

Higher Tier Non-Calculator Paper		mark scheme	Paper 1 of 5 from ZigZag Education
1.	a) $x \leq 1$ b) $x = 3$ or -3 c) $\frac{x}{2} + \frac{x}{3} = 2$ $\times 6$	A1 A1A1 M1	
	$3x + 2x = 12$ $5x = 12$ $x = 12/5 = 2.4$	A1	
	d) $\frac{x+1}{2} + \frac{x}{3} = 1$ $\times 6$	M1	
	$3x+3+2x = 6$ $5x = 3$ $x = 3/5 = 0.6$	A1	7 marks
2.	a) i) 1, 5, 9, 13, 17, 21 ii) 2, 5, 10, 17, 26, 37, 50 b) i) $4n - 3$ ii) $n^2 + 1$ c) $100 \times 2 + 2 = 202$ d) $2n + 2$	A1 A1 A1 A1 A1 A1	6 marks
3.	a) J = area (ii) b) K = length (i)	A1 A1	2 marks
4.	a) $120 = 2 \times 2 \times 2 \times 3 \times 5$ b) 0.00001234 c) $\frac{13.8 \times 0.022}{133} \approx \frac{10 \times 0.02}{100}$ numerator/denominator	A1 A1 B1 or appropriate rounding	
	$\approx \frac{0.2}{100} = 0.002$ accept 0.002 – 0.0028	A1	4 marks
5.	a) Construction marks, correct ± 0.5 mm b) Within 3cm AB, Bisector of angle B to give nearer AB than BC	B1A1 B1B1	4 marks
6.	a) $1 + 3 = 4$ $1 + 4 = 5$ L.C.M. of 4 and 5 is 20 Therefore 20 balls b) tree diagram with probs $1/5$ and $4/5$ twice calculating probs at end of tree by multiplication $1/4 \times 1/5 = 1/20$ and $3/4 \times 4/5 = 12/20$ adding probs to give $13/20$	M1 A1 A1 B1 A1 for either A1	6 marks
7.	$^{3/7}x \leq 100$ $x = 233.333^{\text{r}} = 233$ complete panels	M1 A1	2 marks
8.	a) Values– calculating a moving average $\pounds 2.00, \pounds 2.05, \pounds 2.10, \pounds 2.15, \pounds 2.20$ A1 any two correct b) The moving average steadily increases by $\pounds 0.05$ a quarter	M1 A1 all correct A1	4 marks
9.	a) 1.5cm^2 b) $V = 1.5 \times 4 = 6\text{cm}^3$ c) scale factor = $12/4 = 3$ $x = 3 \times 3 = 9\text{cm}$ d) slanted length $\sqrt{10}$ $2 \times 1.5 + 12 + 4 + 4\sqrt{10} = 19 + 4\sqrt{10}$ (a = 19, b = 4, c = 10)	A1 A1 M1 A1 A1 A1A1	7 marks

10. a) bigger square has side $x+1$ B1
change in Area = biggest – smallest M1
 $= (x+1)^2 - x^2$ M1 Allow reverse order
 $= x^2 + 2x + 1 - x^2 = 2x + 1$ A1
- b) Let smaller square have side length = y M1 Allow LHS= $y^2 - x^2$
 $x^2 - y^2 = 6x - 9$
 $\therefore y^2 = x^2 - 6x + 9$ M1
 $\therefore y = \sqrt{x^2 - 6x + 9}$ A1
 $\therefore y = x - 3$ (ignoring $3 - x$) A1
 \therefore perimeter = $4x - 12$ A1 8 marks
11. a) $(1-4)^{-2} = 1/(-3)^2 = 1/9$ M1A1
b) $8^{4/3} = 2^4$ or 16 A1
c) $100^{-1/2} = 1/10$ A1 4 marks
12. Let $x = 0.93939393^{\text{r}}$
 $100x = 93.93939393$ M1
 $99x = 93$ M1
 $x = 93/99 = 31/33$ A1 3 marks
13. a) **c-b** A1
b) $-1/2\mathbf{a} + \mathbf{b} + 1/2(\mathbf{c} - \mathbf{b}) = -1/2\mathbf{a} + 1/2\mathbf{b} + 1/2\mathbf{c}$ M1A1 3 marks
14. a) $2/6 \times 2/6 \times 2/6 = 1/27$ (multiply same fraction) M1A1
b) $4/6 \times 4/6 \times 4/6 = 8/27$ A1 3 marks
15. a) $x^2 + 4x - 5 = (x + 2)^2 - 9$ A1A1
b) $(x + 2)^2 - 9 = 0$ M1
 $(x + 2)^2 = 9$
 $x + 2 = \pm 3$ M1A1
 $x = -2 \pm 3 = 1$ or -5 . (answers MUST be achieved by completing the square, o.w. zero! marks)
A1A1
c) Shift up 5 units. A1
d) **Stretch scale factor 2 in the y direction.** A1A1 10 marks
16. Using mid-points of the second table B1

Increase in Height in cm mid-point	Frequency	mid-point times Frequency
1	10	10
3	20	60
5	10	50
7	10	70
9	50	450
TOTAL	100	640

average estimated increase = $640/100 = 6.4\text{cm}$ A1
estimate of height is **65.1cm** + $6.4\text{cm} = 71.5\text{cm}$ A1 3 marks
using an estimate from the first table when the exact answer is known would be incorrect!

17. a) i) $\angle \text{CAF} = \angle \text{ABC}$ or $\angle \text{ADC}$ A1
ii) Prove the alternate segment theorem.
 $\angle \text{ABC} = \angle \text{ADC}$ (angles in the same segment) B1
 $\angle \text{ACD} = 90^\circ$ (AD diameter) B1
 $\angle \text{CAF} = 90^\circ - \angle \text{DAC}$ B1
 $\angle \text{CAF} = 90^\circ - (180 - 90 - \angle \text{ADC}) = \angle \text{ADC}$
 $\angle \text{CAF} = \angle \text{ADC}$ B1

	b)	i)	$x = 180 - 103 = 77^\circ$	A1	
			$y = 25^\circ$ (alternate segment theorem)	A1	
		ii)	AOC = $2 \times 103 = 206^\circ$ obtuse = $360 - 206 = 154^\circ$	M1A1	
			[or $2 \times x = 154^\circ$ (ft!) M1A1]		9 marks
18.	a)		$f = \frac{k}{d^3}$	M1	
			$4 = k/2^3$	M1	
			$k = 32$	B1	
			$f = 32/4^3$	M1	
			$f = 0.5\text{N}$	A1	
	b)		$16 = 32/d^3$	M1	
			$d^3 = 2 \quad d = \sqrt[3]{2}$	A1	7 marks
19.	a)		$x^2 - 14x + 16 = (x - 7)^2 - 49 + 16 = (x - 7)^2 - 33$	A1A1	
	b)		double translation	A1	
			$f(x)$ translated 7 units LEFT and (translated) <i>33 units up</i> .	A1A1ft	5 marks
20.			$\sqrt{3L} = \frac{V}{2\pi}$	M1	
			$3L = \frac{V^2}{4\pi^2}$	M1	
			$L = \frac{V^2}{12\pi^2}$	A1	3 marks