

Teacher Support Materials 2008

Maths GCE

Paper Reference MD01

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Question 1b

1 Six people, A, B, C, D, E and F, are to be matched to six tasks, 1, 2, 3, 4, 5 and 6.

The following adjacency matrix shows the possible matching of people to tasks.

	Task 1	Task 2	Task 3	Task 4	Task 5	Task 6
A	0	0	1	0	1	1
В	0	1	0	1	0	0
С	0	1	0	0	0	1
D	0	0	0	1	0	0
Ε	1	0	1	0	1	0
F	0	0	0	1	1	0

(a) Show this information on a bipartite graph.

(2 marks)

(b) Initially, *A* is matched to task 3, *B* to task 4, *C* to task 2 and *E* to task 5. From this initial matching, use the maximum matching algorithm to obtain a complete matching. List your complete matching. (5 marks)



Commentary

In all examiners reports it has been highlighted that candidates must clearly show their alternating path. Moreover if they choose to work on their diagram then no more than 1 path should be on a diagram. This' solution' shows a number of arrows on the diagram with **no** clear order shown. The candidate appears to start at vertex1 but it is then unclear how the path follows on. The candidate only scores the mark for the final match

(b)	A3, B4, C2, E5			Initial match
	Start from <i>D</i> , <i>F</i> or 1, 6	M1 M1		1st path must go beyond 2nd 2nd path letter/number eg $D-4(+)B/F$ If working is only on diagram, the path(s) must be clear, and only 1 path per diagram can be credited. If 2 paths shown on one diagram, max
	Accept paths in reverse order D - 4 (+)B - 2 (+) C - 6 F - 5 (+)E - 1 or F - 4(+)B - 2(+)C - 6 D - 4(+)F - 5(+)E - 1	A1 A1		mark M1A1 1st correct path 2nd correct path or F - 5(+)E - 3(+)A - 6 D - 4(+)B - 2(+)C - 6(+)A - 3(+)E - 1
	Match: A3, B2, C6, D4, E1, F5	B1	5	Must be clearly stated or indicated

Question 2

2	(a)	Use indic	a quick so ate the pi	ort to rea vot that	arrange ti you use	he follow at each	wing let pass.	ters into	alphabe	etical order	. You must
			Р	В	М	Ν	J	К	R	D	(5 marks)
	(b)	(i)	Find the ascending	maximı g order	um numb when us	er of sw ing a bu	aps nee bble so	eded to r rt.	earrange	a list of 8	8 numbers into (1 mark)
		(ii)	A list of maximur list of nu	8 numb n numb mbers?	ers was er of swa	rearrang aps was	ed into needed.	ascendir What c	ng order an be d	using a bu educed abo	ubble sort. The original <i>(1 mark)</i>

Student response

$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	
New Sequence = BD J th MN PR	

1 Question number Diginal P5 01) Leave blank 52 ons an B chis My BDStampki Br М N ·• 1-. .² P T k k سنايا بالمعاتي فالبسط R D D P C=63=4 28 bi The original Sequence was 14 verence order ĥ Ь 3ai n-10 ;; **k**y) 1-1 A BODEDEE JA) - 18 19 - bì, A 18 +3152+ R 19 O -2+16 Ć 18 A D F 2+ 18 19 F Ź (-, Η Т T 18 ю tb , 120017 k.

Commentary

This solution shows a lack of understanding of a quicksort. They have started with a pivot of J, perfectly acceptable – although not the best approach. They think that M is before J in the alphabet! On the next line they have chosen to work with the first sublist only – again acceptable. Next line working with the second subset is **ok** apart from their earlier mistake. However they have then ignored working with the the first subset ie B D and moved onto the second subset.

The overall solution has scored the method mark but none of the accuracy marks. The second accuracy mark was achievable if they had considered B D at the appropriate time

Ì	2(a)		Б			Ŧ	17	D	L	141		TT ' '1 ,
		P	В	м	N	J	ĸ	ĸ	D	MI		Using quick sort
		<u>B</u>	М	Ν	J	Κ	D	Ρ	<u>R</u>	A1		First pass (based on their pivot)
		B	<u>M</u>	Ν	J	Κ	D	Ρ	R			
		B	J	Κ	D	Μ	<u>N</u>	Р	R	A1		A correct third pass
		B	<u>D</u>	l	<u>K</u>	Μ	Ν	Р	R	A1		All passes correct
										B1	5	Consistent pivots clearly labelled (at least three passes)
	(b)(i)	28								B1	1	
	(ii)	In rev	verse	order						B1	1	Allow descending
									Total		7	

Question 3b



Student Response

ed ges 3. \mathcal{X} Q îİ _ -7 D Ð 16 ٦ B 7 \sim 8 8 1 \bigcirc Ħ 11 Ş, 0



Commentary

Every year a number of candidates fail to realise the difference between finding a minimum spanning tree and a path through a network. This solution typifies the problem. The candidate has started at *A* and worked through to *H*. It is still possible that these candidates gain some reward as their 'path' is still a spanning tree. Candidates must be aware that both Prim's and Kruskal's algorithm are fundamental parts of the course

3(a)(i)	10	B1	1	
(ii)	n-1	B1	1	
(b)	Condone candidates attempting all of part (b) together / in different order			

Question 4(a)(ii)

4 David, a tourist, wishes to visit five places in Rome: Basilica (B), Coliseum (C), Pantheon (P), Trevi Fountain (T) and Vatican (V). He is to start his tour at one of the places, visit each of the other places, before returning to his starting place.

