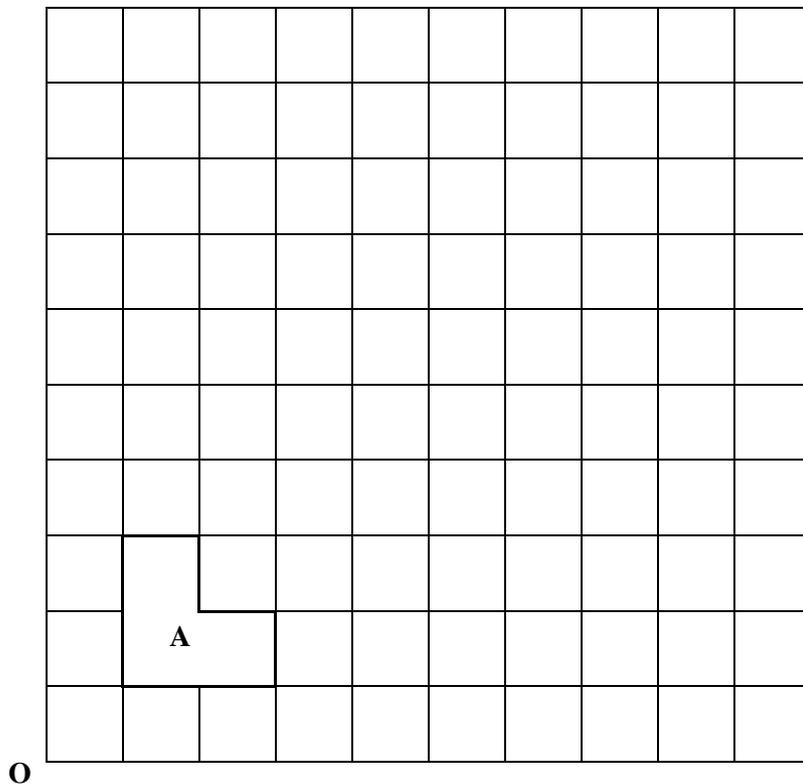
8. Calculate the two missing angles **a** and **b**.

Not drawn accurately



4 marks

9. The diagram contains shape A, which is a two dimensional shape. Shape B is an enlargement of shape A, with scale factor 3. The centre of enlargement is at the bottom left corner of the diagram, marked O.
- (a) Copy the diagram and draw shape B onto the diagram.



- (b) Draw on the diagram a line of symmetry which is common to shapes A and B. 7 marks
- (c) Write down the perimeters of the two shapes A and B. Link these answers to the enlargement.

10. There are four balls on a pool table. Two of these balls have a coloured spot on them, and the other two have a coloured stripe on them. Each ball is also marked with a single number. The spotted balls are marked with the numbers 1 and 2, and the striped balls are marked with the numbers 3 and 4. All the balls are put into a bag, and Jane selects one ball from the bag at random.
- (a) What is the probability that the selected ball is numbered 3?
- (b) What is the probability that the selected ball is spotted, or even numbered, or both?
- (c) What is the probability that the selected ball is odd numbered and striped?

Jane then selects a 2<sup>nd</sup> ball at random, so she now has two pool balls. The possible pattern combinations are represented in the following table. There are 4 possible combinations.

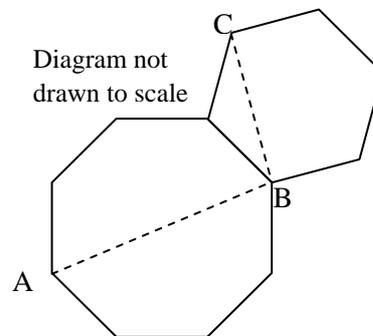
| First Ball Selected | Second Ball Selected |
|---------------------|----------------------|
| stripe              | spot                 |
| stripe              | stripe               |
| spot                | spot                 |
| spot                | stripe               |

Jane begins to similarly list the possible combinations of numbers. She begins:

| First Ball Selected | Second Ball Selected |
|---------------------|----------------------|
| 1                   | 2                    |
| 1                   | 3                    |

- d) Explain why the table does not have the combination 1, 1.  
 e) Copy and complete the table of possible number combinations.  
 f) How many possible combinations of numbers are there? 6 marks

11. a) Multiply out and simplify the expression  $(x - 3)(x + 4)$ .  
 b) Factorise the expressions:  
 i)  $x^2 + 3x$   
 ii)  $x^2 - 10x - 11$

