

1	C	2	A	3	D	4	B	5	D	6	C	7	A
8		9	A	10	D	11	C	12	A	13	D	14	B
15	A	16	B	17	D	18	D	19	B	20	A	21	C
22	A	23	A	24	C	25	D	26	C	27	B	28	A
29	B	30		31	C	32	A	33	A	34	C	35	D
36	A	37	C	38	D	39	B	40	C	41	D	42	B
43	C	44	A	45	C	46	B	47	A	48	D	49	B
50	A	51	B	52	D	53	C	54	D	55	B	56	B
57	A	58	D	59	C	60	D	61	C	62	B	63	D
64	B	65	C	66		67	C	68	A	69	D	70	B
71	C	72	B	73	D	74		75	D	76	D	77	A
78	C	79	C	80	C	81	C,B	82	A,B	83	B,C	84	D,B
85	B,D												



Explanations:

1. () $8 = \frac{100}{R+5} \Rightarrow R = 7.5$

2. ()

$$\text{RMS value} = \sqrt{3^2 + \left(\frac{4}{\sqrt{2}}\right)^2} = \sqrt{3^2 + \frac{16}{2}} = \sqrt{17}$$

$$\text{RMS value} = \sqrt{17}$$

3. ()

4. () In the steady state C is open

$$\therefore V_C = 10V$$

$$V_1 = Z_1 I_1 + Z_1 I_2$$

$$V_2 = Z_2 I_2 + Z_1 I_2 + Z_1 I_1 = (Z_1 + Z_2) I_2 + I_1 Z_1$$

$$\begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = \begin{bmatrix} Z_1 & Z_2 \\ Z_1 + Z_2 & Z_1 \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix}$$

5. ()

6. ()

$$T(s) = \frac{s^2 + 4}{(s+1)(s+4)} = 0 \Rightarrow s = \pm j_2 = \pm j\omega$$

$$\omega = 2$$

7. () All the root locus branches starts at $S = 0$

$$\varepsilon^1 \text{ also going to } \infty \text{ with an angle } \frac{180}{3} = 60$$

So, answer is (A).

8. () Phase = $-180 + \tan^{-1}(\omega)$

$$\text{Phase} = -180, \omega = 0$$

$$\text{Phase crossover frequency} = 0;$$

$$\text{gain} = \frac{\sqrt{H\omega^2}}{\omega^2} = \infty$$

$$\text{gain margin} = \infty$$

9. ()

10. ()

11. ()

$$S = \int_1^{\infty} x^{-3} dx = \frac{x^{-4}}{-4} \Big|_1^{\infty} = \frac{0+1}{4} = \frac{1}{4}$$

$$S = \frac{1}{4}$$

12. ()

$$\frac{dx}{dt} = -3x(t), sx(s) = -3x(s)$$

$$x(s) = \frac{x_0}{s+3}$$

$$x(t) = x_0 e^{-3t}$$

13. ()

14. ()

15. ()

16. ()

17. ()

18. ()

$$P = \frac{V^2}{X_{series}}; \frac{P_1}{P_2} = \left(\frac{800}{400}\right)^2 = 4; P_2 = \frac{P_1}{4}$$

19. ()

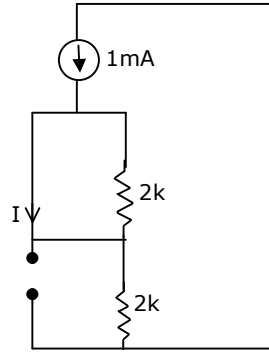
20. ()

21. ()

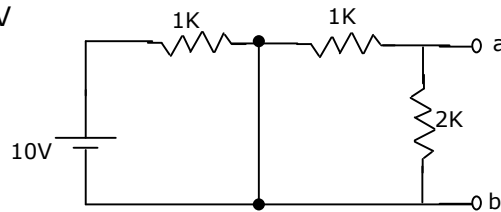
22. () PMMC voltmeter reads only DC

$$\therefore V = 2V$$

23. () $D_1 \rightarrow \text{short}$
 $D_2 \rightarrow \text{open}$
 $I = 0 \text{ mA}$



