

Teacher Support Materials 2009

Maths GCE

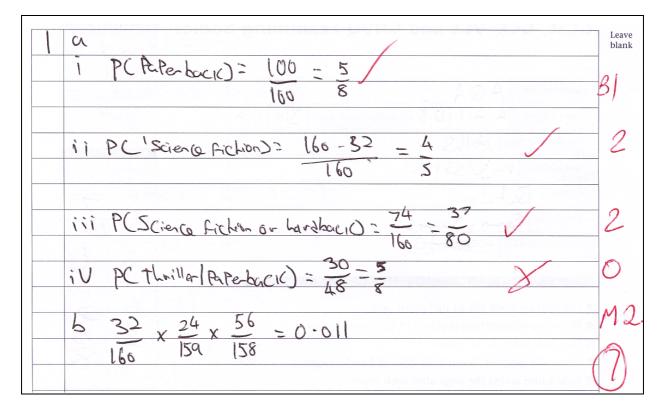
Paper Reference MS/SS/1B

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			Subject of	category		
		Crime	Romance	Science fiction	Thriller	Total
Turn	Hardback	8	16	18	18	60
Тур	Paperback	16	40	14	30	100
(a) A book	Total ok is selected at is:	24 random fro	56 m the bookca	32 ase. Calcula	48 te the probab	160 bility that the
	ok is selected at	random fro				
bool (i)	ok is selected at is: a paperback;	random fro on;	m the bookca			pility that the

Calculate, to three decimal places, the probability that one is crime, one is romance and one is science fiction. (4 marks)

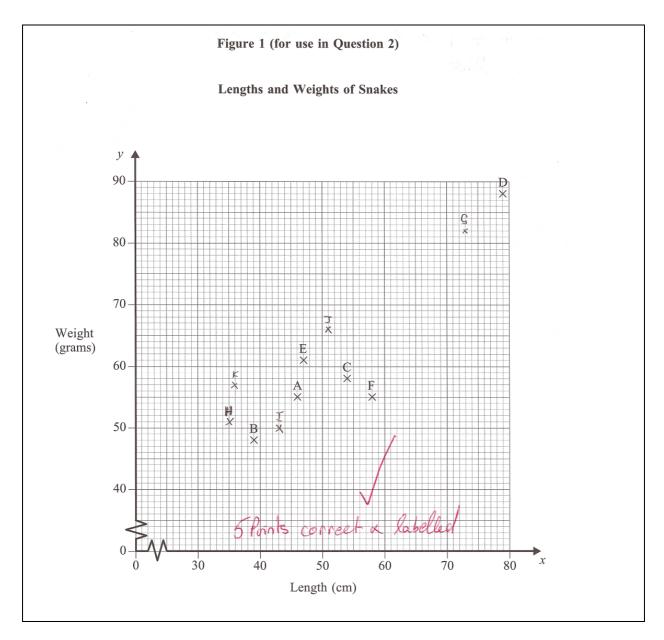


As was usually the case, the candidate has scored full marks in parts (a)(i), (ii) & (iii), although in the latter part an incorrect answer of $\frac{92}{160}$ was regularly seen. Part (a)(iv) was often more of a challenge and here the candidate has found P(Paperback | Thriller). The candidate's answer to part (b) was by far the most common. The three correct subject totals have been divided by 160, 159 & 158 respectively (those who used 160³ lost a further mark) but no account has been taken of the 3! = 6 permutations.