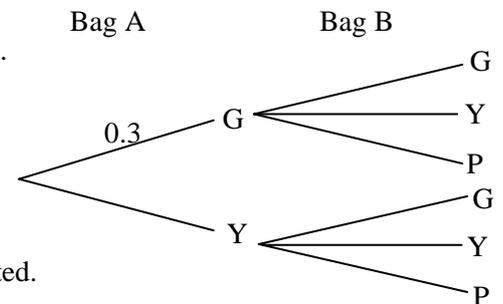


12. The diagram shows two regular polygons of side 3cm. Calculate lengths AB and length BC, giving your answers to 2 decimal places. 10 marks

13. a) Write 48 as the product of primes.  
 b) Write  $48^3$  as the product of primes. 4 marks

14. Bag A contains 3 green balls and 7 yellow balls  
 Bag B contains 7 green balls and 2 yellow balls and a pink ball.

- a) Copy and complete the tree diagram with probabilities



- b) Calculate the probability that no yellow balls are selected. 4 marks

15. The speed of light in vacuum is exactly 299,792,458 m/s.

- a) i) Write 299,792,458 in standard index form to 4 significant figures.  
 ii) Write 299,792,458 in standard index form to 3 significant figures.

The metre is defined as the length of the path travelled by light in vacuum during a time interval of  $\frac{1}{299\,792\,458}$  of a second.

- b) Write  $1 \div 299\,792\,458$  in standard index form to 3 significant figures.

The speed of sound in dry air is given approximately by  $v$ , where

$$v = 331.4 + 0.6T \text{ m/s (where } T \text{ is the Celsius temperature.)}$$

- c) Calculate the speed of sound at 54°C, where C stands for Celsius.

- d) Taking the speed of sound to be 331.4m/s, calculate the ratio of the speed of light to the speed of sound in the form  $n:1$ , with  $n$  given to 2 significant figures. 7 marks

16. The heights of 100 people in an army regiment are summarised in the following table:

| Height in metres   | Frequency |
|--------------------|-----------|
| $1.4 < h \leq 1.5$ | 15        |
| $1.5 < h \leq 1.6$ | 25        |
| $1.6 < h \leq 1.7$ | 34        |
| $1.7 < h \leq 1.8$ | 26        |

The smallest height was 1.44m. The largest height was 1.78m tall. The median height was 1.62m. The first quartile height was 1.53m. The third quartile height was 1.72m.

Using a suitable scale, draw a box and whiskers plot of the heights of the people in the squad. 3 marks

17. The scale used in this diagram is 1cm represents 5km.  
 Reproduce the sketch map showing points A and B roughly 5cm apart, and make sure that the line AB is not horizontal or vertical.  
 Points A and B represent mines in a mine field in the ocean.  
 A boat navigates its way through the middle of the two mines such that it is always equidistant from each mine.

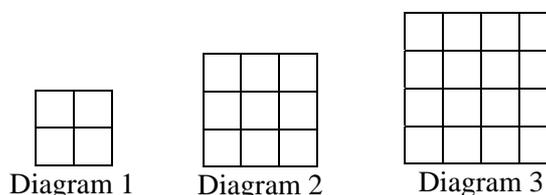
~~B~~

Use a ruler and compasses only to show the path of the boat.  
 Clearly mark on the diagram the path of the boat. 5 marks

~~A~~

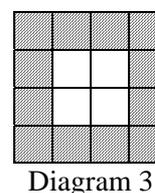
18. The hire charge for a jeep £54 per day plus £2 per mile.  
 Ahmid wishes to hire the jeep for 3 days. He spends £ $x$  with  $x > £162$  and he travels  $y$  miles.
- Write down an expression for the cost of Ahmid's trip in terms of  $y$ .
  - Find an expression for the distance travelled  $y$  in terms of  $x$ . 5 marks

19. In the following, Diagram 1 uses 4 tiles.



- a) Formulate an expression in terms of  $n$ , for the number of tiles in the  $n^{\text{th}}$  diagram.

The outside square of tiles are shaded, as shown for diagram 3:  
 Diagram 3 has 12 shaded tiles and 4 white tiles.



- b) Formulate an expression in terms of  $n$ , for the number of shaded tiles in the  $n^{\text{th}}$  diagram, with  $n > 1$ .
- c) Formulate an expression in terms of  $n$ , for the number of white tiles in the  $n^{\text{th}}$  diagram, with  $n > 1$ . 6 marks

20. The width of a rectangular swimming pool is  $x$  metres.  
 The length of the pool is 5m **less** than its width.  
 The total area of the pool is  $50\text{m}^2$ .

- Show that  $x^2 - 5x - 50 = 0$
- Solve the equation  $x^2 - 5x - 50 = 0$  and interpret your solutions. 5 marks