24. ()
 25. () For MOSFET, $V_{GS} = 2\text{V}$, $V_t = 1\text{V}$
 $V_{GS} > V_t$, so MOSFET is turn-on
 $V_{ab} = 0\text{V}$



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26. ()
 27. ()
 28. ()
 29. ()
 30. ()
 31. ()
 32. ()

$$V_{RY} = V \angle 0$$

$$V_{YB} = V \angle -120$$

$$V_{BR} = V \angle 120$$

$$I_R = \frac{V_{RB}}{R} = \frac{-V \angle 120}{R} = \frac{V}{R} \angle -60$$

$$I_Y = \frac{V_{YB}}{R} = \frac{V}{R} \angle -120$$

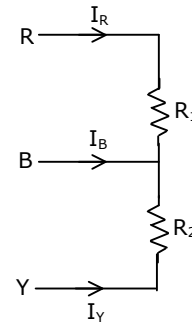
$$I_R + I_Y + I_B = 0$$

$$I_B = -(I_Y + I_R) = \frac{-V}{R} (\angle -60 + \angle -120)$$

$$= \frac{-V}{R} (-0.5 - j0.866 - 0.5 - j0.866)$$

$$= \frac{-\sqrt{3}V}{R} \angle -90 = \sqrt{3} \left(\frac{V}{R} \right) \angle 90$$

$$I_R : I_Y : I_B = 1 : 1 : \sqrt{3}$$



33. ()

$$V_{\text{rms}} = \sqrt{\frac{\frac{1}{3} \times 1^2 \times \frac{T}{2}}{T}} = \sqrt{\frac{1}{6}}$$

$$V_{\text{rms}} = \frac{1}{\sqrt{6}}$$

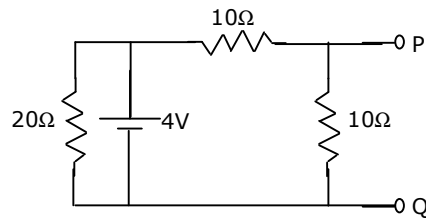
34. () In the steady state, inductor is drawing 1A, ε^1 acts as a short.
When $t = 0^+$, inductor acts as a open circuit.
 $i_L = 1\text{A}$

35. ()

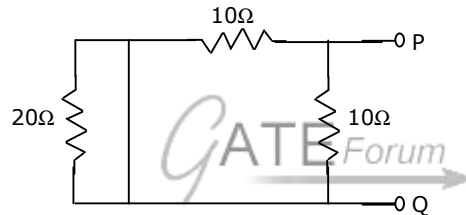
36. ()

$$V_{PQ} = 2\text{V}$$

$$V_{Th} = 2\text{V}$$



For R_{Th} ,



$$R_{Th} = 5\Omega$$

37. ()

Characteristic equation is $1 + G(s)H(s) = 0$;

$$\frac{K(1-s)}{(1+s)} + 1 = 0$$

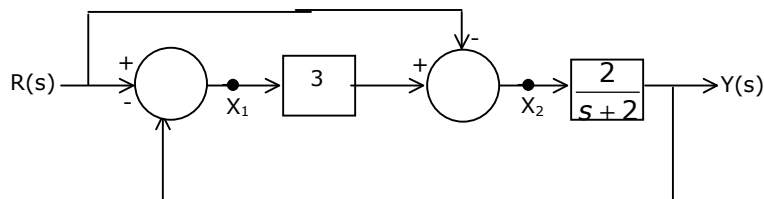
$$K - Ks + S + 1 = 0; \quad S(1-K) + (K+1) = 0$$

$$\text{For stable system,} \quad 1-K > 0 \quad K+1 > 0$$

$$1 > K; \quad K < +1 \quad K > -1$$

$$|K| < 1$$

38. ()