Q	Solution	Marks	Total	Comments
1(a) (i)	P(P) = 100/160 = 50/80 = 25/40 = 10/16			In (a), ratios (eg 100:160) are only penalised by 1 mark at first correct answer
	= 5/8 = 0.625	B1	1	CAO
(ii)	$P(S') = 1 - \frac{32}{160}$ or $P(S) = \frac{32}{160}$	M1		Or equivalent Ignore labels of <i>S</i> ′ & <i>S</i> Can be implied by correct answer
	= $128/160 = 64/80 = 32/40 = 16/20 = 8/10$ = $4/5 = 0.8$	A1	2	CAO
(iii)	$\frac{60+32-18}{160} \text{ or } \frac{60+14}{160} \text{ or } \frac{32+8+16+18}{160}$	М1		Or equivalent Can be implied by correct answer
	= 74/160 = 37/80 = 0.462 to 0.463	A1	2	CAO/AWFW (0.4625)
(iv)	$P(T P) = \frac{\frac{30}{160}}{(i)}$	M1		Or equivalent Can be implied by correct answer But watch for $\frac{18}{160}$ or $\frac{48}{160}$
	= 3/100 = 3/10 = 0.3	A1	2	CAO
(b)	P(1C & 1R & 1S) =			
	$\frac{24}{160} \times \frac{56}{159} \times \frac{32}{158}$	M1		Multiplication of any 3 different given subject totals
	160 159 158	M1		Multiplication of 160, 159 & 158
	$(0.15 \times 0.35220 \times 0.20253) \times 6$	M1		Accept 3dp accuracy Award for $3 \le$ multiplier ≤ 6
	= 0.064 to 0.0644	A1		AWFW (0.0642) Do not accept a fraction as answer A correct answer can imply 4 marks
	Special Case:			
	(Any given subject total) + 160 seen anywhere in (b)	(M1)	4	Can award if no marks scored in (b) Accept a decimal equivalent
	seen anywhere in (0)	Total	11	Accept a ucciniar equivatent

,												
	Snake	Α	В	С	D	Е	F	G	Н	Ι	J	K
	x	46	39	54	79	47	58	73	35	43	51	36
	у	55	48	58	88	61	55	82	51	50	66	57
)	Interpret	your v	value ir	n conte	xt.							en x : (- (-
ĺ	Interpret On Figu	-				liagran	n for th	nese da	ta.			(.
b) c) d)	-	re 1, c	omplet	e the s	catter of					le and		(- (- (-
c)	On Figu Subsequ (i) Gi	re 1, c ently it ven tha	omplet	e the s nd that le adul	catter of , of the t snake	e 11 ad s are g	ult sna enerall	kes, 9 y large	are ma er than	male a	2 are 1	(- (4 (4 femal

number 2)aj	r=0.89 Not 385	Leave blank O.
b)	There is a strong positive correlation between length of snakes and their weights	BZ.
Q	[Figure 1]	2
dji 📣	Female snakes - Snakes G and D	31
13	r≈0.2	80
	<u>revised part ()</u> For male snakes, there is a weak positive correlation between length and weight	60 7
		()



Whilst many candidates scored full marks for this question, the above solution illustrates some common errors that lost marks. Given Instruction 5 on the Front Page of the Question Paper, the value of r was required to at least three decimal places. Part (b) required a reference to the strength and the sign of the correlation in context; all referenced here. The 5 points are accurately plotted and labelled (candidates were penalised for omitting the latter). The candidate has identified the two most likely female snakes but the estimated value of r for the remaining 9 male snakes is outside the acceptable range of 0.25 to 0.75, actual value is 0.488. Despite a correct revised interpretation, the final mark is not available as it is dependent upon the estimated value of r being within the acceptable range.

Q	Solution	Marks	Total	Comments
2(a)	r = 0.893 to 0.8933	B3		AWFW (0.89319)
	r = 0.89 to 0.896	(B2)		AWFW
	r = 0.8 to 0.95	(B1)		AWFW
	or			
	Attempt at $\sum x \sum x^2 \sum y \sum y^2 \&$ $\sum xy$	(M1)		561 30667 671 42613 & 35882 (all 5 attempted)
	Attempt at S_{xx} S_{yy} & S_{xy}	(111)		2056 1682 & 1661 (all 3 attempted)
	Attempt at correct corresponding formula for r	(m1)		
	r = 0.893 to 0.8933	(A1)	3	AWFW
(b)	Fairly strong / strong / very strong positive (linear) correlation / relationship / association / link (but not trend)	B1dep		Or equivalent; must qualify strength and indicate positive Dependant on $0.8 \le r \le 0.95$ B0 for some/average/medium/etc
	between			
	length and weight of adult snakes	B1	2	Context; providing $0 \le r \le 1$
(c)	Figure 1: 5 correct labelled points 4 or 3 correct labelled points	B2 (B1)	2	Deduct 1 mark if points not labelled
(d)(i)	D and G	B1	1	Both CAO
(ii)	r = 0.25 to 0.75	B1		AWFW (0.48790) No penalty for calculation Accept a range only if whole of it falls within 0.25 to 0.75
	Fairly weak / weak / some / moderate positive (linear) correlation / relationship / association / link	B1dep	2	Or equivalent; must qualify strength and indicate positive Dependant on $0.25 \le r \le 0.75$ B0 for very weak/little/slight/hardly
	Do not accept comparison with value in (a) or statement in (b)			any/fair/average/medium/anything involving strong/etc
		Total	10	

