Student Bounty.com Duration: Three Hours

#### Read the following instruction carefully

1. This question paper contains 24 pages including blank pages for rough work. Please check all pa discrepancy, if any.

- 2. Write your registration number, your, name and name of the examination centre at the specified locations on half of the Optical Response Sheet (ORS).
- Using HB pencil, darken the appropriate bubble under each digit of your registration number and the lette 3. corresponding to your paper code.
- 4. All questions in this paper are of objective type.
- 5. Questions must be answered on the ORS by darkening the appropriate bubble marked A, B, C, D) using HB pencil against the question number on the left hand side of the ORS. For each question darken the double of the correct answer. In case you wish to change an answer, erase the old answer completely. More than one answer bubbled against a question will be treated as an incorrect response.
- There are a total of 65 questions carrying 100 marks. 6.
- Questions Q.1 Q.25 will carry 1-mark each, and questions Q.26 Q.55 will carry 2-marks each. 7.
- Questions Q. 48-Q.51 (2 pairs) are common data questions and question pairs (Q. 52, Q.53) and (Q.54, Q.55) are linked 8. answer questions. The answer to the second question of the linked answer questions depends on the answer to the first question of the pair. If the first question in the linked pair is wrongly answered or is un-attempted, then the answer to the second question in the pair will not be evaluated.
- 9. Questions Q.56 - Q.65 belong to General Aptitude (GA), Questions Q.56 - Q.60 will carry 1-mark each, and questions Q.61 – Q.65 will carry 2-marks each. The GA questions will begin on a fresh page starting from page 13.
- 10. Un-attempted questions will carry zero marks.
- Wrong answers will carry NEGATIVE marks. For Q.1 -Q.25 and Q.56 Q.60, 1/3 mark will be deducted for each 11. wrong answer. For Q.26 – Q. 51 and Q.61 - Q.65, 2/3 mark will be deducted for each wrong answer. The question pairs (Q.52, Q.53), and (Q.54, Q.55) are questions with linked answers. There will be negative marks only for wrong answer to the first question of the linked answer question pair i.e., for Q.52 and Q.54, 2/3 mark will be deducted for each wrong answer. There is no negative marking for Q.53 and Q.55.
- 12. Calculator (without data connectivity) is allowed in the examination hall.
- 13. Charts, graph sheets or tables are NOT allowed in the examination hall.
- Rough work can be done on the question paper itself. Additionally, blank pages are provided at the end of the question 14. paper for rough work.

#### Notations and Symbols used

$\Lambda / I$	•	$\{\lambda \in \Lambda : \lambda \not\in I\}$
N	:	The set of all natural numbers
Z	:	The set of all integers
$Z_{n}$	:	The set of all integers modulo <i>n</i>
Q	:	The set of all rational numbers
R	:	The set of all real numbers
$R^n$	:	The set of all <i>n</i> -tuples of real numbers
C	:	The set of all complex numbers
C[0, 1]	:	The set of all complex valued continuous functions on [0, 1]
$P_n[a, b]$	:	The set of all polynomials of degree at most $n$ defined on $[a, b]$
GL(2, R)	:	The group of all $2 \times 2$ real invertible matrices under multiplication

 $\int Y \subset Y \cdot Y \not\subset Y$ 

## Q.1-Q.25 Carry one mark each

- 1. Let E and F be any two events with  $P(E \cup F) = 0.8, P(E) = 0.4$  and P(E|F) = 0.3. Then P(F) is
  - (a.)  $\frac{3}{7}$
  - (b.)  $\frac{4}{7}$
  - (c.)  $\frac{3}{5}$
  - $(d.)\frac{2}{5}$
- 2. Let X have a binomial distribution with parameters n and p, where n is an integer greater than 1 and 0 . If <math>P(X = 0) =P(X=1), then the value of p is
  - (a.)  $\frac{1}{n-1}$
  - $(b.)\frac{n}{n+1}$
  - $(c.)\frac{1}{n+1}$
  - $(d.)\frac{1}{n+1^{\frac{1}{n-1}}}$
- Let u(x, y) = 2x(1-y) for all real x and y. 3. Then a function v(x, y), so f(z) = u(x, y) + iv(x, y) is analytic, is
  - (a.)  $x^2 (y-1^2)$
  - (b.)  $(x-1)^2 y^2$
  - (c.)  $(x-1)^2 + y^2$
  - (d.)  $x^2 + (y-1)^2$
- f(z) be Let analytic on  $D = \{z \in \mathbb{C} : |z-1| < 1\}$  such that f(1) = 1. If  $f(z) = f(z^2)$  for all  $z \in D$ , then which one of the following statements is NOT 00rr00t9