The table shows the times, in minutes, to travel between these places. David wishes to keep his travelling time to a minimum.

	В	С	Р	Т	V
В	_	43	57	52	18
С	43	_	18	13	56
Р	57	18	_	8	48
Т	52	13	8	_	51
V	18	56	48	51	_

- (a) (i) Find the total travelling time for the tour *TPVBCT*. (1 mark)
 - (ii) Find the total travelling time for David's tour using the nearest neighbour algorithm starting from T. (4 marks)

Student Response



Commentary

Every year in the examiner's report, it is brought to the attention of centres that the nearest neighbour algorithm finds a Tour. This means that a path **returns** to the start vertex. This solution shows the classic mistake. The candidate still scores 1 of the method marks.

4(a)(i)	130	B1	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
(ii)	<i>T P C B V T</i> 8 18 43 18 51	M1 M1	Tour (vertices or edges) starting from T (Letters not numbers) Visits all vertices starting from T
	= 138	A1 B1	Correct order 4

Question 4(b)(i)

(b) (i) By deleting *B*, find a lower bound for the total travelling time for the minimum tour. (5 marks)

Student Response



Commentary

The method of finding lower bounds is still not well understood. Conceptually it is difficult but it is important that centres concentrate on pupils understanding. Having deleted a vertex candidates need to connect the remaining vertices with a minimum spanning tree **not** a tour without the deleted vertex. The solution highlights this error. The candidate has correctly identified the 2 shortest edges from B, but has found a **tour** starting and finishing at T. This makes the idea of adding 2 extra edges bizarre.

(b)(i)		M1		Spanning tree with 3 edges
	PT, CT, PV	A1		Correct
	<i>C</i> •	ml		2 edges from <i>B</i>
	+ 2 shortest from B 43 V 18 B	A1		Correct
	(Lower bound =) 130	A1	5	CSO

Question 5(a)



Student Response

5-0	, add = vertices - A B C D	Å
	AB 300 270 = \$40	
	CD 346 270	_
	AC 300 290 = 580	
		6
	AD 260 = 5 30	\sum
	BC 270	
	10 20 1 5 20 5 24 50	
	19x0 + 5 50 - A450	O

Commentary

When trying to find optimal Chinese postman routes candidates must list the odd vertices, write down possible pairings, evaluate the sums of these pairings and then add the shortest value onto the total of all the edges. This solution is a candidate knowing something about odd vertices but not knowing exactly what to do.

They have found *AB*, *AC* and *AD* without realising that **pairs** of vertices are required. Again in their explanation they have referred to Eulerian without fully understanding the implications.

T	5(a)	Odds A, B, C, D	M1		PI (but A, B, C, D must be mentioned)
			ml		Considering 3 sets of pairings of odd vertices, eg <i>AB</i> with <i>CD</i> etc
		AB + CD = 270 + 270 = 540 $AC + BD = 290 + 290 = 580$ $AD + BC = 260 + 270 = 530$	A2,1,0		A1 for 2 correct, A2 for all correct
		Repeat AD, BC	A1F		Follow through their shortest pairing PI by adding 530 to 1920 Or <i>AEHD</i> or <i>DHEA</i> and <i>BFGC</i> or <i>CGFB</i> listed in any route
		(Length = 1920 + 530 =) 2450 (metres)	B1	6	

Question 6(a)

6	[Figure 1, printed on the insert, is provided for use in this question.]
	A factory makes two types of lock, standard and large, on a particular day.
	On that day:
	the maximum number of standard locks that the factory can make is 100; the maximum number of large locks that the factory can make is 80; the factory must make at least 60 locks in total; the factory must make more large locks than standard locks.
	Each standard lock requires 2 screws and each large lock requires 8 screws, and on that day the factory must use at least 320 screws.
	On that day, the factory makes x standard locks and y large locks.
	Each standard lock costs £1.50 to make and each large lock costs £3 to make.
	The manager of the factory wishes to minimise the cost of making the locks.
	(a) Formulate the manager's situation as a linear programming problem. (5 marks)

Student Response

		Diank
6		
<u> </u>		
a)	$\chi \leq 100$	
	Y 4 80 / /]
	Xtyz 60 /	
	Y7X X	~
	(2x+8y 2320) ⇒ x+44y/2160	\supset
	C = 1.5 x + 35	

Commentary

The question clearly states the variables as x and y. This candidate has chosen to ignore the question and use s and l. This would be acceptable if later these letters were amended to x and y. This candidate was not penalised for notation in the remaining parts of the question Linear programming questions will always be set using x and y as the variables, as the questions will normally require graphical solutions.

Mark Scheme

6(a)	All inequalities must be as below			
	$x \leq 100, y \leq 80$	B1		Both
	$x + y \ge 60$	B1		
	x < y	B1		
	$2x + 8y \ge 320$	B1		OE
	(minimise $C = 1.5x + 3y$	B1	5	

Question 7



Student Response



Commentary

Dijkstra's algorithm is a fundamental topic in Decision 1. Candidates cannot expect to be rewarded if they choose to answer a question by inspection or by complete enumeration. This solution shows a candidate writing down values at vertices with **no** working. The only marks that are available for candidates in this case are the final mark for 43 at H (and a mark for the route, if required)