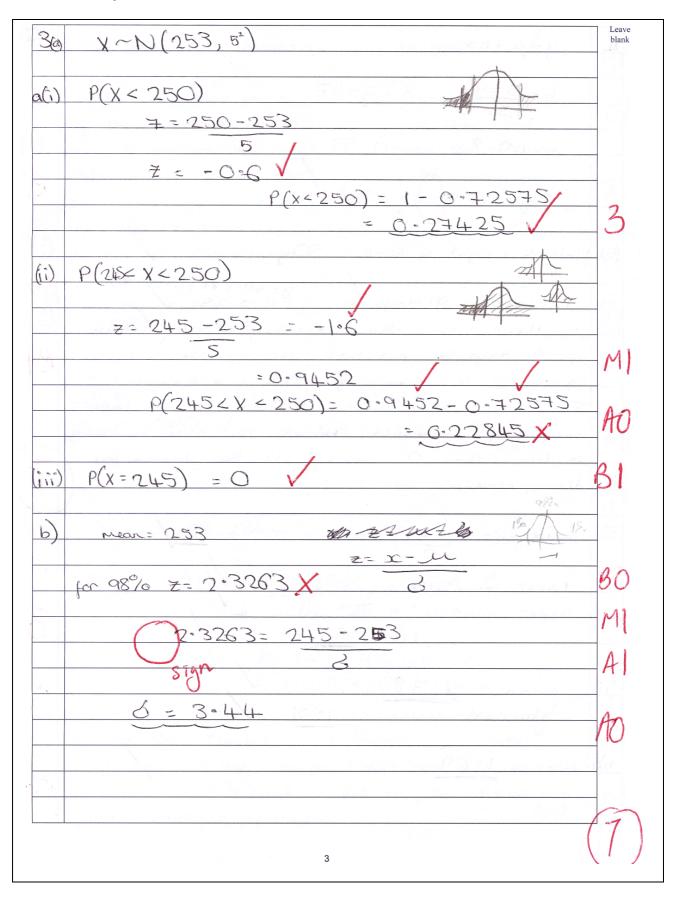
- 3 The weight, X grams, of talcum powder in a tin may be modelled by a normal distribution with mean 253 and standard deviation σ .
 - (a) Given that $\sigma = 5$, determine:

(i)
$$P(X < 250)$$
; (3 marks)

(ii) P(245 < X < 250); (2 marks)

(iii)
$$P(X = 245)$$
. (1 mark)

(b) Assuming that the value of the mean remains unchanged, determine the value of σ necessary to ensure that 98% of tins contain more than 245 grams of talcum powder. (4 marks)



The normal distribution sketches have enabled the candidate to identify the appropriate areas (< 0.5 or > 0.5) and only an arithmetic slip has prevented full marks in part (a)(ii). Many candidates gave an answer of 0.72575 to part (a)(i) and one of 0.67095 to part (a)(ii). Such answers only scored a total of 1 or 2 marks. About 50% of candidates attempted calculations in part (a)(iii) for no reward whatsoever. The above answer to part (b) shows the two most common errors; an incorrect *z*-value coupled with the mysterious loss of a negative sign!