- (d.) f'(1) = 0
- The maximum 5. independent solutions of the a

 $\left(\frac{z}{2}\right) = \frac{1}{2}$   $\left[f(z)\right]$ equation  $\frac{d^4y}{dx^4} = 0$ , with the cond

- y(0) = 1, is
- (a.)4
- (b.)3
- (c.)2
- (d.)1
- 6. Which one of the following sets of functions is NOT orthogonal (with respect to the  $L^2$ -inner product) over the given interval?
  - (a.)  $\{\sin nx : n \in \mathbb{N}\}, -\pi < x < \pi$
  - (b.)  $\{\cos nx : n \in \mathbb{N}\}, -\pi < x < \pi$
  - (c.)  $\left\{ x^{2n+\frac{1}{2}} : n \in \mathbb{N} \right\}, -1 < x < 1$
  - (d.)  $\left\{ x^{2n+\frac{1}{2}} : n \in \mathbb{N} \right\}, -1 < x < 1$
- $f:[1,2]\to \mathbf{R}$ 7. is a non-negative Riemann-integrable function such that  $\int_{-\infty}^{2\pi} \frac{f(x)}{\sqrt{x}} dx = k \int_{-\infty}^{2\pi} f(x) dx \neq 0,$ belongs to the interval
  - (a.)  $0, \frac{1}{2}$
  - $(b.)\left(\frac{1}{3},\frac{2}{3}\right)$
  - $(c.)\left(\frac{2}{3},1\right)$
  - $(d.)\left(1,\frac{4}{3}\right)$
- 8. The set X = R with the metric 1.. ..

(c.) complete but not bounded

(d.) compact but not complete

9.

$$f(x,y) = \begin{cases} \frac{xy}{(x^2 + y^2)^{5/2}} \left[ 1 - \cos(x^2 + y^2) \right], & (x,y) \neq (0,0) \\ k, & (x,y) = (0,0) \end{cases}$$

Then the value of k for which f(x, y) is continuous at (0, 0) is

- (a.)0
- $(b.)\frac{1}{2}$
- (c.) 1
- $(d.)\frac{3}{2}$
- 10. Let A and B be disjoint subsets of R and let m\* denote the Lebesgue outer measure on **R**. Consider the statements:

$$P: m*(A \cup B) = m*(A) + m*(B)$$

- O: Both A and B are Lebesgue measurable R: One of A and B is Lebesgue measurable Which one of the following is correct?
- (a.) If P is true, then Q is true
- (b.) If P is NOT true, then R is true
- (c.) If R is true, then P is NOT true
- (d.) If R is true, then P is true
- $f: \mathbf{R} \to [0, \infty)$  be a Lebesgue 11. measurable function and E be a Lebesgue measurable subset of R such  $\int_{C} f dm = 0$ , where *m* is the Lebesgue

measure on R. Then

- (a.) m(E) = 0
- (b.)  $\{x \in \mathbb{R} : f(x) = 0\} = E$
- (c.)  $m({x \in E : f(x) \neq 0}) = 0$
- (d.)  $m({x \in E : f(x) = 0}) = 0$
- If the nullity of the matrix  $\begin{bmatrix} k & 1 & 2 \\ 1 & -1 & -2 \\ 1 & 1 & 4 \end{bmatrix}$  is 12.
  - 1, then the value of k is (a) 1

- Student Bounty Com 13. an eigenva remaining eiger
  - (a.)  $\frac{1}{2i}$
  - (b.)  $-\frac{1}{2i}$
  - (c.)0
  - (d.)1
- 14. For the linear programming problem

Minimize 
$$z = x - y$$
,

subject to 
$$2x + 3y \le 6$$
,

$$0 \le x \le 3$$
,

$$0 \le y \le 3$$
,

the number of extreme points of its feasible region and the number of basic feasible solutions respectively, are