$$X_1 = R(s) - y(s)$$

$$X_2 = 3[R(s) - y(s)] - R(s) = 2R(s) - 3y(s)$$

$$y(s) = [2R(s) - 3y(s)] \frac{2}{s+2}$$

$$\frac{Y(s)}{R(s)} = \frac{4}{s+8}$$

$$R(s) = \frac{1}{s} \text{ given}$$

$$Y(s) = \frac{4}{s(s+8)}$$

$$\text{steady state error} = \lim_{s \rightarrow 0} sY(s) = \lim_{s \rightarrow 0} \frac{4s}{s+8}$$

$$\text{steady state error} = 0.5$$

39. ()

$$\text{Phase of } G(s)H(s) \text{ is } -90 - \left(\frac{180}{\pi}\right)(0.25\omega)$$

$$-90 - \left(\frac{180}{\pi}\right)0.25\omega = -90 - \left(\frac{180}{\pi}\right)\left(\frac{\omega}{4}\right)$$

when it passes through negative real axis phase = -180

$$-90 - \left(\frac{180}{\pi}\right)\left(\frac{\omega}{4}\right) = -180$$

$$\omega = 2\pi$$

$$\text{gain at this point is } \left| \frac{\pi e^{\frac{s}{4}}}{s} \right| = \frac{\pi}{\omega}$$

$$= \frac{\pi}{2\pi} = 0.5$$

it cross - vertical axis at $-0.5+j0$

40. ()

$$G(s)H(s) = \frac{K + 0.366s}{s(s+1)}$$

$$\text{phase margin (PM)} = 180 + \left[-90 - \tan^{-1} \omega - \tan^{-1} \left(\frac{0.366\omega}{K} \right) \right]$$

$$\text{PM} = 60, \omega = 1 \text{ rad/sec.}$$

$$\text{Substitutions, } K = 1.366$$

41. ()

42. ()

43. ()

44. ()

$$f(x) = x^2 e^{-x}, \frac{df(x)}{dx} = 2x e^{-x} + x^2 e^{-x} (-1) = 0$$

$$(2x - x^2) e^{-x} = 0$$

$$x = 2$$

45. ()

$$\text{gradient} = \frac{\partial u}{\partial x} i + \frac{\partial u}{\partial y} j$$

$$= xi + \frac{2}{3} yj$$

@ (1,3) point, $i+2j$ magnitude is $\sqrt{5}$

46. ()

$$\frac{d^2 x}{dt^2} + 3 \frac{dx}{dt} + 2x(t) = 5$$

$$(s^2 + 3s + 2) x(s) = 5$$

$$x(s) = \frac{5}{s^2 + 3s + 2}$$

$$t \rightarrow \infty, s \rightarrow 0$$

$$\lim_{t \rightarrow \infty} f(t) = \lim_{s \rightarrow 0} sF(s) = \lim_{s \rightarrow 0} \left[\frac{s \cdot 5}{s^2 + 3s + 2} \right] = 0$$

$$\lim_{t \rightarrow \infty} f(t) = 0$$

47. () As $t \rightarrow \infty \Rightarrow S \rightarrow 0$

$$\lim_{s \rightarrow 0} sF(s) = \frac{s[5s^2 + 23s + 6]}{s(s^2 + 2s + 2)} = 3$$

$$\lim_{s \rightarrow 0} sF(s) = 3$$

$$48. () F(z) = \frac{1}{z+1} = 1 - \frac{1}{z^{-1}+1}; c$$

inverse z-transform to $8(k) - (-1)^k; k \geq 0$

49. ()

50. ()

$$51. () (i) E \propto \text{speed}; \frac{50KW}{P} = \frac{1}{\left(\frac{1}{2}\right)}; P = 25KW$$

Power $\propto E$.