Q	Solution	Marks	Total	Comments
3(a)	$X \sim N(253, 5^2)$			
(i)	$P(X < 250) = P\left(Z < \frac{250 - 253}{5}\right) =$	М1		Standardising (249.5, 250 or 250.5) with 253 and $(\sqrt{5}, 5 \text{ or } 5^2)$ and/or (253 – x)
	P(Z < -0.6) = 1 - P(Z < 0.6) = 1 - 0.72575	ml		Area change; may be implied
	= 0.274 to 0.275	A1	3	$\begin{array}{ll} AWFW & (0.27425) \\ (1 - answer) \Rightarrow M1 max \end{array}$
(ii)	P(245 < X < 250) = [C's(a)(i)] - P(X < 245)	M1		Or equivalent; must be clear correct method if answer incorrect and answer > 0
	= (i) - P(Z < -1.6) = 0.27425 - 0.0548			
	= 0.219 to 0.22(0)	A1	2	AWFW (0.21945) M1 A0 for $[1 - (i)] - 0.0548 = 0.67095$ M0 A0 for $0.9452 - [(i)] = 0.67095$ M1 A1 for $0.9452 - [1 - (i)] = 0.21945$
(iii)	P(X=245) = 0 or zero or impossible	B1	1	Ignore any working B0 for 'for impossible to calculate'
(b)	98% (0.98) $\Rightarrow z = -2.05$ to -2.06	B1		AWFW; ignore sign (-2.0537)
	$z = \frac{245 - 253}{\sigma}$	M1		Standardising 245 with 253 and σ ; allow (253 – 245)
	= -2.0537	A1		Only allow: ±2.05 to ±2.06 ±2.32 to ±2.33
	σ = 3.88 to 3.9(0) Note:	A1		AWFW (3.8954)
	$\frac{245-253}{\sigma} = 2.0537 \implies \sigma = 3.8954$			
	\Rightarrow B1 M1 A1 A0		4	Or equivalent inconsistent signs
		Total	10	

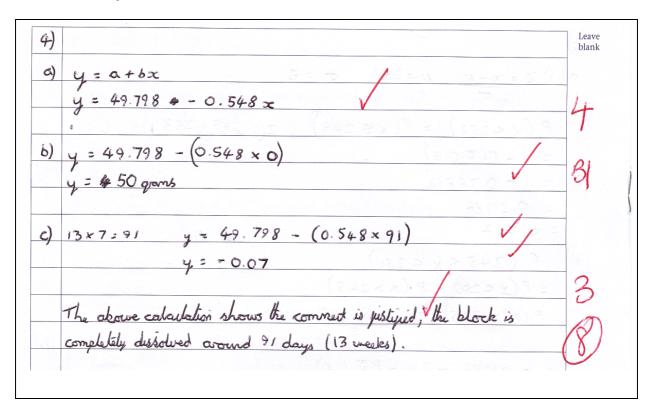
Question 4

4 As part of an investigation, a chlorine block is immersed in a large tank of water held at a constant temperature. The block slowly dissolves, and its weight, y grams, is noted x days after immersion. The results are shown in the table.

x days	5	10	15	20	30	40	50	60	75
y grams	47	44	42	38	35	27	23	16	9

- (a) Calculate the equation of the least squares regression line of y on x. (4 marks)
- (b) Hence estimate, to the nearest gram, the initial weight of the block. (1 mark)
- (c) A company which markets the chlorine blocks claims that a block will usually dissolve completely after about 13 weeks. Comment, with justification, on this claim. (3 marks)

Student Response



Commentary

Undoubtedly, the best answered question on the paper with a mode of 8 marks. The above illustrates a typical concise solution. A correct equation (to appropriate accuracy – not –0.55) followed by the (rather unnecessary) substitution of x = 0 with an answer as requested to the nearest gram. In part (c), the candidate has shown the necessary substitution of 91 to give $y \approx 0$ followed by a sensible conclusion. At this final step, a minority of candidates felt that any (minute) weight disproved the claim! Those candidates who substituted y = 0 to give $x \approx 91$ were equally rewarded. However comments only referencing 'extrapolation' did not gain full marks.