- (a.) 3 and 3
- (b.)4 and 4
- (c.) 3 and 5
- (d.)4 and 5
- 15. Which one of the following statements is correct?
  - (a.) If a Linear Programming Problem (LPP) is infeasible, then its dual is also infeasible
  - (b.) If an LPP is infeasible, then its dual always has unbounded solution
  - (c.) If an LPP has unbounded solution, then its dual also has unbounded solution
  - (d.) If an LPP has unbounded solution, then its dual is infeasible
- Which one of the following groups is 16. simple?
  - (a.)  $S_3$
  - (b.) GL(2, R)
  - (c.)  $Z_2 \times Z_2$
  - $(d.) A_5$
- Consider 17. extension the algebraic  $E = Q(\sqrt{2}, \sqrt{3}, \sqrt{5})$  of the field **Q** of rational numbers. Then [E: O] the degree of E over Q, is

18. The general solution of the partial differential equation  $\frac{\partial^2 z}{\partial x \partial y} = x + y$  is of the

(a.) 
$$\frac{1}{2}xy(x+y)+F(x)+G(y)$$

(b.) 
$$\frac{1}{2}xy(x-y)+F(x)+G(y)$$

(c.) 
$$\frac{1}{2}xy(x-y)+F(x)G(y)$$

$$(d.)\frac{1}{2}xy(x+y)+F(x)G(y)$$

- 19. The numerical value obtained by applying the two-point trapezoidal rule to the integral  $\int_{r}^{1} \frac{\ln(1+x)}{x} dx$  is
  - (a.)  $\frac{1}{2} (\ln 2 + 1)$
  - $(b.)\frac{1}{2}$
  - (c.)  $\frac{1}{2} (\ln 2 1)$
  - $(d.)\frac{1}{2}\ln 2$
- $l_{\nu}(x), k = 0, 1, ...., n$ 20. denote Lagrange's fundamental polynomials of degree n for the nodes  $x_0, x_1, \dots, x_n$ . Then
  - the value of  $\sum_{k=0}^{n} l_k(x)$  is
  - (a.)0
  - (b.)1
  - (c.)  $x^n + 1$
  - $(d.) x^n 1$
- 21. Let X and Y be normed linear spaces and  $\{T_n\}$  be a sequence of bounded linear operators from X to Y. Consider the statements:
  - $P:\{||T_nx||:n\in\mathbf{N}\}$  is bounded for each
  - $Q:\{||T_n||:n\in\mathbb{N}\}$  is bounded

- Student Bounty.com Y is a Ba
- (c.) If X is a Ba
- (d.) If Y is a Banach
- X = G[0, 1]22.

$$||x||_1 = \int_0^1 |x(t)| dx, x \in C[0,1]|$$

$$\Omega = \{f \in X' : ||f|| = 1\}$$
, where  $X'$  denote the dual space of  $X$ . Let  $C(\Omega)$  be the linear space of continuous function on  $\Omega$  with the norm  $\|u\| = \sup_{s \in \Omega} |u(s)|, u \in C(\Omega)$ .

Then

- (a.) X is linearly isometric with  $C(\Omega)$
- (b.) X is linearly isometric with a proper subspace of  $C(\Omega)$
- (c.) there does not exists a linear isometry form X into  $C(\Omega)$
- (d.) every linear isometry from X to  $C(\Omega)$  is onto.
- 23. Let X = R equipped with the topology generated by open intervals of the form (a,b) and sets of the form  $(a,b) \cap \mathbf{Q}$ . Then which one of the following statements is correct?
  - (a.) X is regular
  - (b.)X is normal
  - (c.)  $X \setminus Q$  is dense in X
  - (d.) O is dense in X
- 24. Let H, T and V denote the Hamiltonian, the kinetic energy and the potential energy respectively of a mechanical system at time t. If H contains t' explicitly, then  $\frac{\partial H}{\partial t}$

is equal to

(a.) 
$$\frac{\partial T}{\partial t} + \frac{\partial V}{\partial t}$$

(b.) 
$$\frac{\partial T}{\partial t} - \frac{\partial V}{\partial t}$$
  
 $\frac{\partial V}{\partial t} = \frac{\partial T}{\partial t}$ 

$$I\left[y(x)\right] = \int_{0}^{1} (2x - xy - y') y' dx, \text{ is}$$

(a.) 
$$2y''-y=2$$

(b.) 
$$2y'' + y = 2$$

(c.) 
$$y'' + 2y = 0$$

(d.) 
$$2y'' - y = 0$$

# Q.26-Q.55 Carry two marks each

26. Let X have a binomial distribution with parameters n and p, n=3. For testing the hypothesis  $H_0: p=\frac{2}{3}$  against  $H_1: p=\frac{1}{3}$ , let a test be: "Reject  $H_0$  if  $X \ge 2$  and accept  $H_0$  if  $X \le 1$ ". Then the probabilities of Type I and Type II errors respectively are

