

Higher Tier Calculator Paper		mark scheme	Paper 1 of 5 from ZigZag Education
1.	19/100	A1	1 mark
2.	(a) x^{10} (b) $2x^4$ (c) x^{15}	A1 A1 A1	3 marks
3.	(a) rotation of 180° (clockwise or anti-clockwise) about $(\frac{1}{2}, 2)$ (b) translation of 4 units in the x direction (c) reflection in the line $x = \frac{1}{2}$	A1 A1 A1 A1	5 marks
4.	(a) right angled triangle angle at circumference from a diameter (b) isosceles triangle tangents from a point are equal in length (c) angle $DAC = x^\circ$ angle $BAC = (90 - x)^\circ$	A1 A1 A1 A1 M1 A1	6 marks
5.	(a) $\frac{2}{2+3} \times \text{£}100$ $\text{£}40$ (b) $\text{£}100 - \text{£}39.75 = \text{£}60.25$ $b = (60.25 \div 39.75) \times 241$ $b = 241$	M1 A1 M1 M1 A1	5 marks
6.	area of triangular face = $\frac{1}{2} \times 8 \times 2 = 8\text{cm}^2$ slant height = $\sqrt{2^2 + 4^2} = \sqrt{20}\text{cm}$ surface area = $2 \times 8 + 2 \times 1.5 \times \sqrt{20} + 1.5 \times 8$ 41.4cm^2	M1 M1 M1 A1	4 marks
7.	(a) $m - 3 = 3j$ $j = \frac{1}{3}(m - 3)$ (b) $\frac{3V}{\pi} = r^3$ $r = \sqrt[3]{\frac{3V}{\pi}}$ (c) $pw - w = 1$ $w(p - 1) = 1$ $w = 1/(p - 1)$	M1 A1 M1 A1 M1 M1 A1	7 marks
8.	(a) all points correctly plotted (b) straight line drawn accurate line drawn in appropriate position (c) positive correlation (moderate) (d) method lines seen on graph $60 - 68$	B1 B1 B1 A1 M1 A1	6 marks
9.	(a) $(x + 2)(x + 3)$ $(x + 2)(x + 3) = 0, x = -2$ or $x = -3$ (b) (i) $2x + 3 = 3x - 3$ $x = 6$ (ii) $x = \frac{12}{14} = \frac{6}{7}$	A1 A1 A1 M1A1 A1	

(c) $2 + 3x < 17x$
 $2 < 14x$
 $x > \frac{1}{7}$

M1
A1

8 marks

10

(a)

x	-2	-1	0	1	2	3
$y = x^2 - 2x - 2$	6	1	-2	-3	-2	1

all values correct

A1

(b) points correctly plotted
smooth curve drawn through points

A1

A1

(c) $x = -0.75 \pm 0.05$, or between 2.75 ± 0.05
(numerical is -0.73, 2.73).

A1A1ft

5 marks

11.

a)

x	-3	-2	-1	0	1	2	3
$y = 2x^2 + 4x - 8$	-2	-8	-10	-8	-2	8	22

A1A1

b) Suitable and correct axis for value
Correct graph plotted
Joined by smooth curve

A1

A1

A1

c) reading off values which intersect with x -axis, $x = 1.2$
by symmetry $x = -3.2$ (or rounding to same)

A1

A1ft

[also accept $x =$ less than 1.3 but rounding to 1.3 or $x =$ more than -3.3 and rounding to -3.3 A1A1]

d) Line $y = -4$ drawn on;
 $x = 0.7$ or $x = -2.7$ (or rounding to same)

M1

A1ft A1ft

10 marks

[also accept $x =$ less than 0.8 and rounding to 0.8 or $x =$ more than -2.8 and rounding to -2.8 A1A1]

12.

Least upper bound $= (200 \div 8.5) \times (50 \div 4.5)$
 $= 23 \times 11$
 $= 253$

A1

M1 consistent rounding down to whole number

The alternative tessellation gives 220 (44×5)
Greatest lower bound $= (200 \div 9.5) \times (50 \div 5.5)$
 $= 21 \times 9$
 $= 189$

A1

The alternative tessellation gives 180 (36×5).

B1 for calculating any correct pair of tessellation answers 253/220, 189/180
4 marks

13.

a) $\frac{120}{x} + \frac{120}{x+10}$ (hours)

B1 for either expression seen +A1

b) $5 = \frac{120}{x} + \frac{120}{x+10}$

A1 ft

c) $5 = \frac{240x + 1200}{(x)(x+10)}$

M1 any correct multiplication

$5x^2 + 50x = 240x + 1200$

M1 2nd correct multiplication

$5x^2 - 190x - 1200 = 0$

M1 simplification

$x^2 - 38x - 240 = 0$ as required

A1

d) $x = \frac{-(-38) \pm \sqrt{(-38)^2 - (4 \times 1 \times -240)}}{2 \times 1}$

M1

$x = \frac{38 \pm \sqrt{2404}}{2}$

$x = 43.515... = 43.5 \text{ km/h}$ (discard negative root)

A1

\therefore return speed $= x + 10 = 53.5 \text{ km/h}$ to 3sf as required

A1 ft

9 marks

14. a) $30 = k \times 60^2$ M1
 $k = 8\frac{1}{3} \times 10^{-3} = 1/120$ M1
 $t = \frac{s^2}{120}$ A1
- b) $t = \frac{45^2}{120}$ M1
 $t = 16.875 = 17$ to the nearest whole number as required A1 5 marks
15. a) $PD^2 = PL^2 + LD^2 - 2 \times PL \times LD \times \cos 127$ M1
 $PD^2 = 6.9^2 + 14^2 - 2 \times 6.9 \times 14 \times \cos 127$
 $PD = 18.9705\dots$ km accept any number rounding to 19.0km A1
- b) $\frac{\sin 127}{18.97\dots} = \frac{\sin LPD}{14}$ M1
 $\sin LPD = 14 \times \frac{\sin 127}{18.97\dots} = 0.5893827\dots$ M1
 $LPD = 36.113216\dots$, Bearing = $180 - LPD = 180 - 36.11\dots = 143.9^\circ$ to 1d.p. as required A1 5 marks
16. a) $DAB = x^\circ$
 $ADC = 180 - x^\circ$ (parallel lines, C-angle) M1 - with explanation
 $DCB = 180 - x^\circ$ (cyclic quadrilateral) M1- with explanation
 $EDC = ECD = x^\circ$ (angles on straight line)
 \therefore triangle EDC isosceles A1 - correct proof.
- b) $PAB = 133 - x$ (angles on a straight line)
 $ACB = (133 - x)^\circ$ (alternate segment) M1A1 5 marks
17. a) $\vec{ST} = \mathbf{c} - \mathbf{a}$ A1
b) $\vec{PU} = \mathbf{a} + \mathbf{c}$ A1
c) $\frac{1}{2}(\mathbf{a} - \mathbf{c} + \mathbf{b})$ A1
d) $\frac{1}{2}(\mathbf{a} + \mathbf{b})$ A1 4 marks
18. a) i) $P = (1/10)^4 = 0.0001$ A1
ii) $P = 10(1/10)^4 = 0.001$ M1A1
b) $P = 10(1/10)^n$ OR $(1/10)^{n-1}$ or equivalent A1 4 marks
19. a) New heights are 12, 4 respectively A1 for either
Plotting correct height polygons with correct widths
(20 \rightarrow 30 = 12 units, 30 \rightarrow 45 4 units) A1A1
- b) missing numbers in table are 48, 56.
 $170 - (16 + 48 + 56 + 24 + 12) = 14$ A1 4 marks