Q	Solution	Marks	Total	Comments
4(a)	b (gradient) = -0.5485 to -0.5475	B2		AWFW (-0.54814)
	b (gradient) = -0.55 to -0.54	(B1)		AWFW
	Omission of -ve sign	(B0)		
	a (intercept) = 49.7 to 49.9 a (intercept) = 49 to 50	B2 (B1)		AWFW (49.7982) AWFW
	or	(61)		Awrw
				305 14975 281 & 6980 (10173)
	Attempt at $\sum x \sum x^2 \sum y \& \sum xy (\sum y^2)$			(all 4 attempted)
	or	(M1)		
	Attempt at S_{yy} & S_{yy}			4638.89 & -2542.78
	-7 -7	(m1)		(both attempted)
	Attempt at correct formula for b (gradient) b (gradient) = -0.5485 to -0.5475	(A1)		AWFW
	a (intercept) = 49.7 to 49.9	(A1) (A1)	4	AWFW
	a (mercept) = 45.7 to 45.5	(AI)	7	AWIW
				If a and b not identified
	Accept a & b interchanged only if identified			anywhere in question, then:
	correctly by a clearly shown equation (stated			-0.5485 to -0.5475 ⇒ B1
	answers are not sufficient) in (b) or (c)			49.7 to 49.9 ⇒ B1
(b)				
(0)	C's value of intercept from (a) providing > 47			Accept value rounded to nearest
	or	B1F	1	integer (50)
	Value 50 stated even if (a) incorrect or not		-	()
	attempted			
(c)	13 weeks ⇒ 91 days	B1		Stated or used
				Accept a descriptive answer that
		DI		includes 91 and a value in range AWFW (-0.08254)
	y = -1.1 to $+ 1.1$	B1		AWFW (-0.08254)
	01			
	$y = 0 \implies x = 89$ to 93	(B1)		AWFW (90.84942)
	v			Accept a descriptive answer that
				includes a value in range and 13
	\Rightarrow 13 weeks (approximately)	(B1)		Stated
	Note:			
	B1 B1 or (B1) (B1) are available even if (a) not attempted			
	not aucilipicu			
				Or equivalent; ignore reasoning
	Thus claim appears justified	D1 J		unless contradictory
	or Thus tablet likely to have dissolved	B1 dep		Dependent upon 2nd B1 in (c) or 2nd
	-			(B1) in (c)
	or			
	Extrapolation required so cannot comment	(B1)		Not dependent
	Excaporation required so cannot confinent	(11)		rot dependent
	Note:			
	If (B1) for extrapolation maximum mark is 2;			
	other mark available is for 91		3	
		Total	8	
	1		-	

Question 5

The	result	s, for the 99 households with ch	nildrer	n, are	shown	in th	e tabl	e.		
		Number of children (x)	1	2	3	4	5	6	7	
		Number of households (f)	14	35	25	13	9	2	1	
(a)	For t	hese 99 households, calculate v	alues	for:						
	(i)	the median and the interquarti	le ran	ge;						(3 marks
	(ii)	the mean and the standard dev	iation	1.						(3 marks
(b)	In fa	ct, 163 households were survey	ed, of	whic	h 64 d	contain	ned no	o child	lren.	
	(i)	For all 163 households, calcul- household.	ate th	e valu	e for	the me	ean ni	ımber	of ch	ildren per (2 marks
	(ii)	State whether the value for the 163 households, will be smalle in part (a)(ii).				~				
	(iii)	It is claimed that, for all 163 l household may be modelled a					· · · · ·			children per
		Comment, with justification, of other than the discrete nature of the second se			n. Yo	ur con	nment	shou	ld refe	er to a fact (2 marks

 $\frac{Median}{2} = \frac{(n+1)^{th}}{2} \text{ piece of data} = \frac{99+1}{2}$ Sai Leave = 80th blank 2 BI - 3 children. ian = ua - La UQ 3/99+1 =25# = 7 th LQ = 99+1 A children child ren • 2 32. 2 children -Sali BI 2:78 245 (354) 1 -Mean = Ex -99 n 32 50 = 1522 (35F) Srx -1.31 9 1 N-I 98 MI 20 -1.69 (35F) Sbi 275 Mean = AI 163 BI Sbii It will be larger but depon reason. V not Shii 4 b modelled by can normal a distribution as it is not random Sample, a people will decide how many they children want to have.