(a.) 
$$\frac{20}{27}$$
 and  $\frac{20}{27}$ 

(b.) 
$$\frac{7}{27}$$
 and  $\frac{20}{27}$ 

(c.) 
$$\frac{20}{27}$$
 and  $\frac{7}{27}$ 

(d.) 
$$\frac{7}{27}$$
 and  $\frac{7}{27}$ 

27. Let 
$$I = \int_C \frac{f(z)}{(Z-1)(Z-2)} dz$$
, where

$$f(z) = \sin \frac{\pi z}{2} + \cos \frac{\pi z}{2}$$
 and C is the curve

|z|=3 oriented anti-clockwise. Then the value of *I* is

- (a.)  $4\pi i$
- (b.)0
- (c.)  $-2\pi i$
- (d.)  $-4\pi i$

28. Let 
$$\sum_{n=\infty}^{\infty} b_n z^n$$
 be the Laurent series expansion of the function

(b.) 
$$b_{-3} = 1$$
,

(c.) 
$$b_{-2} = 0, b_0 = -$$

(d.) 
$$b_0 = 1, b_2 = -\frac{1}{6}, b_4 = 36$$

29. Under the transformation  $w = \sqrt{z}$  region  $D = \{z \in \mathbb{C} : |z| < 1\}$  is transformation

(a.) 
$$\{z \in \mathbb{C} : 0 < \arg z < \pi \}$$

$$(b.) \{ z \in \mathbf{C} : -\pi < \arg z < 0 \}$$

(c.) 
$$\left\{ z \in \mathbf{C} : 0 < \arg z \frac{\pi}{2} \text{ or } \pi < \arg z \frac{3\pi}{2} \right\}$$

(d.) 
$$\left\{ z \in \mathbb{C} : \frac{\pi}{2} < \arg z < \pi \text{ or } \frac{3\pi}{2} < \arg z < 2\pi \right\}$$

30. Let y(x) be the solution of the initial value problem

$$y''' - y'' + 4y' - 4y = 0,$$

$$y(0) = y'(0) = 2, y''(0) = 0$$

Then the value of  $y\left(\frac{\pi}{2}\right)$  is

(a.) 
$$\frac{1}{5} \left( 4e^{\frac{\pi}{2}} - 6 \right)$$

(b.) 
$$\frac{1}{5} \left( 6e^{\frac{\pi}{2}} - 4 \right)$$

(c.) 
$$\frac{1}{5} \left( 8e^{\frac{\pi}{2}} - 2 \right)$$

(d.) 
$$\frac{1}{5} \left( 8e^{\frac{\pi}{2}} + 2 \right)$$

31. Let y(x) be the solution of the initial value problem

$$x^2y'' + xy' + y = x,$$

$$y(1) = y'(1) = 1$$

Then the value of  $y\left(e^{\frac{\pi}{2}}\right)$  is

$$(b.)\frac{1}{2}\left(1+e^{\frac{\pi}{2}}\right)$$

(c.) 
$$\frac{1}{2} + \frac{\pi}{4}$$

$$(d.)\frac{1}{2} - \frac{\pi}{4}$$

32. Let  $T: \mathbb{R}^3 \to \mathbb{R}^3$  be a linear transformation defined by T(x, y, z) = (x+y, y+z, z-x). Then, an orthonormal basis for the range of T is

(a.) 
$$\left\{ \left( \frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}, 0 \right), \left( \frac{1}{\sqrt{3}}, -\frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}} \right) \right\}$$

(b.) 
$$\left\{ \left( \frac{1}{\sqrt{2}}, -\frac{1}{\sqrt{2}}, 0 \right), \left( \frac{1}{\sqrt{6}}, \frac{1}{\sqrt{6}}, \frac{2}{\sqrt{6}} \right) \right\}$$

(c.) 
$$\left\{ \left( \frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}, 0 \right), \left( \frac{1}{\sqrt{6}}, \frac{1}{\sqrt{6}}, -\frac{2}{\sqrt{6}} \right) \right\}$$

(d.) 
$$\left\{ \left( \frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}, 0 \right), \left( \frac{1}{\sqrt{3}}, -\frac{1}{\sqrt{3}}, -\frac{1}{\sqrt{3}} \right) \right\}$$