(ii) In field control, speed is above rated speed by reducing field flux

$$\therefore E = \frac{\phi z N P}{60 a}; E \propto (\phi N)$$

$$\phi \downarrow N \uparrow$$

E is constant

$$P = 50 \text{ KW}$$

52. () Torque = $K_a \phi I_a$

$$E = K_a \phi \omega_m$$

$$P = EI_a = K_a \phi \omega_m I_a$$

53. ()

54. ()

55. ()

56. ()

57. ()

$$\frac{Te(st)}{Te(fl)} = \left(\frac{Ist}{IfI} \right)^2 sfl$$

$$= 6^2 \times 0.004$$

$$\frac{Te(st)}{Te(fl)} = 1.44$$

58. ()

$$x_s = 0.4 \Omega / km$$

$$x_m = 0.1 \Omega / km$$

$$x_0 = x_s + 2x_m$$

$$x_0 = 0.62 \Omega / km$$

$$x_l = x_s - x_m = 0.3 \Omega / km$$



59. () Power factor 0.97 lag is due to capacitor installed.

$$\therefore Q = P \tan \phi = 4 \times \tan [\cos^{-1} (0.97)]$$

$$Q = 1 \text{ MVAR}$$

$$P = 4 \text{ MW}$$

If capacitor goes out of service,

$$Q = P \tan \phi \rightarrow P = \frac{Q}{\tan \phi} \rightarrow \tan \phi = \frac{2+1}{4} = 0.75$$

$$\cos \phi = 0.8 \text{ lag}$$

$$Q = 2+1=3$$

60. ()

$$Y_{22} = j0.1 - j20 + j0.1 = -j19.8$$

$$Y_{22} = -j19.8$$

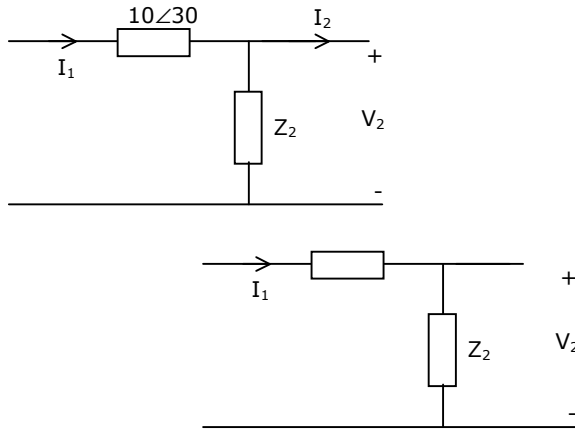
$$\frac{dF_1}{dP_1} = \frac{dF_2}{dP_2};$$

61. () $b + 2CP_1 = b + 4CP_2$

$$P_1 = 2P_2; P_1 + P_2 = 150$$

$$P_1 = 100, P_2 = 400$$

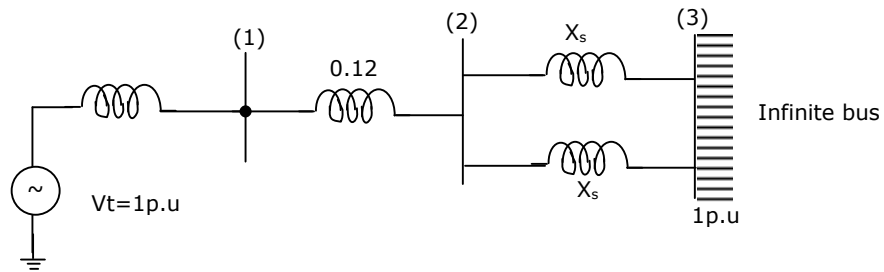
62. () $I_2=0, C = \frac{I_1}{\sqrt{2}} = \frac{1}{Z_2}$



$$Z_2 = 40 \angle -45$$

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63. ()



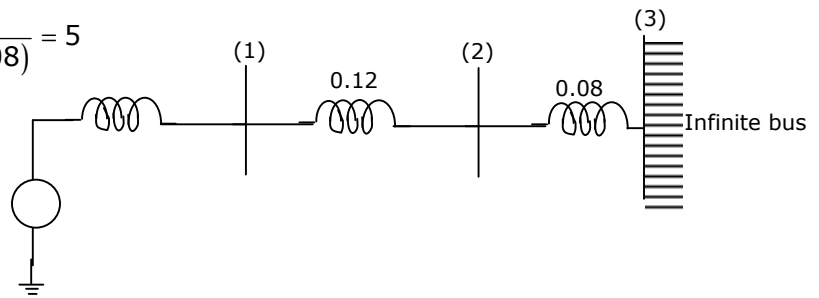
$$P = \left(\frac{Vt_1 \times Vt_2}{X_s} \right) \sin \delta$$