Unlike here, it was not unusual to simply see stated correct answers to parts (a)(i) & (ii). Where such stated answers were incorrect, often 3 or even 6 marks were lost. Many candidates, as here, also answered parts (b)(i) & (ii) correctly; some even obtaining 1.69 after making a total mess of part (a)(ii). Almost all answers to part (a)(iii), as here, were incorrect though usually claiming 'correct' due to either a large sample or the CLT. This revealed a marked lack of knowledge of the latter. A large (>30 say) sample enables one to assume that the sample mean is approximately normally distributed; not the sample and certainly not the population!

Q	Solution	Marks	Total	Comments
5(a) (i)	Median (50) = 3 If not identified, then assume order is median then IQR	B1		CAO Do not award marks if correct answers are based on shown incorrect method; eg accept use of
	IQR(75-25) = 4 - 2 = 2	B2		99/2, etc but not 276/2, etc CAO; but 25^{th} value \Rightarrow IQR = 2 \Rightarrow B0
	Special Cases: Identification that $LQ = 2$ and $UQ = 4$	(B1)		Both CAO
	Statement of ≥4 cumulative frequencies F: 14 49 74 87 96 98 99	(M1)	3	Can award if no marks scored in (i) even if then applied to continuous data
(ii)	Mean = $\frac{\sum fx}{\sum f} = \frac{275}{99} = 2.77$ to 2.78	B1		AWFW (2.778)
	If not identified, assume order is \overline{x} then s SD $(\sum fx^2 = 933) = 1.3(0)$ to 1.32	B2		Treat rounding to integers as ISWAWFW(1.307 & 1.314)
	Special Case: Evidence of $\frac{\sum fx}{99}$	(M1)	3	Can award if no marks scored in (ii)
(b)(i)	Mean ₁₆₃ = $\frac{99 \times \text{Mean}_{99}}{163}$ or $\frac{\sum fx \text{ from}(a)(ii)}{163}$	M1		Or equivalent; may be implied by an answer within range
	= 1.68 to 1.69	A1	2	AWFW (1.687)
(ii)	Increase	B1	1	CAO; or equivalent (1.696) Ignore any working (1.702)
(iii)	Data is (positively/negatively) skewed / not symmetric / bimodal / not bell-shaped from frequency distribution / given table			
	or [C's mean in (b)(i)] - 2 × [C's SD in (a)(ii)] < 0	B1		Or equivalent
	or [C's mean in (b)(i)] - 2×[1.69 to 1.71] < 0			(-1.75 to -0.90)
	Thus claim appears not valid	B1 dep	2	Or equivalent Dependent upon previous B1
	Total		11	

6 (a) The time taken, in minutes, by *Domesat* to install a domestic satellite system may be modelled by a normal distribution with unknown mean, μ, and standard deviation 15.

The times taken, in minutes, for a random sample of 10 installations are as follows.

47 39 25 51 47 36 63 41 78 43

Construct a 98% confidence interval for μ .

(b) The time taken, Y minutes, by *Teleair* to erect a TV aerial and then connect it to a TV is known to have a mean of 108 and a standard deviation of 28.

Estimate the probability that the mean of a random sample of 40 observations of Y is more than 120. (4 marks)

(5 marks)

(c) Indicate, with a reason, where, if at all, in this question you made use of the Central Limit Theorem. (2 marks)

Student Response

$\hat{b}_{\alpha} = 47$	Leave blank B
	BO
$CI = m \bar{z} \pm z \times f$	MI
1.98℃I= 47±2.0537× =	AI
=(37.26,56.74)	AO
$6 b \times n (108, 28^2)$	
$Variance = \frac{\sigma^2}{n}$	
$=\frac{784}{40}$	
= 19.6	
$P(Y > 120) = P(z > \frac{120 - 108}{\sqrt{19.6}})$	
= P(z > 2.71)	
$= 1 - P(z \le 2 \cdot 7 i)$	4
= 1 - 0.99664 = 0.00336	RI
6) c) In part (b); the sample size was sufficiently large (i.e. >30)	
for the Central Cimit Theorem to apply.	
for the server through the group	81