33. Let  $T: P_3[0,1] \rightarrow P_2[0,1]$  be defined by (Tp)(x) = p''(x) + p'(x). Then the matrix representation of T with respect to the bases  $\{1, x, x^2, x^3\}$  and  $\{1, x, x^2\}$  of  $P_3[0,1]$  and  $P_2[0,1]$  respectively is

(a.) 
$$\begin{bmatrix} 0 & 0 & 0 \\ 1 & 0 & 0 \\ 2 & 2 & 0 \\ 0 & 6 & 3 \end{bmatrix}$$

(b.) 
$$\begin{bmatrix} 0 & 1 & 2 & 0 \\ 0 & 0 & 2 & 6 \\ 0 & 0 & 0 & 3 \end{bmatrix}$$

$$(d.) \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 2 & 2 \end{bmatrix}$$

- Consider  $\{u_1, u_2, u_3\}$  of  $\mathbb{R}^3$ ; where  $u_1$   $u_2 = (1, 1, 0)$ ,  $u_3 = (1, 1, 1)$ . Let be the dual basis of  $\{u_1, u_2, u_3\}$  a linear functional defin by f(a, b, c) = a + b + c, (a, b), If  $f = \alpha_1 f_1 + \alpha_2 f_2 + \alpha_3 f_3$ , then  $(\alpha_1, a)$
- (a.)(1,2,3)

34.

- (b.)(1,3,2)
- (c.)(2,3,1)
- (d.)(3,2,1)
- 35. The following table gives the cost matrix of a transportation problem

The basic feasible solution given by  $x_{11} = 3$ ,  $x_{13} = 1$ ,  $x_{23} = 6$ ,  $x_{31} = 2$ ,  $x_{32} = 5$  is

- (a.) degenerate and optimal
- (b.) optimal but not degenerate
- (c.) degenerate but not optimal
- (d.) neither degenerate nor optimal
- 36. If  $z^*$  is the optimal value of the linear programming problem

Maximize  $z = 5x_1 + 9x_2 + 4x_3$ 

subject to 
$$x_1 + x_2 + x_3 = 5$$
  
 $4x_1 + 3x_2 + 2x_3 = 12$ 

$$x_1, x_2, x_3 \ge 0$$

then

(a.) 
$$0 \le z^* < 10$$

(b.) 
$$10 \le z^* < 20$$

(c.) 
$$20 \le z^* < 30$$

(d.) 
$$30 \le z^* < 40$$

37. Let  $G_1$  be an abelian group of order 6 and  $G_2 = S_3$ . For j = 1, 2, let  $P_j$  be the statement:

" $G_j$  has a unique subgroup of order 2".

- (c.)  $P_1$  holds but not  $P_2$
- (d.)  $P_2$  holds but not  $P_1$
- 38. Let G be the group of all symmetries of the square. Then the number of conjugate classes in G is
  - (a.) 4
  - (b.)5
  - (c.)6
  - (d.)7
- 39. Consider the polynomial ring  $\mathbf{Q}[x]$ . The ideal of  $\mathbf{Q}[x]$  generated by  $x^2 3$  is
  - (a.) maximal but not prime
  - (b.) prime but not maximal
  - (c.) both maximal and prime
  - (d.) neither maximal nor prime
- 40. Consider the wave equation  $\frac{\partial^2 u}{\partial t^2} = 4 \frac{\partial^2 u}{\partial x^2}, \quad 0 < x < \pi, t > 0, \quad \text{with}$   $u(0, t) = u(\pi, t) = 0, \quad u(x, 0) = \sin x \quad \text{and}$   $\frac{\partial u}{\partial t} = 0 \quad \text{at} \quad t = 0. \text{ Then } u\left(\frac{\pi}{2}, \frac{\pi}{2}\right) \text{ is}$ 
  - (a.) 2
  - (b.)1
  - (c.)0
  - (d.)-1
- 41. Let  $I = \int_C \frac{e^y}{x} dx + \left(e^y \ln x + x\right) dy$ , where C

is the positively oriented boundary of the region enclosed by

- $y = 1 + x^2$ , y = 2,  $x = \frac{1}{2}$ . Then the value of *I*
- $(a.)^{\frac{1}{8}}$
- (b.)  $\frac{5}{24}$
- (c.)  $\frac{7}{24}$
- $(d.)\frac{3}{8}$
- 42. Let  $\{f_n\}$  be a sequence of real valued