$$P_{\max} = \frac{Vt_1 Vt_2}{X_s}$$

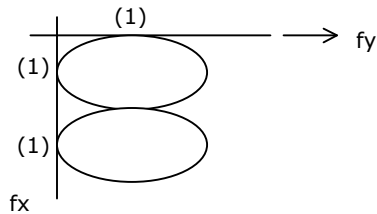
$$6.25 = \frac{1 \times 1}{\left(\frac{X_s}{2} + 0.12 \right)}$$

$$X_s = 0.08$$

$$P_{\max_{\text{now}}} = \frac{1 \times 1}{(0.12 + 0.08)} = 5$$



64. ()



$$\frac{f_y}{f_x} = \frac{\text{No. of intersections of the horizontal line with curve}}{\text{No. of intersections of the vertical line with curve}} = \frac{1}{2}$$

$$f_x = \frac{4}{2\pi} \quad x(t) = P \sin(4t + 30)$$

$$f_y = \frac{2}{2\pi}; \quad \omega_x = 4 = 2\pi f_x$$

$$\omega_y = 2$$

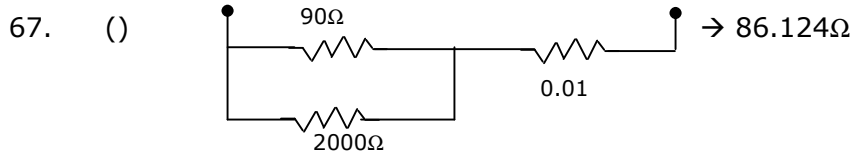
$$y(t) = Q \sin(2t + 15)$$

65. () Multiplying power $m = \frac{I}{I_m} = \frac{500}{100} = 5$

$$m = 5;$$

$$m = 1 + \frac{R_m}{R_{\text{shint}}} = 5 \Rightarrow R_{\text{short}} = \frac{0.1}{4} = 0.025\Omega$$

66. ()



$$\text{error} = \frac{90 - 86.124}{86.124} = 4.5\%$$

68. ()

69. () $W_1 = 10.5$

$$W_2 = -2.5$$

$$W = W_1 + W_2; W = 8 \text{ kW}$$

$$\tan \phi = \sqrt{3} \left(\frac{w_1 - w_2}{w_1 + w_2} \right) = \sqrt{3} \left[\frac{10.5 - (2.5)}{10.5 + 2.5} \right]$$

$$\phi = 70.43$$

$$\cos \phi = 0.3347$$

70. ()

$$I_E = 1 \text{ mA}, \alpha = \frac{\beta}{\beta + 1} = 0.9909$$

$$\beta = 100$$

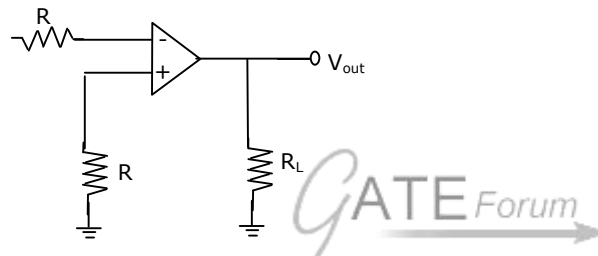
$$I_C = \alpha I_E = \left(\frac{100}{101} \right) \text{ mA} = 990.099 \mu\text{A}$$

$$I_C = \beta I_B, I_B = 9.9 \mu\text{A} \approx I_B = 10 \mu\text{A}$$

71. ()

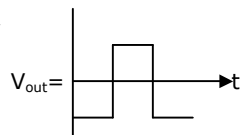
72. ()

73. ()



Here op-amp in saturation.