Commentary

Very few candidates scored full marks here; the above illustrates typical mistakes. Perhaps as a result of Question 3(b), the candidate has used an incorrect *z*-value in part (a) and so lost 2 of the 5 marks. Part (b) involving standard error is completely correct; illustrating the noticeable improvement. Standardising using $\sigma = 28$ lost all 4 marks. In answering part (c), the candidate has identified (b) correctly but, in common with almost all candidates, has not given the correct reason **that the distribution of Y was unknown**.

Q	Solution	Marks	Total	Comments
6(a)	Mean = $\frac{470}{10}$ = 47	B1		CAO
	98% (0.98) $\Rightarrow z = 2.32$ to 2.33	B1		AWFW (2.3263)
	CI for μ is $\overline{x} \pm z \times \frac{\sigma}{\sqrt{n}}$	M1		Used Must have \sqrt{n} with $n \ge 1$
	Thus $47 \pm 2.3263 \times \frac{15}{\sqrt{10}}$	A1F		F on \overline{x} and z only
	Hence 47 ± 11.0 to 11.1 Or (35.9 to 36.0, 58.0 to 58.1)	A1	5	CAO & AWRT (accept 11) AWRT (accept 36 & 58)
(b)	$Y \sim N(108, 28^2)$			
	Variance of $\overline{Y}_{40} = 28^2/40 = 19.6$ $\sqrt{\text{SD}}$ of $\overline{Y}_{40} = 28\sqrt{40} = 4.425$ to 4.43	B1		CAO Stated or used AWFW
	$P(\overline{Y}_{40} > 120) = P\left(Z > \frac{120 - 108}{28/\sqrt{40}}\right)$	M1		Standardising 120 with 108 and $\sqrt{19.6}$ or (4.425 to 4.43) or equivalent; allow (108 – 120)
	= P(Z > 2.71) = 1 - P(Z < 2.71)	ml		Area change; may be implied
	= 1 - 0.99664 = 0.0033 to 0.0034	A1	4	AWFW (0.00336) (1 - answer) \Rightarrow B1 M1 max
(c)	Part (b) or Teleair times	B1		Or equivalent; ignore reasoning
	Distribution of Y not known	B1		Or equivalent; must be clear reference to Y or population B0 for $n > 30$
	Note: To score B1 B1 there must be both a clear indication of where in question and a valid reason		2	Any reference to part (a) \Rightarrow B0 B0
		Total	11	

- 7 Mr Alott and Miss Fewer work in a postal sorting office.
 - (a) The number of letters per batch, *R*, sorted incorrectly by Mr Alott when sorting batches of 50 letters may be modelled by the distribution B(50, 0.15).

Determine:

- (i) $P(R \le 10)$;
- (ii) $P(5 \le R \le 10)$.

(4 marks)

- (b) It is assumed that the probability that Miss Fewer sorts a letter incorrectly is 0.06, and that her sorting of a letter incorrectly is independent from letter to letter.
 - (i) Calculate the probability that, when sorting a batch of 22 letters, Miss Fewer sorts exactly 2 letters incorrectly. (3 marks)
 - (ii) Calculate the probability that, when sorting a batch of 35 letters, Miss Fewer sorts at least 1 letter incorrectly. (2 marks)
 - (iii) Calculate the mean and the variance for the number of letters sorted correctly by Miss Fewer when she sorts a batch of 120 letters. (2 marks)
 - (iv) Miss Fewer sorts a random sample of 20 batches, each containing 120 letters. The number of letters sorted correctly per batch has a mean of 112.8 and a variance of 56.86.