integrable

Consider the

 $P_1:\{f_n\}$  converg

 $P_2: \{f'_n\}$  converges un

$$P_3: \int_a^b f_n(x) dx \to \int_a^b f(x) dx$$

 $P_A$ : f is differentiable

Then which one of the following NOT be true

- (a.)  $P_1$  implies  $P_3$
- (b.)  $P_2$  implies  $P_1$
- (c.)  $P_2$  implies  $P_4$
- (d.)  $P_3$  implies  $P_1$
- 43. Let  $f_n(x) = \frac{x^n}{1+x}$  and  $g_n(x) = \frac{x^n}{1+nx}$  for  $x \in \mathbb{N}$ . Then on the interval [0,1],
  - (a.) both  $\{f_n\}$  and  $\{g_n\}$  converges uniformly
  - (b.) neither  $\{f_n\}$  nor  $\{g_n\}$  converges uniformly
  - (c.)  $\{f_n\}$  converges uniformly but  $\{g_n\}$  does not converge uniformly
  - (d.)  $\{g_n\}$  converges uniformly but  $\{f_n\}$  does not converges uniformly
- 44. Consider the power series  $\sum_{n=1}^{\infty} \frac{x^n}{\sqrt{n}}$  and

$$\sum_{n=1}^{\infty} \frac{x^n}{n}$$
. Then

- (a.) both converge on (-1, 1]
- (b.) both converge on [-1, 1)
- (c.) exactly one of them converges on (-1, 1]
- (d.) none of them converges on [-1, 1]
- 45. Let  $X = \mathbf{N}$  be equipped with the topology generated by the basis consisting of sets  $A_n = \{n, n+1, n+2, ....\}, n \in \mathbf{N}$ . Then X is

- (d.) Neither compact nor connected
- 46. Four weightless rods form a rhombus PORS with smooth at the joints. Another weightless rod joins the midpoints E and Fof PO and PS respectively. The system is suspended from P and a weight 2W is attached to R. If the angle between the rods PO and PS is 20, then the thrust in the rod EF is
  - (a.)  $W \tan \theta$
  - (b.)  $2W \tan \theta$
  - (c.)  $2W \cot \theta$
  - (d.)  $4W \tan \theta$
- For a continuous function f(t),  $0 \le t \le 1$ , 47. integral equation  $y(t) = f(t) + 3\int_{0}^{1} tsy(s) ds$  has
  - (a.) a unique solution if  $\int_{0}^{1} sf(s) ds \neq 0$
  - (b.) no solution if  $\int_{0}^{1} sf(s) ds = 0$
  - (c.) infinitely solution many  $\int sf(s)ds = 0$
  - (d.)infinitely many solutions  $\int sf(s)ds \neq 0$

## **Common Data Questions** Common Data for Questions 48 and 49:

Let X and Y be continuous random variables with the joint probability density function

$$f(x, y) = \begin{cases} ae^{-2y}, & 0 < x < y < \infty \\ 0, & otherwise \end{cases}$$

- 48. The value of a is
  - (a.)4
  - (b.)2
  - (c.)1

- (b.) 3
- (c.)2
- (d.)1

### **Common Data for Question**

Student Bounty.com Let  $X = \mathbf{N} \times \mathbf{O}$  with the subspace topolo

on 
$$\mathbb{R}^2$$
 and  $P = \left\{ \left( n, \frac{1}{n} \right) : n \in \mathbb{N} \right\}$ 

- 50. In the space X,
  - (a.) P is closed but not open
    - (b.) P is open but not closed
    - (c.) P is both open and closed
    - (d.) P is neither open nor closed
- The boundary of P in X is 51.
  - (a.) an empty set
  - (b.) a singleton set
  - (c.) P'
  - (d.) X

### **Linked Answer Questions** Statement for Linked Answer Questions 52 and 53:

For a differentiable function f(x), the integral  $\int_{0}^{\pi} f(x)dx$  is approximated by the formulas  $h[a_0 f(0) + a_1 f(h)] + h^2[b_0 f'(0) + b_1 f'(h)]$ which is exact for all polynomials of degree at most 3.