So,

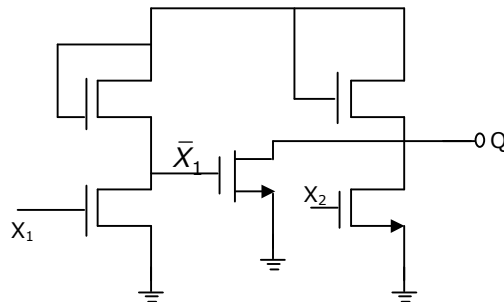


$$\bar{Q} = X_2 + \bar{X}_1;$$

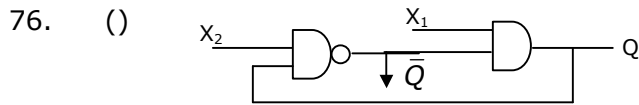
$$Q = X_1 \bar{X}_2$$

74. () Ambiguous

75. ()



$$\bar{Q} = X_2 + \bar{X}_1; Q = X_1 \bar{X}_2$$



$x_1 = x_2 = 1$; Q is always toggling
so, Q is unstable.

77. () Even though voltage across the device $\rightarrow 0$, current is flowing
so device is turn on

$$\text{Energy lost} = \frac{1}{2} VI(t_1 + t_2)$$

78. ()

79. () $V_S = 100V$ $f = 1 \text{ KHz}$
 $R_L = 5$ $D = 0.5$
 $L = 200 \text{ mH}$ $T = 1 \text{ msec.}$

$$T_a = \frac{L}{R_L} = 40 \text{ msec.}$$

Ripple current in the load current is

$$\begin{aligned} &= \frac{V_S}{R} \left[\frac{\left(1 - e^{-\frac{\alpha T}{T_a}}\right) \left(1 - e^{-\frac{(1-\alpha)T}{T_a}}\right)}{1 - e^{-\frac{T}{T_a}}} \right] \\ &= \frac{100}{5} \left[\frac{\left(1 - e^{-\frac{1}{2} \times \frac{1}{40}}\right) \left(1 - e^{-\frac{1}{2} \times \frac{1}{40}}\right)}{\left(1 - e^{-\frac{1}{40}}\right)} \right] \end{aligned}$$

$$\text{Ripple current} = 0.1249 \approx 0.125A$$

80. () $\text{Test} = Tl + J \left(\frac{d\omega}{dt} \right) = Tl + J(a)$

$$15 = 7 + J(2) \Rightarrow J = 4 \text{ Nm}^2$$

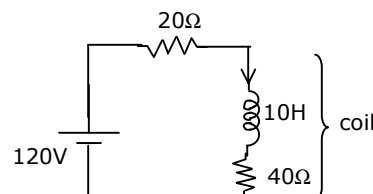
81. (A) ()

$$V_{out} = \frac{V_{max}}{2\pi} (1 + \cos \alpha) = V_{o(rms)} (1 + \cos \alpha)$$

$$V_{out} = 230V, V_o = 230$$

$$\alpha = 90$$

Position 1:



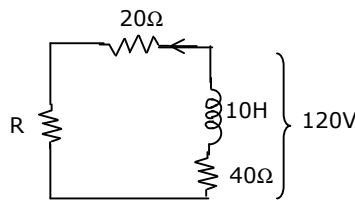
$$I_{\text{coil}} = \frac{120}{40 + 20} = 2A$$

Inductor acts as a short circuit.

Position 2:

$$120V = (20 + R) 2$$

$$R = 40\Omega$$



(B) () Total resistance = $40 + 40 + 20 = 100\Omega = R$

$$\text{Time constant} = \frac{R}{L} = \frac{100}{10} = 10 \text{ sec}$$

$$\therefore i(t) = 2e^{-10t}$$

$$\text{Balance energy left} = 100 - 95 = 5\% = 0.05.$$

Since the stored energy is proportional to the square of the current, the current at this instant is

$$i = \sqrt{0.05} \times \text{initial current}$$

$$= 2\sqrt{0.05}$$

$$2\sqrt{0.05} = 2e^{-10t} \Rightarrow t = 0.15 \text{ sec.}$$

82. (A) ()