Comment on the assumptions that the probability that Miss Fewer sorts a letter incorrectly is 0.06, and that her sorting of a letter incorrectly is independent from letter to letter. (3 marks)

Leave 7) blank a) $\times \sim B(50, 0.15)$ $P(R < 10) = P(R \leq 9)$ BI = 0.7911 = 0.791 $ii) P(S \leq R \leq 10)$ $= P(R \le 10) - P(\le 5)$ = 0.8801- 0.2194 M2 = 0.661 b) i) $\binom{22}{300} \times 0.06^2 \times 0.94^{20} \times \sqrt{5} (22, 0.06)$ 3 2 = 0.241 ii) x~B(35,0.06) (35) × 0.06 × 0.94 34 = 0.256 ()1-0.256=0.744 X 11) mean = np = 120 × 0.94 = 112.8 V 2 Varanie = ng (1-p) = 112.8 × (0.06) = 6.77 BI iv) The means both have the same value of 112.8, however the The pobability of 0.06 is therefore incorrect. The asunction BO the each letter is gorted meen independently carrot be commented BO on by only looking at the mean and variance. We would ned More information. 6

Whilst most candidates scored quite well on this question, few gained full or nearly full marks. Marks were often lost in part (a) for quoting 0.8801 as the answer to (i) and/or, as here, using one incorrect value in (ii). Whilst it was very rare indeed to see an incorrect answer to part (b)(i), it was equally rare to see a correct answer to part (b)(ii). The above illustrates a typical error of calculating 1 - P(1) rather than 1 - P(0). In common with this candidate, almost all candidates were able to score full marks in part (b)(iii), though a minority ignored the word '**correctly**'. In order to score any marks in part (b)(iv), a **comparison** of means and/or variances was required. Whilst this candidate has so done for the first mark, subsequent statements are incorrect conclusions.

Q	Solution	Marks	Total	Comments
7(a)	$R \sim B(50, 0.15)$			
(i)	P(R < 10) = 0.791	B1		AWRT (0.7911)
(ii)	$P(5 \le R \le 10) = 0.8801 \text{ or } 0.7911$ (p ₁)	M1		Accept 3 dp accuracy $(1 - p_2) - p_1 \Rightarrow M0 M0 A0$ $p_1 - (1 - p_2) \Rightarrow M1 M0 A0$ only providing result > 0
	minus 0.1121 or 0.2194 (p ₂)	M1		Accept 3 dp accuracy
	= 0.768	A1		AWRT (0.7680)
	or			
	B(50, 0.15) expressions stated for at least 3 terms within $4 \le R \le 10$ gives probability	(M1)		Can be implied by correct answer
	= 0.768	(A2)	4	AWRT
(b)	Confusion of 22, 35, 120 and/or 0.15, 0.06			Do not treat as misreads
(i)	S ~ B(22, 0.06)	M1		Used in (b)(i) as evidenced by any correct binominal term for $S > 0$
	$P(S = 2) = {\binom{22}{2}} (0.06)^2 (0.94)^{20}$	A1		Can be implied by correct answer Ignore any additional terms
	= 0.24 to 0.242	A1	3	AWFW (0.24125)
(ii)	$P(S \ge 1) = 1 - q^{35}$ where $0.84 \le q \le 0.96$	M1 (B1)		Can be implied by correct answer Award for $(0.94)^{35}$ seen in an expression but not if accompanied by a multiplier $\neq 1$
	= 0.885 to 0.89	A1	2	AWFW (0.88532)
(iii)	Mean = np = 120 × 0.94 = 112.8 or 113 If not identified, assume order is μ then σ^2	B1		Either
	Variance = $np(1-p)$ = 120 × 0.94 × 0.06 = 6.76 to 6.78	B1	2	Must clearly state variance value AWFW (6.768)
(iv)	Means are (approximately) the same stated			Must have scored 1st B1 in (iii)
	or Variances are (very) different stated	B1		Must have scored 2 nd B1 in (iii)
	Agree with P(sorts letter incorrectly) = 0.06	B1 dep		Dependent on 'means same' stated
	Disagree with independent from letter to letter	B1 dep	3	Dependent on 'variances different' stated
		Total	14	