- 52. The value of  $a_1$  and  $b_1$  respectively are
  - (a.)  $\frac{1}{2}$  and  $-\frac{1}{12}$
  - (b.)  $-\frac{1}{12}$  and  $\frac{1}{2}$
  - (c.)  $\frac{1}{2}$  and  $\frac{1}{12}$

(a.) 
$$\frac{1}{2}$$
 and  $\frac{1}{2}$ 

(b.) 
$$\frac{1}{12}$$
 and  $-\frac{1}{12}$ 

(c.) 
$$\frac{1}{2}$$
 and  $\frac{1}{12}$ 

(d.) 
$$\frac{1}{2}$$
 and  $-\frac{1}{12}$ 

### Statement for Linked Answer Questions 54 and 55:

X = C[0, 1] with Let the inner product  $\langle x, y \rangle = \int_{0}^{1} x(t) \overline{y(t)} dt, x, y \in C[0, 1],$ 

$$X_0 = \left\{ x \in X : \int_0^1 t^2 x(t) dt = 0 \right\}, \text{ and } X_0^{\perp} \text{ be the orthogonal complement of } X_0.$$

- 54. Which one of the following statements is correct?
  - (a.) Both  $X_0$  and  $X_0^{\perp}$  are complete
  - (b.) Neither  $X_0$  nor  $X_0^{\perp}$  is complete
  - (c.)  $X_0$  is complete but  $X_0^{\perp}$  is not complete
  - (d.)  $X_0^{\perp}$  is complete but  $X_0$  is not complete
- Let  $y(t) = t^3, t \in [0, 1]$  and  $x_0 \in X_0^{\perp}$  be the 55. approximation of Then  $x_0(t), t \in [0,1]$  is

56. Whien of closest in me

### Circuitous

- (a.) cyclic
- (b.) indirect
- (c.) confusing
- (d.) crooked
- Student Bounty.com 57. The question below consists of related words followed by four words. Select the pair that best expl the relation in the original pair.

### Unemployed: Worker

- (a.) fallow: land
- (b.) unaware : sleeper
- (c.) wit: jester
- (d.) renovated: house
- 58. Choose the most appropriate word from the options given below to complete the following sentence:

If we manage to \_\_\_\_\_ our natural resources, we would leave a better planet for our children.

- (a.) uphold
- (b.) restrain
- (c.) cherish
- (d.) conserve
- 59. Choose the most appropriate word from the options given below to complete the following sentence:

His rather causal remarks on politics his lack of seriousness about the subject.

- (a.) masked
- (b.) belied
- (c.) betrayed
- (d.) suppressed
- 60. 25 persons are in a room. 15 of them play hockey, 17 of them play football and 10 of them play both hockey and football. Then the number of persons playing either hockey nor football is:
  - (a.)2
  - (b.)17
  - (c.)13
  - (d.)3

61. Modern warfare has changed from large scale clashes of armies suppression of civilian populations. Chemical agents that do their work silently appear to be suited to such warfare; and regretfully, there exist people in military establishments who think that chemical agents are useful tools for their cause.

> Which of the following statements best sums up the meaning of the above passage:

- (a.) Modern warfare has resulted in civil strife
- (b.) Chemical agents are useful in modern warfare
- (c.) Use of chemical agents in warfare would be undesirable
- (d.) People in military establishments like to use chemical agents in war.
- 62. If 137 + 276 = 435 how much is 731 +672?
  - (a.) 534
  - (b.) 1403
  - (c.) 1623
  - (d.) 1513
- 63. 5 skilled workers can build a wall in 20 days: 8 semi-skilled workers can build a wall in 25 days; 10 unskilled workers can build a wall in 30 days. If a team has 2 skilled, 6 semi-skilled and 5 unskilled workers, how long will it take to build the wall?
  - (a.) 20 days
  - (b.) 18 days
  - (c.) 16 days
  - (d.) 15 days
- Given digits 2, 2, 3, 3, 3, 4, 4, 4, 4 how 64. many distinct 4 digit numbers greater than 3000 can be formed?
  - (a.) 50
  - (b.)51
  - (c.) 52
  - (d.)54
- 65. Hari (H), Gita (G), Irfan (I) and Saira (S) are siblings (i.e. brothers and sisters). All were born on 1st January. The age

- s age > Irfan's age + i. пап Saira's a.
- Student Bounty.com ii. The age di Saira is 1 year the oldest and San
- iii. There are no twins.

In what order were they born

- (a.) HSIG
- (b.) SGHI
- (c.) IGSH
- (d.) IHSG