$$A = \begin{bmatrix} 0 & 1 \\ 0 & -3 \end{bmatrix} B = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

$$X(0) = \begin{bmatrix} -1 \\ 3 \end{bmatrix}$$

$$\phi(t) = L^{-1} \left[(SI - A)^{-1} \right] = L^{-1} \left[\left[\begin{pmatrix} S & 0 \\ 0 & S \end{pmatrix} - \begin{pmatrix} 0 & 1 \\ 0 & -3 \end{pmatrix} \right]^{-1} \right]$$

$$= L^{-1} \left[\left[\begin{pmatrix} S & -1 \\ 0 & S+3 \end{pmatrix} \right]^{-1} \right] = L^{-1} \begin{bmatrix} \frac{1}{s} & \frac{1}{s(s+3)} \\ 0 & \frac{1}{s+3} \end{bmatrix}$$

$$\phi(t) = \begin{bmatrix} 1 & \frac{1}{3}(1 - e^{-3t}) \\ 0 & e^{-3t} \end{bmatrix}$$

(B) ()

$$\begin{aligned}
 x(t) &= L^{-1} \left[(SI - A)^{-1} [x(0) + BVCS] \right] \\
 &= L^{-1} \left[\begin{bmatrix} \frac{1}{s} & \frac{1}{s(s+3)} \\ 0 & \frac{1}{s+3} \end{bmatrix} \left\{ \begin{pmatrix} -1 \\ 3 \end{pmatrix} + \begin{pmatrix} \frac{1}{s} \\ 0 \end{pmatrix} \right\} \right] \\
 &= L^{-1} \left[\begin{bmatrix} \frac{1}{s} & \frac{1}{s(s+3)} \\ 0 & \frac{1}{s+3} \end{bmatrix} \left\{ \begin{pmatrix} -1 + \frac{1}{s} \\ 3 \end{pmatrix} \right\} \right] \\
 &= L^{-1} \left[\begin{bmatrix} \frac{1}{s^2} - \frac{1}{s} + \frac{3}{s(s+3)} \\ \frac{3}{s+3} \end{bmatrix} \right] \\
 x(t) &= \begin{bmatrix} t - e^{-3t} \\ 3e^{-3t} \end{bmatrix}
 \end{aligned}$$

83. (A) () $S = 1000 \text{ KVA}, 6.6 \text{ KV}, \lambda, 3\text{-phase}$

$$X_s = 20\Omega$$

$$\text{p.f} = 1$$

$$S = \sqrt{3} V_L I_L \cos \phi, 1000 \times 10^3 = \sqrt{3} \times 6600 \times I_L \times 1$$

$$I_L = 87.47 (L - L)$$

$$E_{ph} = V_{ph} + jI_{ph} \times s = 3810.62 + j1749.4$$

$$E_{ph} = 4192.99V$$

$$E_{induced} = 7.262KV \text{ } L - L$$

- (B) () $KW = KVA \cos \phi$

$$P = 1000 \text{ KW}$$

$$10000 = \frac{7.2 \times 10^3 \times 6.6 \times 10^3}{20} \sin \delta$$

$$\delta = 24,88$$

84. (A) () When a 3- ϕ , fault occurs, the fault current is limited by the positive sequence reactance only

$$\therefore 4000 \times 10^6 = 220 \times 10^3 \times I$$

$$I = \frac{220 \times 10^3}{X}$$

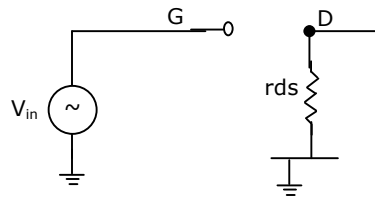
$$X \text{ positive} = 12.1\Omega$$

- (B) ()

85. (A) () $I_m = \frac{\partial i_{ds}}{\partial V_{gs}} = 1ms$

- (B) () $A_v = -gm \text{ } r_{ds}$

small signal equivalent circuit is



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